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THE PERIODIC AND DYNAMIC STRUCTURE OF CHROMATIN

REFEREES:
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PD DR. KARL ROHR
To life and light!
Summary

The organisation of chromatin is non-random and shows a broad diversity across cell types, developmental stages, and cell cycle stages. During G0 and G1 phase of interphase, chromatin displays a bivalent status. The condensed chromatin (heterochromatin) at the nuclear periphery is mostly associated with low levels of gene expression, while the loosened chromatin (euchromatin) towards the interior of the nucleus is associated with higher gene expression. This quiescent picture of interphase radically changes when the cell cycle progresses toward cell division. Firstly, during S phase, DNA is replicated, and chromatin progressively condenses. This is followed by the G2 phase that shows a compact heterochromatin recruited towards the centre of the nucleus. At the beginning of mitosis, the chromosomes condense with a significant topological change in their organisation and are segregated during the next stages of the cell division. Meiotic chromosomes are also highly condensed as mitotic chromosomes but show a particular functional structure, which prepares germ cells to exchange DNA sequences between their homologous chromosomes to generate diversity. To summarise, chromatin experiences dramatic organisational changes during mitosis and meiosis. These changes in chromatin organisation during the lifetime of a cell show that chromatin is not a static entity but highly dynamic in nature.

For a variety of reasons, conventional light and electron microscopy have not been able to fully capture the finer details of chromatin organisation and dynamics. For a long time, description of the interphase nucleus was limited to delineate the euchromatin-heterochromatin dichotomy or describe some specific nuclear elements such as the nucleolus. Advancements in molecular biology during the last thirty years have brought an immense amount of information about how chromatin is organised and genes are regulated. As a classical example, the globin gene has been shown to display a highly constrained shape forced by chromatin looping that brings the regulatory regions to the promoter of the gene. Nowadays, genomic studies can acquire an immense amount of information regarding chromatin organisation and gene regulation, leaving one with the expectation that structure of individual genes could potentially be described visually if sufficient specificity and resolution were reached. With the advent of various super-resolution methods, in particular, single molecule localisation microscopy (SMLM) based methods and recently developed strategies for labelling DNA, it is now possible
to study chromatin organisation and underlying gene regulatory mechanisms at the nanoscale.

During my PhD, I have analysed a broad range of nuclear phenotypes using SMLM. My analyses contribute to the description of a periodic and dynamic structure of chromatin. Moreover, I have described several elementary chromatin structures that I call chromatin domains, both in interphase and meiosis, that are potentially associated with a local function such as gene activation or silencing.

Firstly with colleagues, I established an experimental setup to study chromatin organisation with single molecule localisation microscopy. I investigated how UV-induced photo-conversion of conventional DNA dyes allows increasing sufficiently the labelling density such that it is possible to study various organisational aspects of chromatin in basal interphase. An adequate imaging protocol has been established to bring DNA minor groove binding dyes such as Hoechst 33258, Hoechst 33342 and DAPI (4’6-diamidino-2-phenylindole) into an efficient blinking state necessary to record single molecule locations with high precision. This method was applied to several cell types to investigate the chromatin organisation during different stages of the cell cycle at the highest resolution currently achievable with light microscopy.

The results show that the method can capture several hierarchical levels of chromatin organisation. In reverse hierarchical order, I could describe previously known chromatin territories of 1000 nm, subchromosomal domains of 500 nm, chromatin domains of 100 to 400 nm (and further sub-categories of active or repressed domains) and chromatin fibres below 100 nm, mostly between 30 to 60 nm. Individual nucleosomal domains are also described, which tend to cluster in batches of 10-15 nucleosomes, a number close to one found in genomic studies upstream to promoter regions. Next, with colleagues, I studied the dynamics of chromatin using stress as a model system. It was found that short-term oxygen and nutrient deprivation provokes chromatin to shrink to a hollow, condensed ring and rod-like configuration, which reverses back to the initial structure when the stress conditions cease. The condensed network of rods and rings interspersed with large, chromatin-sparse nuclear voids were 40-700 nm in dimension, capturing another level of chromatin organisation not described before.

Finally, I explored the unique properties of chromatin during meiosis, which has escaped analysis at the single-molecule level until now. Single molecule analysis revealed unexpected highly recognisable periodic patterns of chromatin. Firstly, I observed that meiotic chromatin show unique clusters of 250 nm diameter along the synaptonemal complex, extended laterally by chromatin fibres forming loops. These clusters show a remarkable periodicity of 500 nm, a pattern possible to spot because of the highly deterministic nature of pachytene chromosomes and the resolution of the experimental setup. Furthermore, guided by genomic data, I selected histone modifications associated with different chromatin states to dissect
the morphology of meiotic chromosomes. I could examine the morphology of these chromosomes into three spatially distinct nanoscale sub-compartments. Histone mark H3K4me3 associated with active chromatin was found in a lateral position, potentially located at the places of de novo double-strand breaks. Repressive histone mark H3K27me3 was shown to display a surprising medial symmetrical and periodic pattern, putatively associated with recombination. Finally, centromeric histone mark H3K9me3 locates at one of meiotic chromosome ends and is potentially associated with repression of repeated regions and pairing of homologous chromosomes at early stages. I summarise these findings in a comprehensive final model.

Overall, I have used new information brought by super-resolution technologies to show the dynamics of chromatin in various processes and novel orders of chromatin compaction, which were not reported previously. Among these new levels of chromatin compaction are the interphase hierarchical chromatin domains, the stress pattern of cells upon oxygen and nutrients deprivation and the novel epigenetic domains found at pachytene stage of meiosis. These architectures show that the organisation of chromatin is more complex than thought before, dynamic in nature and shows a high order of periodicity. Further investigation is, therefore, necessary to understand how chromatin transits from a 'beads-on-string' model to the intermediary chromatin domains and finally to the commonly observed X-shaped chromosomes.
Zusammenfassung


Weiterhin untersuchte ich zusammen mit Kollegen die Dynamik von Chromatin unter Einfluss von „Stress“. Wir fanden heraus, dass kurzzeitiger Sauerstoff- und Nährstoffentzug Chromatin dazu anlässst, sich zu einem hohlen, kondensierten Ring sowie zu stabähnlichen Konfigurationen zusammenzuziehen, wobei diese Chromatinkonfigurationen zur Ausgangsstruktur zurückkehren nachdem die Stressbedingungen enden.

Das kondensierte Netzwerk aus Stäbchen und Ringen ist mit großen, chromatinarmen nuklearen Hohlräumen von 40-700 nm Durchmesser durchsetzt, was eine weitere Ebene an zuvor unbeschriebener Chromatinorganisation darstellt.

Durchmesser entlang des synaptonemalen Komplexes aufweist, welche lateral von schleifenformenden Chromatinfasern erweitert werden.


Weitere Untersuchungen sind daher notwendig um zu verstehen, wie Chromatin von einem Perlenschnurmodell zu intermediären Chromatinmänenen und abschließend zu den gemeinhin beobachteten X-förmigen Chromosomen wechselt.
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<td>µm</td>
<td>Micrometer</td>
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<tr>
<td>3D</td>
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<td>Ac</td>
<td>Acetylation</td>
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<td>AFM</td>
<td>Atom force microscopy</td>
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<td>BALM</td>
<td>Binding-activated localisation microscopy</td>
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<td>BaLM</td>
<td>Bleaching/blinking assisted localisation microscopy</td>
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<tr>
<td>bp</td>
<td>Base pair</td>
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<tr>
<td>CCD</td>
<td>Charge coupled device</td>
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<td>CLSM</td>
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<td>Cyanine 5</td>
</tr>
<tr>
<td>DAPI</td>
<td>4',6-diamidino-2-phenylindole</td>
</tr>
<tr>
<td>ddNTP</td>
<td>Deoxynucleotide</td>
</tr>
<tr>
<td>DNA</td>
<td>Deoxyribonucleic acid</td>
</tr>
<tr>
<td>DSB</td>
<td>Double strand break</td>
</tr>
<tr>
<td>EdU</td>
<td>5-ethynyl-2'-deoxyuridine</td>
</tr>
<tr>
<td>EM</td>
<td>Electron microscopy</td>
</tr>
<tr>
<td>emGFP</td>
<td>Emerald green fluorescent protein</td>
</tr>
<tr>
<td>FISH</td>
<td>Fluorescence in situ hybridization</td>
</tr>
<tr>
<td>fPALM</td>
<td>Fluorescence photo-activated localization microscopy</td>
</tr>
<tr>
<td>fps</td>
<td>Frames per second</td>
</tr>
<tr>
<td>FRC</td>
<td>Fourier ring correlation</td>
</tr>
<tr>
<td>FRET</td>
<td>Fluorescence resonance energy transfer</td>
</tr>
<tr>
<td>FWHM</td>
<td>Full width at half maximum</td>
</tr>
<tr>
<td>GFP</td>
<td>Green fluorescent protein</td>
</tr>
<tr>
<td>H2B</td>
<td>Histone 2B</td>
</tr>
<tr>
<td>H3</td>
<td>Histone 3</td>
</tr>
<tr>
<td>H3K9ac</td>
<td>Histone 3 lysine 9 acetylation</td>
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<tr>
<td>H3K14ac</td>
<td>Histone 3 lysine 14 acetylation</td>
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<tr>
<td>H3K27ac</td>
<td>Histone 3 lysine 27 acetylation</td>
</tr>
<tr>
<td>H3K27me3</td>
<td>Histone 3 lysine 27 tri-methylation</td>
</tr>
<tr>
<td>H3K4me1</td>
<td>Histone 3 lysine 4 mono-methylation</td>
</tr>
<tr>
<td>Acronym</td>
<td>Full Term</td>
</tr>
<tr>
<td>---------</td>
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</tr>
<tr>
<td>H3K4me2</td>
<td>Histone 3 lysine 4 di-methylation</td>
</tr>
<tr>
<td>H3K4me3</td>
<td>Histone 3 lysine 4 tri-methylation</td>
</tr>
<tr>
<td>H3K9me3</td>
<td>Histone 3 lysine 9 tri-methylation</td>
</tr>
<tr>
<td>H4</td>
<td>Histone 4</td>
</tr>
<tr>
<td>HAT</td>
<td>Histone acetyl-transferase</td>
</tr>
<tr>
<td>HDAC</td>
<td>Histone deacetylase</td>
</tr>
<tr>
<td>HL-1</td>
<td>Cardiomyocyte cell line</td>
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<tr>
<td>iPALM</td>
<td>Interference photo-activated localization microscopy</td>
</tr>
<tr>
<td>kb</td>
<td>Kilobase</td>
</tr>
<tr>
<td>kDa</td>
<td>Kilodalton</td>
</tr>
<tr>
<td>LBC</td>
<td>Lampbrush chromosome</td>
</tr>
<tr>
<td>LCR</td>
<td>Locus control region</td>
</tr>
<tr>
<td>LM</td>
<td>Light microscopy</td>
</tr>
<tr>
<td>LSM</td>
<td>Least-squares method</td>
</tr>
<tr>
<td>LTR</td>
<td>Long terminal repeat</td>
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<tr>
<td>Mb</td>
<td>Megabase</td>
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<tr>
<td>Me</td>
<td>Methylation</td>
</tr>
<tr>
<td>MEA</td>
<td>Monoethanolamine</td>
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<tr>
<td>MLE</td>
<td>Maximum likelihood estimation</td>
</tr>
<tr>
<td>mRNA</td>
<td>Messenger RNA</td>
</tr>
<tr>
<td>MSC</td>
<td>Mesenchymal stem cell</td>
</tr>
<tr>
<td>NA</td>
<td>Numerical aperture</td>
</tr>
<tr>
<td>nm</td>
<td>Nanometer</td>
</tr>
<tr>
<td>NND</td>
<td>Nearest neighbour distance</td>
</tr>
<tr>
<td>OND</td>
<td>Oxygen and nutrient deprivation</td>
</tr>
<tr>
<td>OTF</td>
<td>Optical transfer function</td>
</tr>
<tr>
<td>P</td>
<td>Phosphorylation</td>
</tr>
<tr>
<td>PALM</td>
<td>Photo-activated localization microscopy</td>
</tr>
<tr>
<td>PBS</td>
<td>Phosphate buffered saline</td>
</tr>
<tr>
<td>PDC</td>
<td>Pixel density classifier</td>
</tr>
<tr>
<td>Pixel</td>
<td>Picture element</td>
</tr>
<tr>
<td>Pol II</td>
<td>Polymerase II</td>
</tr>
<tr>
<td>Pol II Ser2P</td>
<td>Polymerase II serine 2 phosphorylation</td>
</tr>
<tr>
<td>PRDM9</td>
<td>PR domain zinc finger protein 9</td>
</tr>
<tr>
<td>PSF</td>
<td>Point spread function</td>
</tr>
<tr>
<td>PTM</td>
<td>Post-translational modification</td>
</tr>
<tr>
<td>R</td>
<td>Arginine</td>
</tr>
<tr>
<td>RNA</td>
<td>Ribonucleic acid</td>
</tr>
<tr>
<td>ROI</td>
<td>Region of interest</td>
</tr>
<tr>
<td>ROS</td>
<td>Reactive oxygen species</td>
</tr>
<tr>
<td>rRNA</td>
<td>Ribosomal RNA</td>
</tr>
<tr>
<td>S</td>
<td>Serine</td>
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<tr>
<td>S phase</td>
<td>Synthesis phase</td>
</tr>
<tr>
<td>SC</td>
<td>Synaptonemal complex</td>
</tr>
<tr>
<td>SYCP</td>
<td>Synaptonemal complex proteins</td>
</tr>
<tr>
<td>SEM</td>
<td>Scanning electron microscopy</td>
</tr>
<tr>
<td>SIM</td>
<td>Structured illumination microscopy</td>
</tr>
<tr>
<td>SMLM</td>
<td>Single molecule localization microscopy</td>
</tr>
<tr>
<td>SNR</td>
<td>Signal-to-noise ratio</td>
</tr>
<tr>
<td>Term</td>
<td>Definition</td>
</tr>
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<td>-------</td>
<td>------------------------------------------------</td>
</tr>
<tr>
<td>SPDM</td>
<td>Spectral precision distance microscopy</td>
</tr>
<tr>
<td>STED</td>
<td>Stimulated emission depletion</td>
</tr>
<tr>
<td>STORM</td>
<td>Stochastic optical reconstruction microscopy</td>
</tr>
<tr>
<td>Su</td>
<td>Sumoylation</td>
</tr>
<tr>
<td>TAD</td>
<td>Topologically associating domain</td>
</tr>
<tr>
<td>TALE</td>
<td>Transcription activator-like effectors</td>
</tr>
<tr>
<td>TEM</td>
<td>Transmission electron microscopy</td>
</tr>
<tr>
<td>TIRF</td>
<td>Total internal reflection fluorescence</td>
</tr>
<tr>
<td>tRNA</td>
<td>Transfer RNA</td>
</tr>
<tr>
<td>TSS</td>
<td>Transcription start site</td>
</tr>
<tr>
<td>Ub</td>
<td>Ubiquitination</td>
</tr>
<tr>
<td>UV</td>
<td>Ultra-violet</td>
</tr>
<tr>
<td>VH7</td>
<td>A human fibroblast cell line</td>
</tr>
<tr>
<td>VV</td>
<td>Vybrant DyeCycle Violet</td>
</tr>
<tr>
<td>Y</td>
<td>Tyrosine</td>
</tr>
<tr>
<td>YFP</td>
<td>Yellow fluorescent protein</td>
</tr>
<tr>
<td>YOYO-1</td>
<td>A tetracation homodimer of Oxazole yellow</td>
</tr>
</tbody>
</table>
Preface

This thesis is a mixture of a bit of history, a bit of theory, a bit of technical literature, accidental findings, unconventional hypothesis and a series of re-re-writing experiences. Thesis writing is a special experience and as my friend David Fournier would say, one should embrace the opportunity to write a monograph in order to look back on your work and think about its implications. Also, there is a difference between being merely able to fit some 100 figures and 50000 words to compile a thesis without any lore, rhythm or rhyme, and synthesizing a good design with previous facts and fresh analysis to fit a particular purpose. One of the good things about scientific lore is that it lives in heart of the reader for a longer time than an accumulation of facts written within the strict bounds of modern day scientific writing.

Outline of the thesis

In chapter 1, I present a brief historical overview of chromatin research. While writing this chapter, I got reminded about the following quote from G.H. Hardy

"Statesmen despise publicists, painters despise art-critics, and physiologists, physicists, or mathematicians have usually similar feelings: there is no scorn more profound, or on the whole more justifiable, than that of the men who make for the men who explain. Exposition, criticism, appreciation, is work for second-rate minds."

Indeed it was an unusual feeling to write a historical briefing and comment on other people’s work. But contrary to what Hardy says, it was a wonderful learning experience on how chromatin biology has evolved over the years and how new techniques are reconfirming the old findings. It also provided me with a good insight regarding the problems to attack in the future.

In chapter 2, I discuss the design and development of single molecule imaging system to study chromatin architecture with conventional DNA dyes. Furthermore, basics of single molecule localisation microscopy (SMLM) and various elements involved in processing and analysis of single molecule data are discussed.

In chapter 3, I discuss spatial and temporal aspect of chromatin organisation from three viewpoints: basic building blocks, function and dynamics. In particularly, some recent data from SMLM have shown new orders of chromatin never imaged before, the so-called
chromatin domains, an order of compaction of chromatin between the chromatin fibre and the chromosomal territory. These domains are most likely associated to function, either activation or repression of genes. I connect these different features to show how the novel building blocks or patterns can be the result of differential compaction of chromatin as function of various proteins associated with chromatin. One major finding presented here is the ring and rod like shapes chromosomes form when put under stress. Interestingly, it seems that stress is the fastest way to bring two homologous chromosomes together.

In chapter 4, I present the epigenetic make-up of meiotic chromosomes. The periodic and symmetrical organisation of pachytene chromosomes makes me believe that simple mathematical principles lie underneath the seemingly complex looking genome organisation. The challenge is to figure out how various mathematical shapes and curves like conical helices and spirals can combine into one structure that could help chromatin avoid entanglements during assembly and disassembly process. Nevertheless, I propose a model for pairing of homologous chromosomes based on coupling of snakes. I hope with major future advancements in imaging, one will be able to see the live pairing of homologous chromosomes.

In chapter 5, I summarise the major findings of this thesis and put forward some new theories in the spirit of the following quote by Imre Lakatos and discuss some possible future research directions in chromatin biology. "Where theory lags behind the facts, we are dealing with miserable degenerating research programmes".

**Contributions of the thesis**

The main contributions of the thesis are summarized below.

1. **SMLM of DNA dyes**: Initiation of the project and design of the experiments. Observation of the blinking property of minor groove DNA dyes making them applicable for single molecule imaging. Contribution to the development of the optical setup. Adapting the existing post processing algorithms to reconstruct the data done by this method. Development of new algorithms to analyse and calibrate the data (Szczurek*, Prakash*, Lee* et al. 2014; Żurek-Biesiada, Szczurek, Prakash et al. 2015; Żurek-Biesiada, Szczurek, Prakash et al. 2016; this thesis). *: equal contributions.

2. **Structure of interphase chromatin**: Application of SMLM of DNA dyes to study the architecture of interphase chromatin at several structural levels, including chromatin domains and nucleosome domains. Development of algorithms to quantify and characterise chromatin states (Szczurek*, Prakash*, Lee* et al. 2014; Żurek-Biesiada, Szczurek, Prakash et al. 2015; this thesis). *: equal contributions.

3. **Mechanisms of chromatin condensation and reversibility upon stress**: Development of new algorithms to quantify and analyse
chromatin contraction and relaxation (Kirmes*, Szczurek*, Prakash et al. 2015; this thesis). *: equal contributions.

4. Epigenetic landscape of meiotic chromosomes: Initiation of the project and design of the experiments. First super-resolution images of chromatin during meiosis. Application of single molecule auto-correlation to describe periodic clusters of chromatin along the pachytene chromosome. Development of a method to predict chromatin compartments based on post-translational histone modifications. (Prakash et al. 2015; this thesis).


A detailed description of publications listed here can be found at the publication section of the thesis. All figures from previous studies presented here are reproduced according to publisher guidelines and permission policies.

An apology of a stargazing scientist

As a beginner and over-enthusiastic scientist, I might have come up with unconventional hypothesis or speculated a bit too much at certain places or missed some of the important works on chromatin research. The topics covered are quite broad and I do not pretend to have expertise in all areas of chromatin biology.

This thesis is my attempt to provide a brief historical account of chromatin research, basics of localisation microscopy, systematic characterisation of interphase and meiotic chromosomes based on my current knowledge and level of expertise. Thus, it is likely that such a work might open doors for some trivial mistakes. Nonetheless, I hope that this months long intellectual pursuit to decipher the various spatial and functional aspects of chromatin organisation helps in advancing the field.
A Condensed History of Chromatin Research

The cell nucleus is a discernible cellular compartment, where the expression and regulation of genes take place. Due to limited tools and methods, it remained ignored for a long time (until the late 19th century), however nowadays it is a major research topic. The structure of DNA and in-depth study of the nucleus composition has shown that the DNA is heavily constrained by proteins either modulating gene expression or devoted to shaping DNA into various topological structures such as loops and globules. The DNA with all other associated protein machinery and RNA is referred to as chromatin.

For the most part, chromatin research has highly depended on the advancements of microscopy, from the early days of conventional light and electron microscopy of the cell nucleus to the recent advanced high-resolution and live imaging methods. Much more recently, chromatin research has gained a lot from experiments which have tried to map chromatin in 3D inside the cell nucleus to conclude that it is organised in distinct territories. This, essentially, is the story told in the present chapter.

1.1 The early research on the nucleus and chromatin

The nucleus was described for the first time as early as the eighteen century by Antonie van Leeuwenhoek in the nucleated blood cells of salmon. For a long time between the late 17th century and the first thirty years of the 18th, it was at best described as a vesicle and did not show much complexity than the name suggests. Felice Fontana in 1781 describes the first sub-structure in a nucleus of a skin cell from an eel, probably a nucleolus [Baker, 1949]. The power of a good drawing is illustrated by Johann Evangelist Purkyně [Purkyně, 1830], where he presents the germinal vesicle of the hen egg (see Figure 1.1). He comments as follows: "Thus the scar [germinal disk] of the ovarian egg contains a special part, peculiar to itself, a vesicle of the shape of a somewhat compressed sphere. This vesicle is limited by a very delicate membrane and filled with a special fluid, perhaps connected with procreation (for which reason I might call it the germinal vesicle); it is sunk into a white breast-shaped projection composed of globules and perforated in the middle" according to John

Figure 1.1: Purkinje drawings of the germinal vesicle of a hen egg. Reproduced from the main set of figures in [Purkyně, 1830].

1 Antonie van Leeuwenhoek (1632—1723), a Dutch scientist who discovered micro-organisms by developing sophisticated microscopes. Considered to be the Father of Microbiology.

2 Felice Fontana (1730—1805), an Italian scientist, considered to be the father of modern toxicology.

3 Johann Evangelist Purkyně (1787—1869), Czech physiologist. His broad contributions touch neurophysiology, reproduction research, physiology of the vision, pharmacological properties of plants and study of cell composition.
Baker’s translation from Latin [Baker, 1949].

As Baker points out, the nuclear envelope and the nucleoplasm are described here for the first time. This first comprehensible picture of a nucleus also brought the first sound hypothesis regarding the function of the nucleus, a “connection with procreation”, exemplifying the need to find quality signals in biology, and so proper animal or cellular models with extraordinary properties. As a consequence, at one glance, one understands what the structure looks like, and what it can do.

Though the nucleus was observed early, its function remained unexplored for a long time. One of the initial hypothesis (~ 1850) stated that nucleus could be the place where new cells emerge [Baker, 1949]. These studies used optical microscopy and were mainly morphological. Mitotic chromosomes, which are easy to observe under a microscope, captured the focus of many researchers and were the only nuclear component to be studied for a long time. Interphase chromosomes, at that time, were considered only by a handful of scientists, among them Theodor Boveri [Boveri, 1888]. The habit to consider only mitosis is also exemplified by modern textbooks, which often present the mitotic chromosomes (highest level in the hierarchy of chromatin compaction) after the initial beads-on-the-string and 30 nm chromatin fibre for the organisation of DNA (Figure 1.2). Interphase chromatin is obviously not organized in X-shape chromosomes and is much more complex.

In the second part of the 19th century, chromatin research was mainly focused on the chemical quantification of nucleic acids and the fractionation of nuclear proteins. The point of view of chemists was slightly different from that of 18th and early 19th century biologists. Most of them wanted to describe the chemical composition of the cell exhaustively. One of them, Friedrich Miescher, decided to do so for immune cells. In 1869, while studying in Tuebingen, he discovered a substance in pure leukocyte solution which caused the nucleus to swallow and explode upon mild injections of an alkaline solution. He found this substance to have a high phosphate proportion and called it nuclein, in reference to its nuclear localization; and later called it nucleic acid [Miescher, 1871, 1874, 1897, Kossel and Kennaway, 1911, Kossel, 1883, 1884] (for detail see [Dahm, 2008]). Later, Albrecht Kossel determined the composition of DNA to be a mixture of adenine, cytosine, guanine and thymine, an important step to understand how information is stored in the DNA molecule [Kossel and Kennaway, 1911, Kossel, 1883, 1884].

1.2 Chromatin bares information: the chromosomes and genes era (1870—1945)

Ernst Haeckel proposed that the nucleus contains factors responsible for heredity (1866). Miescher is the first to have postulated a nuclear origin of a cellular functions, the motion of sperm, though without providing hints about the mechanism [Miescher, 1874, Dahm, 2008].

Figure 1.2: Sketch of a cell: On the left, a cell prior to mitosis. On the right, two sister cells coming from the same mitotic event [Flemming, 1882] (citation inspired by [Cremer and Cremer, 2009b]).

4 Theodor Boveri (1862—1915), German biologist, first to propose that chromosomes occupy distinct territories inside of the cell nucleus. Also known for the Boveri-Sutton chromosome theory and the discovery of the centrosome.

5 Friedrich Miescher (1844—1895), Swiss physician and biologist, most noted for his work on isolation and identification of nucleic acids.

6 Albrecht Kossel (1853—1927), German biochemist, who pioneered the work in the field of genetics. He was awarded the Nobel Prize in Physiology or Medicine in 1910 for the discovery of the five fundamental nucleic bases that constitute nucleic acids: adenine, thymine, guanine, cytosine and uracil.

7 Ernst Haeckel (1834—1919), German biologist known for establishing the first phylogenetic tree of all living forms and for establishing a relation between development and evolution (ontogeny recapitulates phylogeny).
During the second half of the 19th century, probably the most famous work on nuclear functionality [Hertwig, 1875] was conducted by Oscar Hertwig and Richard Hertwig. Oscar Hertwig, using the sea urchin as a model, showed that a male and a female germ cell merge to form the egg [Hertwig, 1875]. Moreover, he showed that organisms come from one cell, leaving biologists with the very complex task of explaining the mechanism of development. Oscar Hertwig’s observations led to the first proof that a nucleus is a place that stores some information.

An interesting point to note is that the Hertwig brothers carried out their initial work at Jena, where Ernst Abbe was pioneering the work in optics, lens design and microscopy around the same time. As optical technology was still limited at the end of the nineteenth century, knowledge about chromatin function was restricted to the description of the metaphase chromosomes and the characterization of chemical composition. Though chromosomes themselves were observed by several scientists in the first half of the nineteenth century, it is only in 1882 that they were associated with mitosis. In a famous work, Walther Flemming described the content of the nucleus under the term chromatin for the first time (Figure 1.2).

After the works of Flemming and others, the mitosis begins to get the focus of the biologists. The nucleus was rapidly hypothesised to be one of the factors where hereditary information can potentially be stored and transmitted to daughter cells. As such, Wilhelm Roux in 1883 said that there is not only a question of quantity in mitosis (meaning that both daughter cells will inherit the same amount of chromatin), but there is also a question of quality (not all chromatin is equivalent), which supposes that all granules of chromatin have different functions. Around the same time, the work of Oscar Hertwig was prolonged by August Weismann germ plasm theory. Weismann defined chromosome heredity as the process by which information is transmitted from one generation to the other via chromosomes of the germ lines, based on Hertwig observations that sperm + egg = zygote, a sufficient note to claim that one needs information from two different cells to form a new individual, and that information is exchanged during the merging of the cells (Figure 1.3). Friedrich Miescher, who characterised nucleic acids using nucleus of leukocytes and salmon sperm, hypothesised that information might be stored on this molecule by a change of stereochemistry; during fecundation, each gamete will contribute with a molecule of a different state to combine in the nucleus of the fertilised egg [Miescher, 1897].

Theodor Boveri and Walter Sutton were the first scientists to establish a link between chromosomes dynamics during mitosis and Mendel’s laws of heredity. According to their theories, there must be entities that are passed differently to the next generation (genes, though the term is coined later in history; see [Boveri, 1904, 1909]).

8 Oscar Hertwig (1849—1922), German zoologist, the first to describe fecundation as the merging of a sperm and an egg.
9 Richard Hertwig (1850—1937), German zoologist known for his work on protists and the relationship between the nucleus and the plasma as well as for his work on meiosis and fecundation.

10 Ernst Abbe (1840—1905), German physicist, a major innovator of modern microscopy. Abbe’s innovations in optics led to great improvements in microscope design and understanding of resolution limits of light microscopy.
11 One wonders to which extent advancements in chromatin biology research have depended on progress in optics and microscopy.
12 Walther Flemming (1843—1905), German biologist, who discovered mitosis.
13 Wilhelm Roux (1850—1924), German zoologist, early embryologist, known for studying the outcome of provoked developmental defects.
14 August Weismann (1834—1914), German evolutionary biologist, known for the germ plasm theory.
15 According to the theory genetic inheritance takes place via germ cells such as egg and sperm cells. Other cells such as somatic cells do not transmit hereditary information to the next generation.
16 Walter Sutton (1877—1916), American geneticist, who contributed to discover that chromosomes inheritance follow the laws of Mendel.
17 Gregor Mendel (1822—1984), German scientist, who discovered fundamental laws of heredity through his experiments on pea plants.
Later, Thomas Morgan\(^8\) was the leading player in the discovery of genes. As a result, he is considered as the founder of the field of genetics. Along with Hugo De Vries\(^9\) and others, he proved that chromosome regions bare information that is variable in different organisms and can be transmitted to next generation. To achieve this, he provoked mutations in flies using irradiations. After proving that the provoked mutations can be inherited, he found that the transmission of certain mutations depends on the gender of the carrier and so, on the presence of the X chromosome. Knowing that the presence of genes on the X chromosome could be shown by this method, Morgan performed appropriate cross-breeding. By examining the phenotypes of the following generations, he could determine if two alleles recombine together more often than predicted by chance, which probably means that the distance between them on the chromosome has an influence on the probability to recombine. The further apart, more likely the recombination of genes will be. This rational was the base for designing experiments leading to a first genetic map, for the X chromosome of Drosophila [Strutevant, 1913].

The earliest visualisation of functional sub-chromosomal structures was done on pachytene stage chromosomes by August Weismann in 1913. Images pointed at prominent bulky regions, regularly spread along the chromosomes, which are probably equivalent to chromatin clusters recently observed in meiosis (see chapter 4 and [Prakash et al., 2015]). Phoebus Levene\(^20\) in 1929 characterised the composition of DNA and found that DNA contained nucleic bases (already identified previously by Kossel), deoxyribose, and a phosphate group. It was much later proven by Chargaff that adenine:thymine and cytosine:guanine ratios were 1:1 [Chargaff et al., 1952].

In 1944, one of the most important experiments in molecular biology, known as Avery—MacLeod—McCarty experiment [Avery et al., 1944], was carried out. The experiment proved that DNA and not proteins carry the information i.e. gene. Another major step was also to show that one gene corresponds to one enzyme (see [Olins and Olins, 2003] for a review).

1.3 Chromatin as a decision center of the cellular factory: the golden age of molecular biology and electron microscopy (1944-1980)

The fifties and the sixties experienced the emergence of molecular biology and the electron microscopy (EM) as methods to explore the way the nucleus responds to the environment and uses its internal program to maintain the survival of the cell. Before the fifties, the description of chromatin was very shallow. On one hand, chemistry had revealed the composition of the nucleus; on another hand, the optical description of chromatin was limited to individual sub-structures, such as the nucleolus or Cajal bodies. Genes had been described indirectly; polytene chromosomes of Drosophila had been characterised

-- Thomas Morgan (1866—1945), American embryologist, who discovered that traits transmitted to the next generation are coded by certain regions on chromosomes, the so-called genes.
-- Hugo De Vries (1848—1935), Dutch botanist who introduced the concept of genes and mutation, which he incorporated in an updated theory of evolution.

-- Phoebus Levene (1863—1940), American biochemist who characterized DNA composition as a mixture of nucleic bases, sugars and phosphate groups.
by autoradiography [Ficq and Pavan, 1957, Lewis, 1945]. Nevertheless, beyond the level of basic chemical compounds and the genetic bands of Drosophila, not much was known about the various regulatory processes happening inside the nucleus, especially in the interphase. Molecular biology has emerged in the middle of the 20th century as an attempt to describe this complexity and bridge the gap between basic chemical assays and visual description of chromatin. This will be achieved mostly by experimental evidence but also by modelling. Prompted by research and thoughts from physicians Niels Bohr21 and Erwin Schrödinger22, who saw that the basic laws of physics have to be at the basis of all living forms, many biologists started to use models to address new questions.

The most famous paper of the twentieth century in the field of biology is the 1953 model of DNA by Watson and Crick published in journal Nature ([Watson et al., 1953] and Figure 1.4). According to him, James Watson23 was inspired by the reading of Schrödinger essay "What is life" [Schrödinger, 1945] in choosing his post-doctoral topic which was on the structure of DNA. In the early fifties, many people, including Linus Pauling24, who had already modelled the alpha-helix of proteins [Pauling et al., 1951], came with the idea that the DNA molecule could be modelled. An earlier hypothesis had claimed that the structure could be a helix, which Pauling falsely thought to be triple [Pauling and Corey, 1953]. Based on experimental evidence from Franklin, Watson along with his collaborator Francis Crick, designed a double helical structure for DNA [Watson et al., 1953]. The model explained how the main components of DNA are placed toward each other: two strands of DNA made of alternating deoxyribose and phosphate, interact via nucleic bases bound to their respective deoxyribose, similarly to the zip of a jacket. The idea of base pairing came from brand new evidence from Erwin Chargaff, who showed that adenine: thymine and cytosine : guanine are 1:1 ratios [Chargaff et al., 1952]. The fantastic model of Watson and Crick revealed how a genetic vocabulary is possible by a combination of nucleic bases and how it can be inherited, by duplication of available information. It also showed how modelling is crucial to biology and how the vision is as important as the data themselves.

This finding prompted many subsequent central questions of biology. At that time, where DNA was freshly known to bare information in the cell, the issue that was slowly arising was how information bared by DNA turns into proteins. The correspondence saying that one gene corresponds to one enzyme had just been postulated [Beadle and Tatum, 1941]. Following Watson and Crick publication, George Gamov25 postulated that a minimum of 3 nucleotides is necessary to code the 20 amino acids; later experiments by Crick showed that this prediction was true [Crick et al., 1961].

21 Niels Bohr (1885—1962), Danish physicist, famous for a model of the atom where electron can transit between orbitals, and for an early quantum theory describing these transitions.

22 Erwin Schrödinger (1887—1961), Austrian physicist, made fundamental contributions to the field of quantum theory.

23 James Watson (1928—), American molecular biologist and visionary, co-discoverer of the structure of DNA with Francis Crick, co-discoverer of mRNA and early promoter of the human genome project.

24 Linus Pauling (1901—1994), American chemist who made several important contribution to biochemistry, discovering the structure of the alpha-helix and contributing to the study of genetic diseases.

25 George Gamow ( 1904— 1968), Russian theoretical physicist and cosmologist, who made some fundamental contributions to molecular genetics.
Another set of experiments led to the discovery of messenger RNA, mainly characterized by Watson and colleagues [Watson, 1963], based on ideas of different discussion groups and seminal reflections by Francois Jacob and Jacques Monod. These investigations led to the conclusion that the nucleus has to be an administrative decision centre of the cell, storing information that can be used to respond to cues. A very remarkable ability of the nucleus is to adapt to the signals from the environment.

The pioneer studies of Salvatore Luria, Alfred Hershey and Max Delbrueck in the 40’s, established phage lambda and bacteria models as important platforms to study genes and their regulation. Until the mid-20th century, how genes can be converted to proteins was not understood. Experiments from Jacob and Monod helped to describe such a phenomenon. They showed the existence of activable gene products, proving that genes respond to external cues. Upon presence of sugar, they demonstrated that an intermediary product, moving to the cytoplasm, was transmittable to another bacteria which was not exposed to the initial cue. The famous “operon paper” also hypothesised that these products are RNA [Jacob and Monod, 1961]. RNA polymerase itself was just discovered in 1960 [Hurwitz, 2005].

The first quantification of mRNA produced by the nucleus was done in the group of James Watson, who had also been central in thinking about possible intermediary elements to turn genes into proteins. The earliest sketch drawn showing the transformation of DNA into RNA to protein is from the hand of Watson, in 1959, according to him [Watson, 2012].

Following pioneer works on DNA copying, Frederick Sanger developed a set of techniques to sequence DNA molecules, first published on tRNA [Sanger, 1981]. This led to more efficient procedures, such as the classical Sanger sequencing protocol, which uses dideoxynucleotides (ddNTP) to interrupt copying of the DNA molecules to sequence at different positions.

Aside from the series of experiments that have led to the ‘central dogma’ of biology (genes transfer information to messenger RNA which is used to build protein), the development of the electron microscope has been a major advancement of the century. Conceived to record the differential transmission of an electron canon on a sample preparation, this microscope allows viewing cells at the nanometer resolution. Many compartments have been discovered using EM: the endoplasmic reticulum, the Golgi apparatus, the chloroplast [Porter et al., 1945] by Albert Claude. It has also helped to describe the ultrastructure of the interphase nucleus and distinguish euchromatin (‘active chromatin’) from heterochromatin (‘inactive chromatin’, see Figure 1.5), and describe nuclear pores along with other nuclear structures (see Chapter 1 of [Busch, 1974] for more information). Most importantly, it was crucial to proving that a nascent RNA comes out of pericentric chromatin and that chromosomes in interphase have an inactive region (central) and an active region (pericentric).

In situ hybridization is another area of research that has been deci-
sive for the description and regulation of a gene. The technique was pioneered by Joseph Gall\textsuperscript{32} [Gall, 1968a,b], who developed a method to purify rRNA molecules. Gall and Pardue then applied hybridization to the localisation of repeated elements on the chromosomes and could visualise for the first time nanoscale chromatin features \textit{in situ} [Gall and Pardue, 1969]. This research shows an early attempt to localise structural and functional pattern on chromosomes, though banding on Drosophila chromosomes had already been shown since long.

Electron microscopy, despite limitations due to the low density of certain cellular components and limited assortment in contrasting compounds, has been an immense advancement in biological research during the 20\textsuperscript{th} century. Radioactive probes used in EM preparation have been slowly replaced by confocal imaging, which allows using fluorescence to stain several types of molecules at the same time, without long, sophisticated EM procedures. Experiments in other areas of research have also shown that the specificity of cells phenotypes (i.e. their function) comes from specific genetic programs executed in the nucleus. For instance, a pioneering experiment has been the successful transplantation of a somatic nucleus to an embryonic stem cell by John Gurdon\textsuperscript{33}, which resulted in a healthy production of tadpoles. This proved that the phenotype of a cell depends on the end products of the genetic program, that are mRNA and proteins [Gurdon et al., 1958].

1.4 Chromatin as a highly structured system: genomic data, localisation methods and modelling (1980 onwards)

The research of the 60’s and 70’s had shown many basic principles of the life of a nucleus, the ‘administration centre’ of the cell. In the following decades, research regarding chromatin function and dynamics has started to take off. The central questions in the field of research on the nucleus were: how many genes does it comprise, and what are they doing? Does the chromatin adopt a given architecture in the nucleus? Are chromosomes, transcription machinery, genes, regulators disposed in a certain way or are things close to stochastic? What about the dichotomy euchromatin/heterochromatin revealed by electronic microscopy? Are there other levels of complexity between the nucleosome level and chromatin dichotomy? Finally, can the nuclear centre store information and change its behaviour using past stimuli which are no longer present? This last question, the question of epigenetics, will be treated in the next section.

Describing the diversity of genes present in a nucleus was certainly not a trivial task. Since Sanger first experiments, sequencing was possible, but at a tiny scale. The first automatic sequencer appeared in 1985, with a speed of 3000 nucleotides per day. Knowing that the genome comprises possibly 100,000 genes, with several kilobase pairs long in each case, researchers had to face both an experimental and a computational challenge. Computation would require a high

\textsuperscript{32} Joseph Gall (1928— ), American cell biologist, known for developing \textit{in situ} hybridization and work on repeated genomic regions such as telomeres.

\textsuperscript{33} John Gurdon (1933— ), a British biologist, the pioneer in the field of cellular reprogramming.
number of very fast processors and was not possible at a decent speed before the 1990’s. The first competitive algorithm for high-throughput DNA sequencing, based on graph theory and so on finding the best path to assembling the sequences generated by enzymatic digestion was developed in the early eighties [Kozak, 1984]. Most importantly, the existence of a vast number of repetitive regions will have to be tackled. A large public consortium started to emerge, on the initiative of several prominent scientists such as James Watson. In the late phase of the project, the public consortium was challenged by an independent project generated by Craig Venter. The two projects published the genome draft by one day of interval [Lander et al., 2001, Venter et al., 2001]. The quest was both a biological and a human milestone, revealing the necessity of community effort to produce genome-wide data, a goal achievable in both academics and entrepreneurial environment.

Many insights came from the human genome sequence: a surprisingly low amount of genes (20,000), the prominence of repeated sequences, and the significant number of horizontal transfer events from various organisms, including bacteria. Aside from getting a catalogue of genes, non-coding RNA and repeated elements, information from genomes has also allowed testing many hypotheses at genome-scale, such as identification of genetic mutations, the design of probes to further track sequences or performing site-specific mutations. Following Joseph Gall’s pioneer method, fluorescent probes were designed to target specific genes (Fluorescence in situ hybridization or FISH) [Langer-Safer et al., 1982, Schardin et al., 1985, Lengauer et al., 1992]. FISH has been extensively used to study the regulation of genes in the genome, at given loci. For instance, interaction between genes has been imaged with this technique (‘gene kissing’, [Cremer and Cremer, 2001, 2009b,a]). Important applications of FISH include the technique of chromosome painting, which aims at using enough probes to be able to see most of the spatial occupancy of a given chromosome.

Today, it is no doubt that interphase chromatin is a very complex structure that has a relationship with the structure of chromosome during metaphase. For instance, the genes remain in the same order along the cell cycle. Nevertheless, during the early days of chromatin research, it was thought that chromosomes become fragmented at the end of the mitosis and clusters together to reform chromosomes at the end of the interphase. Two scientists explored the alternative hypothesis, Rabl and Boveri, and guessed that chromosomes kept defined positions during interphase, though in a more sophisticated manner as during mitosis [Boveri, 1888]. This representation of what are now called “chromosome territories” remained marginal for a long time. When the nucleus architecture was better studied using higher levels of magnification, with the advancement of the electron microscopy, interphase nucleus began to be described in terms of condensed and relaxed chromatin, with the idea that the chromosomes where highly untangled in the nucleus, and that their precise indi-

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34 John Craig Venter (1946— ), American biochemist and geneticist, known for contributing to the first sequencing of the human genome.
vidual localisation did not matter. Some isolated authors described possible models looking closer to the modern view on chromosome territories [Pollister, 1952], but the dichotomy hetero/euchromatin prevailed for long. It is only during the late seventies that the idea that interphase chromosomes occupy certain positions or territories in 3D space started to emerge. The concept was in the air but put aside due to experimental limitations for some decades [Comings, 1980].

The first demonstration of the existence of chromosome territories was shown by [Stack et al., 1977] using specific chemical treatments, to make the DNA mass appear wherever it is located in the nucleus. At the same time, other regions of the nucleus became characterised, such as the perichromatin region, shown to be the zone experiencing most of the transcription, splicing and eventually repair events [Cremer et al., 1982a,b]. Recently, more complex models have been proposed to describe the region between the chromosome territories (described in [Fakan, 2004, Cremer et al., 2004]), some hypothesising for separation of chromosomes, other for intermingling [Branco and Pombo, 2006]. These interchromosomal regions can potentially recruit genes from different chromosomes to transcription machineries [Osborne et al., 2004, Chakalova et al., 2005, Lanctôt et al., 2007, Cremer and Cremer, 2009a,b], while some have shown that the number of transcription factories may be very restricted in adult cells (factories are reviewed in [Sutherland and Bickmore, 2009]).

Several levels of chromatin have been modelled in textbook pictures following EM studies (see [Uhlmann, 2014, Ozer et al., 2015] for a summary). Some regions, ‘clumps of chromatin’, presented in [Monneron and Bernhard, 1969] and visible in other studies, are regions of loose chromatin or euchromatin, though their apparent localisation is only related to the concept of chromosome territory since recently [Albiez et al., 2006]. Indeed, for a long time, apart from the euchromatin/heterochromatin dichotomy, high-order chromatin levels have not been considered. Towards the description of potential high-order structures during interphase, in situ hybridization of entire interphase chromosomes is characterised in [Schardin et al., 1985]. Though chromosome territories are established, and active regions either messy [Branco and Pombo, 2006] or confined to specific regions [Cremer and Cremer, 2001], trans-associations between chromosomes are now also known to happen [Spilianakis et al., 2005, Lomvardas et al., 2006].

Increasing complexity of the nucleus has been captured recently using techniques cataloguing interactions between DNA sequences (chromosome conformation capture [Dekker et al., 2002]). Data have shown interchromosomal interactions to happen preferentially in a short range distance, though the two telomeres of a chromosome may be interacting during interphase [Dekker et al., 2002]. Interphase subchromosomal domains (topologically associating domains, chromatin loops, etc.) have emerged progressively as an intermediate between the beads-on-a-string level (see next section on epigenetics) and the chromosome territory. Ma et al. [Ma et al., 1998] attempted to
measure these intermediary levels of complexity via optics before the advent of genomics, hinting for chromosome domains in the range of 1Mb. HiC data [Rao et al., 2014, Lieberman-Aiden et al., 2009] recently helped to refine the picture and describe more complexities in the chromosome territory regions. It only recently occurred to scientists that intermediate levels also exist. Before HiC and other techniques, territories of 1Mb were thought to exist, but only HiC has allowed estimating the distribution of contacts between regions. A more complex picture has come from data showing dynamics of contacts during different phases of the cell cycle [Naumova et al., 2013]. Having achieved wide success in generating significant amounts of genomic data, genomics is awaiting validation from microscopy.

Benefiting from advancements in the area of fluorescence microscopy, which include the discovery of properties of the green fluorescent protein [Prasher et al., 1992], and new theoretical frameworks (see [Betzig, 1995] and chapter 2 of this work), recent improvements in light microscopy [Hell and Wichmann, 1994, Heintzmann and Cremer, 1999, Gustafsson, 2000, Lidke et al., 2005, Betzig et al., 2006, Rust et al., 2006, Hess et al., 2006, Lemmer et al., 2008, Reymann et al., 2008] have allowed studying the cell nucleus at an unprecedented resolution. These new techniques have been extensively used by Thomas and Christoph Cremer to study chromatin patterns in high resolution (Figure 1.6), leading to a drastic improvement of chromatin description. Thank to them, chromosome territories are now well described, and a picture of chromatin structure with fundamental functional building blocks of chromatin of about 100-400 nm starts to emerge. These so-called chromatin domains are either associated with high or low transcription, depending on their low or high compaction state, respectively (see section 3.2.3 on this report, [Prakash et al., 2015, Boettiger et al., 2016]). In case of embryonic cells, these methods have shown that the number of transcription units is much higher than in differentiated cells (i.e. specialized tissues), but surprisingly each of the units contained only one or two molecules (see myoblasts image, Figure 2 in [Smeets et al., 2014]), while in non-specialized cells, the machineries in lower number have a broader range of genes to transcribe.

Finally, the dynamics of chromatin during interphase is emerging as a new focus for modelling biological processes. Stimulus-induced chromatin changes have been most of the work on dynamics of chromatin in the pre-genomics area [Jacob and Monod, 1961]. Stimulation by UV was shown to decrease chromatin extractability, or in more modern words, accessibility [Smith, 1962]. UV has also shown to induce changes in chromatin localization [Cremer et al., 1982a,b]. Movements of chromatin as a possible way to regulate genes has emerged during the seventies, with concepts such as nuclear matrix [Berezney and Coffey, 1976]. Understanding the dynamics of nuclear architecture during development has progressed a lot using band painting, to monitor the transition between interphase and mitosis and find relationship between defined chromosome positions

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35 Nuclear matrix: nuclear cytoskeleton thought to be involved in chromatin dynamics.
in mitosis and the distribution of chromosomes in 3D space during interphase. Contraction and relaxation of chromatin has also captured attention to study the relationship between structure of chromatin and regulation of gene expression [Shilatifard, 2006]. Recently, application of FRAP has helped to study chromatin dynamics happening in the nucleus (see original method in [Axelrod et al., 1976]).

1.5 The substratum of chromatin memory: epigenetic regulation

The works presented in the previous section have shown that the nucleus contains DNA molecules baring information through a vocabulary of genes, coding for proteins and that this information can be used to respond to external clues. This was a major focus of early molecular biology. In the following decades, up to now, the study of genes and genomes has continuously occupied a prominent place. Nevertheless, researchers have become increasingly aware that genes are not all transcribed at the same time and that the genome needs to modulate their response in space and time. On top of this, it has become more explicit that the spatial disposition of chromatin within the nucleus is essential to modulate the response of the cell to environmental cues. This modulation will be shown to happen through modification of bases of the DNA as well as histone modifications, between other mechanisms summarised under the epithet of epigenetics.

What remains from Jean-Baptiste Lamarck is probably the transmission of information between cells during development, rather than between organisms. Nevertheless, the first statement that can be recognized as an indirect reference to a potential epigenetic regulation of chromatin in a modern sense is the hierarchy of cells during development: "During each cell division on the way from a fertilized egg to an entire organism, each daughter cells obtains one-half of the idioplasm according to mass, but not necessarily according to its quality" [Weismann, 1892, Cremer and Cremer, 2009b]. This is close to the definition of epigenetics. The importance of epigenetics for transcription was taken into account very early in the development of molecular biology. Since the discovery of chromatin and first characterisation of its composition in the nineteenth century, a community of researchers was specifically devoted to study nuclear proteins and their biological importance. Biochemists were nevertheless quite separate from molecular biologists, the latter more focused on high-order processes, while biochemists and chemists by definition focused on the lower scales, on entities such as nucleic acids or enzymes [Hurvitz, 2005]. The composition of histone became characterised in great details by biochemists [Stedman and Stedman, 1951]. They helped to show that histones can inhibit the work of RNA polymerases, and hypothesised that they have a role in compaction.

Biochemical analysis had shown that histones can be acetylated or methylated, an observation relatively easy to obtain given the small size of the proteins. A relationship between this post-translational
modification (both acetylation and methylation) and gene transcription was described very soon after the theorization of messenger RNA [Allfrey et al., 1964]. Allfrey and colleagues showed that upon mild acetylation, histone proteins lose their capacity to inhibit the work of RNA polymerase. In the seventies, the first EM images of nucleosomes were published and revealed the nanoscale structure of chromatin (Figure 1.7).

Histone modifications and DNA methylation were later shown to recruit factors. In this last case, the first proof of DNA methylation binding protein was presented by [Meehan et al., 1989], a study showing for the first time a protein binding methylated CG dinucleotides. Another important notion of chromatin architecture and its accessibility stems in the historical dichotomy between euchromatin and heterochromatin. More recent works have proven that epigenetic marks (acetylations or methylations) are not evenly distributed in the chromatin and that one can find marks associated with regions visually more condensed and others to regions more relaxed. Findings from recent superresolution experiments have helped to describe epigenetic patterns in interphase for active and inactive X chromosomes, showing that clusters of activating and inactivating histone modifications anti-correlate [Zinner et al., 2007, Cremer et al., 2015]. These findings have confirmed patterns already found previously in mitosis or using assays such as ChIP-seq [Barski et al., 2007]. What remain to be confirmed are the domains and loops detected with HiC data [Rao et al., 2014]. Imaging will aim at confirming the reality of these loops and domains and see if more patterns can be found using pure visual methods. Work from [Chandra et al., 2012] and more recently [Boettiger et al., 2016] going in this direction have shown that functional chromatin domains can either display a condensed or relaxed configuration, with different epigenetic signatures associated in each case. An overview of various genomic methods to study chromatin at different length scales is shown in Figure 1.8.

As the ROM (Random Access Memory) of chromatin, epigenetic regulation is right now one of the hottest topic in biology. While the mechanisms that guide a resting cell have been extensively studied, the way the chromatin architecture adapts to its environment is very little studied. For instance, how long a stress can be recorded by a cell? Does chromatin learn from previous cues to adapt better to the next situation? Moreover, how chromatin architecture changes from mother to daughter cell during development, based on surrounding environment?

1.6 Fine-scale chromatin architecture: a new modelling area

In the last years, a new way of analysing chromatin has emerged, following data from in situ hybridization and HiC technique. Biophysicists have started to find patterns and trends in available data to describe possible orders of chromatin that have escaped attention until now. Chromatin is now being viewed as a self-organizing struc-
Figure 1.8: Different genomic methods to study chromatin. The ever expanding range of next-generation sequencing technologies is portrayed. A number of modern sequencing approaches have opened new possibilities to analyse epigenetics at different organisation levels and study various gene regulatory mechanisms. Furthermore, these methods offer numerous opportunities for super-resolution microscopy. Image courtesy: Wolf Gebhardt.

Figure 1.9: Comparison between predicted data and experimental data in the genomic era. The experimental results (bottom panel) were generated using HiC method and show localization of contacts between chromosome regions, an information important to model the 3D structure of the chromatin. In both cases, the red dots show the putative contacts. Image modified from [Sanborn et al., 2015].

A recent study defines chromatin states as ‘binders’ (such as CTCF) and ‘strings’ (DNA molecules) [Barbieri et al., 2012]. In this configuration, binders are in solution and find their targets driven by Brownian movements. Ideally, these binders will target DNA at one unique location. Nevertheless, if a binding site is present at different places in relative close locations on a chromosome, DNA may bind several of them together and form a cluster. The concept matches HiC data, and can explain several known complexity levels of chromatin architecture (chromatin loops, chromatin domains, chromosome territories). Tom Misteli has recently proposed a genome-wide imaging, HIPmap; that is currently being set up to validate HiC contact maps with microscopy [Shachar et al., 2015]. Finally, some recent models have also attempted to study the dynamics of chromatin. For instance, a model by [Sanborn et al., 2015] describes activation of genes as loops forming through cohesin rings and popping out of chromosome territories to enter a compartment containing transcription machineries (Figure 1.9).

The existence of the higher level of chromatin compaction, the chromosome territory, has long been oblivious to scientists. Modelling
helps to integrate data and see to which kinds of architecture the distributions of contacts could fit [Barbieri et al., 2012]. Recent models show a new creativity emerging among biologists to describe chromatin accurately, with the help of concepts from external disciplines such as polymer physics. A lesson from this research is that morphology and structural organisation of mitotic chromosomes might be structurally related to interphasic chromosome territories. One can speculate that there are even more analogies and that studying either mitotic (or meiotic, as I will discuss later) or interphase stage of the cell cycle will help to get information about the other stages of the cell cycle. In any case, a strong validation of proposed models, both with genomics and microscopy, is urgently needed.

1.7 Conclusion

The history of chromatin research provides numerous lessons for research. One of them is the necessity to put forward theories, even if they prove later wrong. Another lesson is obviously the need to put forward the development of new technologies. Though paradoxically, often, new technical insights come from new questions. For instance, how Morgan decided to study DNA to learn about evolution was a beautiful example of perfect experimental design focused on answering a big theoretical question. Lastly, from Watson and Crick to recent insights in the fields of genome architecture, modelling has emerged as a necessity to describe properly chromatin structure and behaviour. Direct observation is only useful if it is linked to genomic data, and as such requires the help of physical models to make sense of the complex available information.

Chromatin has been explored using various methods (light microscopy, biochemistry, histochemistry, genomics) but the usage of these methods was blinded by the fact that scientists thought that investigation of interphase chromatin was a dead end, that there was nothing to learn beyond nucleosomes and euchromatin/heterochromatin dichotomy. Later stages of research have shown that the picture was more complex. Firstly, in situ hybridization experiments have shown repeated regions, meaning that there are non-coding regions between genes. Chromosome territories have then revealed a compaction at the high order in the nucleus, which was no longer considered as a spaghetti dish. Moreover, recently, information coming from next-generation sequencing, chromosome capture and hybridization methods have shown even more complexity. New concepts emerge, such as chromatin loops, chromatin domains, which were unknown before. This research is relatively new, and despite thinking of pioneers [Cremer and Cremer, 2001, 2009a,b], one has to understand that the idea that chromosome functionalities are compartmentalised in the interphase nucleus is relatively new to biological research.

The questions that challenge the researchers now are: how much of the complexity is still to know? Are there functional domains that one is not aware of yet? And can single-molecule imaging help us in
this task? This is the question that I have tried to answer in the work presented here.

1.8 Acknowledgement

This chapter is an outcome of many discussions with David Fournier, who has helped immensely in formulating and revising the text.
“My intention is not to replace one set of general rules by another such set: my intention is, rather, to convince the reader that all methodologies, even the most obvious ones, have their limits.”

Paul Karl Feyerabend

2 Investigating Chromatin Organisation using Single Molecule Localisation Microscopy

2.1 Introduction

In this chapter, I discuss the technical details of single molecule localisation microscopy (SMLM) to investigate spatial and temporal organisation of DNA. The DNA is hierarchically folded at multiple levels to become more compacted and functionally organise itself inside of the nucleus. This spatial arrangement in turn affects the functionality of DNA. Thus one can characterise the organisation of chromatin into three inter-related categories: (1) the basic building blocks, (2) the functional organisation of chromatin and (3) the spatial arrangement of chromatin inside the cell nucleus.

The two classical building blocks: beads-on-a-string and 30 nm chromatin fibre have been extensively studied by EM (Figure 2.1, first column). Furthermore, one can view functional chromatin domains (Figure 2.1, second column) as an emerging building block of chromatin, responsible for its basic functions. I estimate these domains to

Figure 2.1: Chromatin spatial organisation: The spatial organisation of chromatin can be studied at three levels: at the lowest orders, which include the beads-on-a-string model and the chromatin fiber, at the level of functional chromatin domains and at high order chromatin patterns. The functional organisation of chromatin domains can be modeled from perspective of various post-translational histone modifications. Depending upon the kind of modification it is enriched with, chromatin can be either highly condensed, in an open conformation or switch between these two extreme forms. The spatial arrangement of chromatin can also be viewed from three points of views: the chromosome territory model of DNA organisation, the bimodal classification condensed and open chromatin in hetero- and eu-chromatin, and finally the highly condensed configuration during metaphase.
be about 100-400 nm, according to the literature and my own work (see Chapter 3 on interphase chromatin and [Prakash et al., 2015, Boettiger et al., 2016, Rao et al., 2014] for more details). These domains are usually the place of chromatin regulation and can display several configurations, depending on their compaction (Figure 2.1, second column). These compaction states are often associated with different kinds of post-translational histone modifications and can be characterised using information from these modifications [Prakash et al., 2015, Boettiger et al., 2016]. Domains can either be highly condensed (usually baring H3K9me3 modification, a mark associated to the presence of transcriptionally inactive repeated regions) or in an open conformation (mostly at gene promoters and intergenic regions, showing enrichment for H3K4me3, a mark associated to active chromatin). Moreover, chromatin can also be in a state where it switches between these two extreme forms as these domains can also coexist very close to each other (see [Chandra et al., 2012]; for an overview of the different configurations of chromatin domains using microscopy and genomic data, see Figure 3.16). Higher orders of chromatin folding, above the chromatin domains, include: the rather outdated bimodal classification of chromatin into condensed and open regions (heterochromatin and euchromatin), the chromosome territory model of DNA organisation [Cremer and Cremer, 2001] and finally the highly condensed configuration of the metaphase chromosome (Figure 2.1, last column).

As chromatin has a highly complex shape, theoretical models are limited to describe its functional structure. Moreover, the organisation of its basic building blocks, the functional and spatial domains, lies between what can be achieved by conventional light microscopy (LM) and electron microscopy (EM). Although EM has provided considerable insights into the structure and organisation of chromatin, as it is not DNA specific, it fails at capturing the underlying nature of the patterns observed. Moreover, sample preparation for EM includes harsh chemical cross-linking and vacuum treatment, which also influence the sample. Light microscopy techniques can be used to study protein and chromatin function in live cells but these methods suffer from much lower resolution than EM.

Super-resolution light microscopy provides an interesting alternative to EM that fills the gap between the resolution achieved by a conventional microscope [Abbe, 1873, Rayleigh, 1896] and the one required to resolve the individual chromatin domains. The first attempts to improve the resolution used confocal [Cremer and Cremer, 1978, Sheppard and Wilson, 1981] and multiphoton microscopy [Zipfel et al., 2003], allowing for effective background suppression. The advent of various super-resolution methods [Hell and Wichmann, 1994, Heintzmann and Cremer, 1999, Gustafsson, 2000], in particular, Single Molecule Localisation Microscopy (SMLM) based methods [Betzig et al., 2006, Hess et al., 2006, Rust et al., 2006, Lemmer et al., 2008] have allowed to study objects whose structure lies below the diffraction limit.
2.2 Single-molecule localization microscopy: state-of-the-art

2.2.1 Principle of SMLM

The underlying principle of most SMLM based methods is to label proteins or DNA/RNA with fluorescent molecules that can reversibly switch between a fluorescent state and a stable dark state. This process of switching between states is called ‘blinking’, and allows for optical isolation of single molecules. Since only a fraction of molecules will switch back to the fluorescent state at a given time, their precise location can be determined. The final accuracy of the position of a molecule depends on the number of detected photons. With a photon count of $10^4$ in a single glowing phase, one can achieve a resolution down to a few nanometers [Thompson et al., 2002]. In Figure 2.2, many such molecules are separated by a distance less than $\lambda/(2NA)$ and if all of them are ‘on’ simultaneously then one cannot resolve them. However, if only a few of them are ‘on’ while the neighbouring molecules are in dark state, they can be optically isolated and their precise position can be determined (see Figure 2.2). Subsequently, if one collects a series of such images where only a few of the molecules are ‘on’ in each image and localise their position, then a final image revealing the structure of the underlying object can be reconstructed [Small and Parthasarathy, 2014].

Figure 2.2: Schematic illustration of the underlying principle of SMLM using a hypothetical object whose building blocks lie below the diffraction limit. This object is made of point sources indicated by black circles. Photons emitted by these point sources such as biological molecules or fluorophores are smeared out onto the detector of the imaging system due of the wave nature of light. This distribution of photons is commonly known as the point spread function (PSF) of the imaging system (indicated by the shadow in red). PSF has a width of $\lambda/(2NA)$, where $\lambda$ is the wavelength of the fluorescent light and NA is the numerical aperture. Repeated imaging and localisation of individual fluorophores provides high resolution image of the diffraction limited object if one approximates the position of the molecule as the center of the spot. The photoncs in the airy disk, which is the central region of the PSF, are thought to have a repartition that follows a Gaussian distribution if the point source emits a sufficient number of photons [Sengupta et al., 2014].

2.2.2 The different SMLM methods: a historical perspective

Optical isolation of individual molecules in order to circumvent the resolution limit by acquiring signals at different times has been first theorized in 1985 [Burns et al., 1985], and later included in a comprehensive framework by Eric Betzig of what is now known under name single molecule localisation microscopy [Betzig, 1995]. Historically, SMLM was first used outside of the chromatin field. Early design by Betzig was successfully applied in 2006 [Betzig et al., 2006] to study cell architecture in a set-up called Photo-activated localization microscopy (PALM). PALM uses two lasers to provoke the blinking of GFP molecules necessary for single molecule microscopy. The first laser (561 nm) is used as the excitation laser while the second laser (405 nm) is used as the activation laser (see [Sengupta et al., 2014] for a review). The structures imaged showed similar level of resolution as electron microscopy, but helped to mark very precisely the position...
of given proteins on top of the EM image. Set-ups such as STORM (STochastic Optical Recovery Microscopy) use Cy5-Cy3 dye pair as a switch to optically isolate molecules whose separation is below Abbe’s limit. Firstly, all Cy5 molecules are pushed to dark state with a red laser (633 nm) and then a green laser (532 nm) is used to bring a fraction of Cy5 molecules to the florescent state. Though there is no fluorescence from Cy3 itself, a close presence to Cy5 is required for Cy5 to recover from the dark state to a fluorescent emitting state [Rust et al., 2006]. dSTORM (direct STORM), a method which extends early observations by [Rust et al., 2006, Lemmer et al., 2008] uses only one laser to push a conventional fluorochrome, for instance Alexa647, between dark and fluorescent state [Heilemann et al., 2008]. Below, I briefly summarize various approaches that led to development of SMLM in its current working form.

• First theoretical approaches: [Burns et al., 1985, Betzig, 1995]

• First practical approaches:
  2. Blinking of GFP [Dickson et al., 1997]
  3. Blinking of quantum dots [Lidke et al., 2005]
  4. (fluorescence) Photo-activated localization microscopy (PALM/fPALM, [Betzig et al., 2006, Hess et al., 2006])
  5. Stochastic Optical Reconstruction Microscopy (STORM, [Rust et al., 2006])

• Methods using standard fluorophores:
  1. Spectral Precision/Position Distance/Determination Microscopy (SPDM, [Van Oijen et al., 1998, Lemmer et al., 2008, 2009])
  2. direct Stochastic Optical Reconstruction Microscopy (dSTORM, [Heilemann et al., 2008])
  3. Bleaching/blinking assisted localization microscopy (BaLM, [Burnette et al., 2011])

• Methods based on binding activation and kinetics: Binding-activated localization microscopy (BALM, [Schoen et al., 2011])

Herein, I employed SPDM, the method initiated by [Lemmer et al., 2009] and now known as dSTORM [Heilemann et al., 2008]. This method uses a single laser to induce both photoconversion and blinking of a single fluorochrome in one excitation event. This technique was helpful in obtaining a detailed distribution of chromatin, various protein elements and histone modifications, in interphase nuclei (Chapter 3) and during meiosis (Chapter 4). This simple set-up not only enables the analysis of biological samples with the fluorophores used to image DNA molecules in conventional microscopy, but also allows for multi-modal imaging, which can then be used to compare
or combine with the results obtained from other microscopic techniques. In this thesis, I discuss various technical aspects of SMLM applied to standard DNA dyes to study chromatin organisation.

2.3 Application of SMLM to image chromatin

Chromatin has been a rather recent focus in the field of SMLM. The nano-structure of interphase chromatin was first studied by [Bohn et al., 2010] using SMLM. Statistical methods were combined with SMLM to study the distribution of histone H2B in HeLa and VH7 diploid human fibroblast cells. The main question posed by this study is the possibility of the existence of a recurrent universal chromatin nano-domain and if it can vary across the cell lines and the cell cycle. The author reported that chromatin nano-structure is cell type specific and is dependent on the way the chromatin is labelled. A similar conclusion was reached by a recent study [Ricci et al., 2015]. Before I probe further into the limitations of these two studies, I would like to discuss two concepts that are central to localisation microscopy: localization precision and signal density.

2.3.1 The tao of SMLM

Two key aspects of SMLM imaging are localisation precision and signal density. Figure 2.3 shows the interplay between these factors. While the bright fluorophores i.e. fluorophores with high photon count are good for localization precision ($\propto \frac{1}{\sqrt{N}}$, where N is the number of photons), it is highly desired to have only a subset of them ‘on’ in each frame (amount of localized events per unit area). To achieve low signal density for each frame, the lifetime of the dark state needs to be significantly longer than the lifetime of the bright state. The overall high signal density (amount of localized events per unit area) is achieved by acquiring a large number of frame so that the theoretical density of the underlying sample is matched.

2.3.2 Importance of a good localization precision in order to improve resolution

The resolution of a final reconstructed image in localisation microscopy can be attributed to two separate causes. The first is the fact that like any measurement of a physical quantity, the true value to be measured is only approached at an infinite number of measurements. Since the photon count of the localization of a fluorophore is limited, the precision with which the fluorophore location can be predicted is limited too. In this analogy a single measurement corresponds to telling which pixel on the light sensitive array was struck by one single photon. Only with the ensemble comprising many photons spread over the adjacent pixels, a highly precise location of the signal can be determined. The precision can be calculated using the Cramér-Rao Lower Bound [Neice, 2010, Small and Parthasarathy,
and is always above $\lambda / (2NA \cdot \sqrt{N})$, with $\lambda$ the wavelength of the fluorescent light, $NA$ the numerical aperture [Hagmann et al., 2016] and $N$ the number of photons.

The second cause for resolution reduction results directly from the first (the measurement uncertainty): The fact that the uncertainty of a localized event is isotropic makes it literally impossible to tell in which direction the measured position has to be displaced in order to set it to the true location of the fluorophore [Hagmann et al., 2016]. It is important to be aware that the measured position of a fluorophore is not its true position but only the one with the highest probability. The quality of this position estimate is reflected by the localization precision (or uncertainty). In other words, if the same measurement would be carried out several times under the exact same conditions, the acquired locations would be slightly displaced for each measurement. The scale of displacement for every single fluorophore is reflected by its individual localization precision, given by

$$
\sigma^2 = \frac{s^2 + a^2/12}{N} + \frac{8\pi s^4 b^2}{a^2 N^2}
$$

where $s$ is the width of PSF, $N$ is the number of detected photons, $b$ is the background intensity and $a$ is the size of pixels on the camera.

In Figure 2.4, I demonstrate that with an increasingly poor localization precision (from 2 nm to 100 nm), the point-like object start to overlap resulting in a blurred image where fine features cannot be resolved. Another point worth noting is that while the first image has the lowest uncertainty (2 nm), the images with 10 nm and 20 nm uncertainty appear the best. This is due to the fact that higher uncertainty covers for the missing signals by blurring with a bigger radius (see Figure 2.5)
2.3.3 Importance of high signal density to improve signal-to-noise ratio

One of the key to SMLM is its ability to provide structural information at the highest possible resolution among various super-resolution methods. The structural resolution in localisation microscopy depends upon the localisation precision $\sigma_{xy}$ of the individual molecules and the local density of the detected molecules is given by the following formula:

$$\sigma_{xy} = \sqrt{(2.35\bar{\sigma}_{xy})^2 + (2\bar{d}_{NN})^2}$$

$\bar{\sigma}_{xy}$ is the mean lateral localisation accuracy;
$\bar{d}_{NN}$ is the mean distance to the next neighbouring molecules.

The final number of localised signals depends on a number of factors such as labelling efficiency, activation and re-activation frequency and detection efficiency. For example, only a certain percentage of molecules gets labelled and only a subset of these molecules get activated and detected. Furthermore, even a smaller subset of these remaining molecules get reactivated again. This means that only a small subset of the molecules forming the original structure get activated, detected and localised, making it hard to distinguish signals from background. In Figure 2.5, with 120000 points one can resolve fine features of Erika's lips (yellow box), while 1000 points are insufficient to draw any satisfactory conclusions. Thus a minimum critical density of signals of at least $\frac{1}{10}$ of the original structure is often required especially if the underlying structure is unknown, a common case for most super-resolution methods. If this is not possible then an intelligent estimate must be made from the prior knowledge based on other studies (for example, EM).

Figure 2.5: Importance of high signal density: In localisation microscopy, molecules emit fluorescent bursts multiple times before they are bleached (i.e. they stay permanently in dark state), so I use the term ‘signals’ rather than ‘molecules’ here. In all 6 images, the signals were sampled with a localisation uncertainty of 10 nm and the number of signals were gradually increased from 1000 points to 120000 points for a 25 µm² area. A minimum signal density (signal density means the amount of localized events per area) is required to make a first assessment about the underlying structure.
2.3.4 Limitations of previous approaches to study chromatin organisation

Human genome has roughly $10^9$ base pairs and a spherical nucleus $(\frac{4}{3} \pi r^3)$ of 10 $\mu$m radius will have an overall volume of approximately 4000 $\mu$m$^3$. Since the cells in culture are relatively flat, one can assume that they show an ellipsoid shape $(\frac{4}{3} \pi r^2a)$ with the axial thickness $(a = 2 - 3\mu)m$ smaller than the lateral radius $(r = 10\mu)m$. This would bring down the nuclear volume to roughly 1000 $\mu$m$^3$. Since the observation volume is only a fraction of the total volume, I assume that the final volume of the nuclei imaged would be around 200 $\mu$m$^3$ with an optical section of 500-600 nm axially). So, overall one expects to have around $10^8$ putative binding sites/signals in the nuclei. As only a subset of molecules get labelled and are finally detected, the final number of the expected signals is still quite lower. Thus a minimum of $10^7 - 10^8$ signals should be detected in order to get a first accurate representation of chromatin distribution inside the cell nucleus [Szczurek et al., 2014].

In one of the previous studies on chromatin organisation, emGFP conjugated histone protein H2B was expressed [Bohn et al., 2010] while in another similar study [Ricci et al., 2015], H2B was immunostained using Alexa Fluor 647. At present, both of these studies report a labelling density of 100-500 signals per $\mu m^2$ and total identified signals in order of $10^4 - 10^5$. At present, both these studies lack sufficient labelling density to make good estimates about the distribution of chromatin inside the cell nucleus.

Here, I focus on improving the method so that the overall signal density and labelling efficiency of DNA molecules is closer to expected binding sites. In the next section, a simple method which uses direct DNA binding dyes and fulfils the above criteria is presented.

2.4 A method to reach high labelling density of chromatin with SMLM

Previous studies of chromatin distribution inside of the cell nucleus have relied on a fluorophore conjugated with antibodies targeting chromatin via core histone proteins [Bohn et al., 2010, Ricci et al., 2015] but none has used direct staining of DNA. Recently it was found that DNA minor groove binding dyes, such as Hoechst and DAPI, can undergo UV-induced photo-conversion, to be effectively employed in single molecule localization microscopy (SMLM) with high optical and structural resolution. A proposed mechanism is that these minor groove DNA dyes undergo intra-molecular proton transfer between the phenol group and the bisbenzimide nitrogen under UV illumination [Cosa et al., 2001, Carvalho, 2010]. This UV induced photo-conversion leads to a red shift from the blue emitting form to a green emitting form; a second excitation at a higher wave length will push the fluorochrome to a dark state. This situation eventually induces multiple cycles from dark-state to fluorescent
investigating chromatin organisation using single molecule localisation microscopy

Figure 2.6: Figure and caption modified from [Szczurek et al., 2014]. (A) SMLM image of a HeLa cell nucleus stained with Hoechst 33258. Scale bar: 1 µm. (B1-B2) Widefield and SMLM magnifications of the heterochromatin region highlighted in inset (B). (C) Complete nucleus in the widefield mode. (D1-D3) Magnified sections of widefield, SMLM and point representation of nucleolus in (D). (E) Histogram of localization precision with average precision around 26.6 nm. (F) Profiles of the heterochromatic region in the boxes of insets B1 and B2, comparing widefield and localisation images. (G) Hoechst 33258 excitation spectrum and the emission spectrum shift of its photoproduct. The green interval is the detection band of the photoproduct.

State and back to dark state. Fluorescence of these stochastically blinking molecules is registered by illumination with high intensity 491 nm laser, until bleached (i.e. the molecules are permanently in the dark state). It is worth to note that green-emitting forms of both, Hoechst 33258 and DAPI occur rather sparsely, facilitating the optical isolation of individual dye molecules bound to DNA [Szczurek et al., 2014]. To test if the molecules are really photoconverted, SMLM measurements were performed without any prior illumination with 405 nm line. Subsequently, a significantly lower blinking rate in green-yellow channel was observed, resulting in a poor final reconstruction (data not shown). In the reconstruction from these datasets, fine structures of chromatin could not be resolved. However, with low UV excitation (405 nm), a significant increase in number of molecules in blinking state was observed allowing acquisition of more signals. A 630/90 band pass filter was used to record these signals.

Figure 2.6 shows an optimised adjustment of 405/491 nm laser intensities to study the distribution of chromatin inside a HeLa cell nucleus. Compared with previous studies of histone H2B stably expressed with GFP [Bohn et al., 2010], 50 times more signal density was recorded (124 signals per µm$^2$ for H2B labelling as compared to 5000 signals per µm$^2$ here). The nucleus stained with Hoechst (Figure 2.6A) shows higher density of chromatin around the nucleolus and at the periphery of the nucleus likely associated with hetero-
chromatin. Furthermore, a lower density of chromatin is observed towards the interior of the nucleus, in line with previous studies [Cremer et al., 2004, Albiez et al., 2006, Cremer et al., 2015].

2.4.1 Theory of DNA dye fluorescence

Molecules with multiple aromatic cycles which bind the small groove of DNA, such as DAPI, can potentially emit fluorescence. In solution, the structure of the molecules shows a high flexibility, but while interacting with DNA, they become stabilized and display a planar structure, which enhances the degrees of freedom of circulating electrons across aromatic cycles or other features of the molecule. This situation has both effects of increasing the probability of capturing incident photons, as the surface of the molecule increases, and the probability to observe an electron hit by a photon, as an electron occupies more space at a given time ([Biancardi et al., 2013] and Figure 2.7).

Figure 2.7: Transitions between excitation states during the fluorescence process. Fluorescence depends on the rapid and lasting rotation between a ground state (electron of low energy) and an excited state (electron of high energy). During relaxation process of the cycle (red arrow), a photon is emitted that produces light. With time, electron can reach other intermediate states called triplets ($T_1$ and $T_N$ here) that can lead to the deteriorative oxidation of the fluorochrome, resulting in bleaching.

2.4.2 Adapting study of DNA dyes fluorescence to SMLM

Application of blinking properties of DNA dyes to SMLM stems in the photoconversion of individual molecules followed by their excitation to the dark state, a concept pioneered by Betzig using GFP [Dickson et al., 1997, Betzig et al., 2006]. The method has two steps:

1. Optimization of photo-conversion, to ensure that the pattern of photo-converted molecules is optimal to generate blinking patterns.

2. Optimization of buffers, to push a higher number of fluorochrome molecules to photo-conversion and delay bleaching of molecules.
2.4.3 Optimization of the photoconversion process

This step optimizes the amount of molecules photo-converted to obtain high density of signals. The signals are optimally spread in time so that one does not acquire too many signals in a single frame, otherwise one gets unresolved points and poor resolution. To achieve this, the intensity and the timing of photo-conversion, via a 405 nm wavelength excitation pushing DAPI or Hoechst to a green form, has to be calibrated properly. If photo-conversion is absent, the final number of detected signals is low and the final reconstruction is impaired (Figure 2.8).

![Figure 2.8: Optimization of the photoconversion process to obtain good resolution and signal density.](image)

2.4.4 Optimization of the buffer conditions

A strong element in the optimization of the protocol to employ conventional DNA dyes for imaging of DNA molecules is the usage of an effective buffer. Usage of mixes with high concentrations of glycerol seems to be the best option according to recent benchmarks [Zurek-Biesiada et al., 2016]. Beside preserving the nuclear morphology, glycerol prevents the generation of reactive oxygen species (ROS) from the reaction between the fluorochrome and surrounding dioxide molecules. This reaction releases oxygen atoms with a free radical, which are very hostile for biological molecules such as DNA [Bernas et al., 2004]. Glycerol can compete with the fluorochrome for interaction with the free radical, preserving the fluorochrome from degradation [Hussels and Brecht, 2011]. This results in a better photoconversion than if the DNA dye was subjected to more Brownian movements [Biancardi et al., 2013].

2.4.5 Multicolor imaging with DNA

To analyse the spatial arrangement of different nuclear proteins with respect to DNA, optimization of various conventional dyes was studied along with DNA dyes and summarised in Figure 2.9. It is further hoped that the dyes presented in Figure 2.9 will be optimised to allow
the visualization of more fluorochromes within one experiment. This will further enable the analysis of spatial arrangements of various other components of the nucleus in conjunction with chromatin at the level of individual nuclei.

![Table of DNA Dyes and Other Fluorescent Probes](image)

### 2.4.6 A summary of various approaches used to study DNA with SMLM

The strategies to study chromatin inside the cell nucleus can be divided into two broad categories: (1) Direct labelling of DNA and (2) indirect labelling of DNA. Below I provide a brief summary on various approaches that have been used to study chromatin/DNA with SMLM which is pictorially summarised in Figure 2.10.

- **Direct staining methods**

  1. **YOYO-1** is a DNA intercalating dye binding between the two strands of DNA. YOYO-1 and PicoGreen (which binds to the major groove) were previously used to study the organisation of bacterial chromosomes with SMLM [Schoen et al., 2011]. The authors called this method binding-activated localization microscopy (BALM) because both YOYO-1 and PicoGreen bind directly to the DNA and these molecules only get activated when bound to the DNA. This is a good way to improve both labelling efficiency and localisation accuracy as DNA binding increases specificity and is closer to the actual target than antibodies are. These dyes have been shown to work for lambda phage DNA stretches but not for structures which have much higher chromatin density, for example, mammalian cell nuclei. A report
of a successful application of YOYO-1/SMLM to staining of eukaryotic nuclei will be presented in Chapter 3.

2. Hoechst, DAPI and Vybrant Violet (VV). Conceptually this is similar to the binding-activated localization microscopy (BALM). DNA minor groove binding dyes such as DAPI or Hoechst do not ‘blink’ in their standard form. However, with low dose of 405 nm laser, a small proportion of molecules can be photoconverted to green form and start to blink, a property applicable to localisation microscopy. It is proposed that upon UV illumination, these dyes, which either undergo protonation or become photoconverted from blue to green emitting form, might also be driven by hydrogen peroxide [Piterburg et al., 2012]. It must be noted that only one wavelength (491 nm) is required for activation and excitation in the case of VV.

3. Propidium Iodide or DRAQ5 are non-cyanine intercalators that also bind directly to DNA. However, their applicability in superresolution microscopy has yet to be demonstrated.

- Indirect staining methods

1. EdU incorporation: Zessin et. al. [Zessin et al., 2012] were the first to describe a high resolution structure of DNA using precursor incorporation. The authors used EdU (5-ethynyl-2’-deoxyuridine) labelling using click chemistry to image nascent DNA produced during DNA replication. Click-chemistry is a copper-induced covalent binding between an alkyne group of EdU and an azide present in the chemically modified fluorophore [Grammel and Hang, 2013]. This method has two main advantages. Firstly, it is highly specific. The alkyne-azide bond is not commonly found in any biological system and the method is very specific and sensitive. Because of this specificity, the method produces almost no background. Secondly, it is less harmful compared to other popular precursors such as BrdU [Baskin et al., 2007, Grammel and Hang, 2013].

2. Core histone proteins: Bohn et al. [Bohn et al., 2010] studied chromatin organisation inside the cell nucleus by fusing one of the core histone proteins (H2B) with GFP. In this study, H2B was either stably integrated (H2B-GFP) or over-expressed (H2B-emGFP) in the HeLa cells. In other studies, either immuno-labelling against core histone proteins (H3, H2B) was used or cells were transfected with H2B-mEos2 or H2B-PAmCherry for live cell imaging [Ricci et al., 2015].

3. Histone modifications: To study functional chromatin and its compartmentalization, histone modifications were recently used to describe chromatin organisation [Prakash et al., 2015, Boettiger et al., 2016]. These two studies were based on antibody labelling of specific histone modifications. The main problem with such labelling methods is the huge size of primary and secondary antibody (molecular weight around 150-200 kDa) and
the linker length i.e. the distance between the true position of the molecule and the position where the signal is detected, which can be in the order of 7.5 nm for a primary antibody and in the order of 15 nm for a secondary antibody.

- **Sequence specific imaging of DNA:** It is often desired to study specific loci of gene or other DNA sequences instead of the entire chromatin. This specific staining can be performed using Fluorescence In Situ Hybridization (FISH) [Weiland et al., 2011], oligonucleotide probes [Cremer and Cremer, 2001, Müller et al., 2010] or via genome editing techniques such as transcription activator-like effectors (TALE), [Miyanari et al., 2013, Thanisch et al., 2013] CRISPR/Cas9 techniques [Anton et al., 2014, Chen et al., 2013, Wood et al., 2011, Hsu et al., 2014, Doudna and Charpentier, 2014] or SNAP-tag fusion proteins [Klein et al., 2011].

Figure 2.10 compares the overall staining of the cell nucleus with direct and indirect staining. One can observe that direct staining of DNA leads to a more continuous distribution of chromatin as compared to indirect staining, where the distribution seems to be in a speckle-like patterns (see also [Bohn et al., 2010, Ricci et al., 2015] for recent examples of low labelling density). This happens because in specific staining only the functional compartments, usually associated to specific histone modifications, are revealed. For example, H3K14ac is associated with active transcription and hence only sites where chromatin is in a more open conformation fluoresce. Similarly, in EdU incorporation (Figure 2.10, bottom right) only the freshly replicated sites from S-phase are detected (see Chapter 3 for more examples of these two cases).
2.5 SMLM microscope design and imaging pipeline

The basic set-up for SMLM imaging is very similar to the configuration of a wide-field microscope. In the following sections, various aspects of the SMLM such as sample preparation, data acquisition, data reconstruction, data visualisation and data analysis are discussed.

2.5.1 Sample preparation for SMLM

A good SMLM sample follows three criteria. (1) The nano-structure is preserved. (2) A high number of fluorophores bind to the target. (3) Non-specific labelling and background are minimised [Bates et al., 2013]. For preservation of nanostructure, optimised fixation protocols from EM can be used. Optimization of buffer is key and usage of reactive oxygen species competitors which prevent fluorochrome from degradation can help. Background/non-specific signal can severely decrease the quality of a superresolution reconstruction [Betzig et al., 2006]. A comparison of different background scenarios is shown in Figure 2.11. Use of thin samples in addition to an appropriate imaging buffer can help to minimize the background.

2.5.2 Imaging medium

Usage of photo-convertible DNA dyes (Hoechst, DAPI and VV) requires certain components to be present in the ‘switching buffer’. In particular, the switching buffer should contain 0.5 mg/ml Glucose oxidase, 0.04 mg/ml Catalase, 0.1 g/ml glucose in PBS. The use of MEA, one of main components of the STORM/dSTORM imaging buffer diminishes the rate of switching in the case of DNA dyes. The switching buffer facilitates the switching of the steady fraction of spontaneously blinking molecule in each frame. The switching buffer is the same as the oxygen scavenger system in STORM/dSTORM, which mainly reduces photo-bleaching fluorescent dyes. More details on imaging medium can be found in [Szczurek et al., 2014, Żurek-Biesiada et al., 2015, 2016].

2.6 Data acquisition for SMLM

For imaging DNA with photoconvertible DNA dyes, several important aspects have to be considered. Firstly, low power 405 nm illumination in conjunction with a 491 nm laser should be used to increase the number of detected molecules. Similar ideas were previously described in [Heilemann et al., 2008] for photoswitchable fluorescent dyes. However, these dyes have no affinity for DNA. The SMLM measurements were performed with a vertical/upright microscope set-up (see 2.12). The set-up has four laser sources with excitation wavelengths at 405 nm, 491 nm, 561 nm and 647 nm and can be dissected into 3 modules described below.
1. **The illumination module**: The laser beam enters the microscope via mirrors (M) and dichroic mirrors (DM)\{M1-M4, DM1-DM4\}, a collimator arrangement (5x expansion of beam diameter) and neutral density filters (if required). This collimator is made up of two achromates with focal lengths of 30 mm and 150 mm which expand the beams by a factor of 5 to get an homogeneous illumination of the sample.

2. **The localisation module**: To achieve the high laser intensity for the localization mode, a lens [LL] is inserted in the optical pathway, leading to a smaller illuminated area of higher intensity in the object region of interest. The beam is focused by this lens into the back focal plane of an oil immersion objective lens (63x, NA=1.4). The sample is actuated by a piezoelectrical stage [PS] for focusing.

3. **The detection module**: The emitted fluorescent light goes through the DM and is focused by a tube lens [TL] (1.0x, f=200 mm) onto the CCD chip of a highly sensitive 12 bit black-and-white camera. A set of appropriate blocking filters is mounted in a filter wheel [FW] in front of the camera chip.

Before acquiring data, certain parameters have to be optimised. For example, bleaching gradient, blinking and their relation to integration time must be studied prior to the measurement and the final number of acquisition frames should be chosen accordingly. One should try to optimise the integration time of the camera as this determines signal-to-noise ratio and eventually the background of the sample. Acquisition of wide-field images before and after measurement helps to compare the structure of the sample with the final reconstruction. Illumination of the sample should be homogeneous. Furthermore, to
fasten the acquisition time and save disk space, the sample area can be restricted to a region of interest.

### 2.7 Data reconstruction for SMLM

Figure 2.13 presents various steps required to reconstruct a highly resolved image from single molecule coordinates. The operations can be characterized at various levels which are described below.

- **Stack level**: A high number of frames with each frame containing only a few optically isolated molecule must be generated. This data stack can be used to analyse the position of the fluorophore across multiple frames and characterise the fluorophore. Furthermore, a background map for each frame must be calculated and subtracted to get the difference image. This step can be really critical depending on the type of background in the sample (refer 2.13.)

- **Frame level**: Local maxima in each frame are determined and the corresponding regions-of-interest (ROI) are extracted.

- **ROI level**: Each fluorophore is localised and an estimate about the localisation precision for each molecule based on the parameters of the model function should be calculated. An estimation about the
number of photons per molecule is then calculated, an important parameter to study the characteristics of the fluorophores used in the experiments.

- **Error corrections**: Signal from a particular fluorophore occurs more than once during an acquisition and subsequent frames. Removal of signals in multiple consecutive frames is important, so that the same fluorophore is not counted twice. If the sample moved significantly during acquisition, the drift in the sample must be corrected, a common procedure for measurements of long duration. Finally, the events that do not fulfil other quality criteria are removed.

- **Visualisation**: The position of the single molecules should then be visualised to get a nanoscale representation of the biological object. Visualisation methods include for example, Gaussian blurring, triangulation and histogram methods. A visualisation method is selected based on the labelling density and/or the prior knowledge about the underlying structure from other methods such as EM.

- **Analysis**: Finally, different kinds of analysis such as co-localisation, cluster analysis, nearest neighbour, density analysis can be performed on either high resolution images or coordinates of single molecules.

### 2.7.1 Spot finding for SMLM

Algorithms used to precisely identify the locations of fluorophores can be broadly classified into two categories, fitting based and non-fitting based (usually Centroid) methods. While iterative fitting-based methods can usually provide fitted parameters equal or close to the maximum likelihood estimate, *ad hoc* centroid based methods are usually very fast. However, any localisation method will struggle if the underlying model poorly represents the observed data e.g. in case of a high background level, presence of out of focus signals or noise, etc. A particular challenge for the exact fluorophore determination is posed by both spatially and temporally fluctuating background intensities arising from out-of-focus blinking fluorophores. This can happen if the structure is not *per se* 2-dimensional (e.g. PALM using TIRF illumination, see Figure 2.11). In the following sections, I discuss these two broad categories of localisation methods.

**Fitting based methods**

Photons emitted by point sources are smeared out onto the detector of the imaging system due of the wave nature of light. This smear or blur is described by the point spread function (PSF) of the imaging system. The intensity distribution of a photon at the detector follows an Airy function but for practical purposes is approximated with a Gaussian function. The overall model function consists in a 2D Gaussian describing the PSF, a function describing the background
level and one more term to describe the noise. The model function is represented by:

\[
I(x, y) = \frac{A}{2\pi\sigma_x\sigma_y} \exp \left[ -\frac{1}{2} \left( \frac{(x - x_0)^2}{\sigma_x^2} + \frac{(y - y_0)^2}{\sigma_y^2} \right) \right] + B + N
\]

where \(x, y\) are the coordinates of the point emitters, \(\sigma_x, \sigma_y\) are the width of the distribution, \(A\) the peak intensity value of the distribution, \(2\pi\sigma_x\sigma_y\) the normalisation factor, \(x_0, y_0\) the coordinates of the real center of the distribution, \(B\) the background level and \(N\) the noise parameter.

The next task is to optimise the parameter values in order to minimise the error between the signal and the model. The optimisation can be done on all the parameters or just on the coordinates of the emitter positions. Two common methods to optimise the parameters are the least squares method (LSM) and the maximum likelihood estimation (MLE). The principle behind both methods is the same. In LSM, the difference between the signal and model on each pixel is calculated and the error is then squared and added. Based on the error sum, new parameter estimates are made and the sum of the squared errors is calculated again to check if the updated parameter values reduce the error. This process is iterated until the least summed errors are obtained.

In the MLE, the overall process is the same except that detailed information about the experimental conditions such as knowledge about the PSF, noise, background is required. Similarly to LSM, the difference between the signal and the model is calculated and statistics of noise are then used to predict how likely the difference between the model and the signal is. The parameters are tuned to maximise the likelihood of the data. Cramer-Rao Lower Bound (CRLB) states that MLE makes more precise estimates compared to LSM or other parameter optimisation methods [Small and Stahlheber, 2014, Small and Parthasarathy, 2014].

Non-fitting based methods

The fitting methods are often computationally intensive and difficult to handle when the sample is inhomogeneous. Another approach is to find the coordinates of the centroid of the fluorescent spot or in the case of isotropic emitters to take advantage of their radially symmetric shape to estimate the coordinates. When the background is non-uniform and so localisation density is high, due to the additive nature of background noise at regions with high localisation density, the coordinate estimates are biased towards the center of the ROI, often resulting in a grid like patterns (Figure 2.14 and [Best et al., 2014]). Various filtering methods should be used to reduce the background intensity and improve the coordinate estimation. For more details on various algorithms estimating the emitter coordinates, please refer to [Small and Stahlheber, 2014, Small and Parthasarathy, 2014, Chenouard et al., 2014].
2.7.2 Drift correction algorithms for SMLM

The correct position determination of fluorescent molecules is crucial for the interpretation of the localization microscopy data, e.g. to understand the biological structure investigated. The position of fluorophores is highly sensitive to environmental disturbances (e.g. acoustic vibrations) and to mechanical instabilities of the microscope hardware (e.g. thermal expansion, stage drift). These disturbances can cause distortion in the recorded image, significantly affecting the achieved localization accuracy, especially when it is in the order of tens of nano-meter or better. Previously, on line drift correction methods have been described, which estimate and correct the drift experienced during recording of the experiments. Predicting the drift for future frames is a hard task, as the behavior of vibrations cannot be predicted. This can easily be done after measurement.

With colleagues, I developed a drift correction strategy based solely on already acquired data without any fiducial markers [Hagmann et al., 2014]. It was found that in some SMLM set-ups (PALM, STORM), most of the biological samples exhibit enough permanent (photostable) structure that can be used at several time points to gain information about the sample. This information was used to correct the lateral drift based on the underlying structure visible in a raw image sequence (averaged over 10 subsequent frames for one sample image), to then calculate the auto-correlation between sample images. Then two (for x and y) eighth order Fourier series were fitted to the acquired data in order to obtain the drift vectors. Figure 2.15 A-B shows HeLa cell nucleus stained with Hoechst 33258 photo-product before and after drift correction. The long acquisition times resulted in considerable mechanical drift of the stage. In the Figure 2.15, the frames of the data stack are color coded to demonstrate the drift in the sample. The initial frames are coloured blue, while the final frames range from yellow to white. The sample can be seen to drift
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Figure 2.15: Structured based drift correction strategies for localisation microscopy: Some variants of localisation microscopy exhibit enough permanent (photostable) structure that can be used to correct the lateral drift based on the underlying structure visible in a raw image sequence. HeLa cell nucleus stained with Hoechst 33258 photoproduct before (A) and after drift correction (B) are shown. (C) Widefield image of the same nucleus. Due to long measurements, the initial drift was found to be in the order of 500-1000 nm. (D-E) After application of structured based drift correction algorithm drift improved to less than 20 nm, well within the localisation precision. The magnified sections (D and E) show significant improvement in resolution (computed using FRC method [Nieuwenhuizen et al., 2013]). The resolution before drift correction was 125 nm and improved down to 107 nm after [Hagmann et al., 2014].

from top right to bottom left. For the SMLM microscope used for the measurement, the drift was in order of 100-1000 nm (Figure 2.16A) and was determined by image phase correlation. A polynomial or Fourier series (equation below) was fitted through the data, from which the dislocation of every event was subtracted.

\[ y = a_0 + \sum_{i=1}^{n} a_i \cos(iwx) + b_i \sin(iwx) \]

where \(a_0\) is the intercept term in the data (associated with \(i = 0\) cosine term), \(w\) the frequency of the signal and \(n\) the number of harmonics (8 in our case).

In the present case of a cell nucleus with high background, the data were corrected to a final drift under 20 nm (Figure 2.16B), which was reasonable given the high localisation precision (average 25 nm, Figure 2.16C). Furthermore, the resolution computed based on Fourier ring correlation [Nieuwenhuizen et al., 2013] showed a significant enhancement in resolution before (125 ± 12 nm) and after (107 ± 11 nm) drift correction. The drift correction also resulted in significant improvement of neighbour distances. The mean nearest neighbour distances before and after drift correction were approximately 42.95 nm and 39.76 in the zoomed sections of the cell nucleus (Figure 2.15D-E and Figure 2.16D).

Overall, the drift correction resulted in increased local density of chromatin at the nuclear periphery, which is in accordance with nuclear architecture. It is believed that with appropriate drift correction strategies, one can observe true structural features which are often accompanied with a decrease in nearest neighbour distances. Structure
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Figure 2.16: Quantification of sample drift. (A) The drift along x axis was less than 200 nm, however the drift along y axis was in order of 500 nm. (B) After application of structured based drift correction algorithm, the overall drift in both x and y directions was less than 20 nm, well within the localisation precision (C). (D) shows the nearest neighbor distances before and after drift correction. The mean nearest neighbour distance before drift was 42 nm while it improved to 39 nm after correction.

2.7.3 Data visualisation for SMLM

While most imaging modalities generate an image, SMLM provides coordinates single molecules in addition to the image common to the other superresolution methods (STED and SIM). Previously, scattergram of point positions [Hess et al., 2006, Van Oijen et al., 1998], 2D histogram of point positions [Heilemann et al., 2008, Lemmer et al., 2008, Fölling et al., 2008, Egner et al., 2007], localisation precision based Gaussian blurring [Betzig et al., 2006, Rust et al., 2006], nearest neighbour blurring of molecule positions [Kaufmann et al., 2012] and triangulation of localisations [Baddeley et al., 2010] have been the most popular visualisation methods.

In Figure 2.17, localisation precision based Gaussian blurring, triangulation and nearest neighbour blurring of individual molecule are compared. When enough number of nearest neighbour molecules are taken into consideration (20 in the present case), the underlying structure becomes increasingly visible. This happens because blurring locations with a Gaussian is not the best choice when the labelling density is low. In such a case the pointillist appearance of the emitters based drift correction demonstrates high background and that the underlying structure of datasets can be used to correct drift. Using this approach, one can successfully correct the localisation microscopy data down to a final drift under 5 nm. The results are comparable to fiducial markers based strategies. Moreover, the resolution of the final reconstructions is substantially enhanced and the natural limit of localisation precision is achieved.
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Figure 2.17: Comparison of various visualisation algorithms: Comparison of Gaussian blurring based localisation precision, triangulation and nearest neighbour blurring of individual molecules is shown. When enough nearest neighbour points are taken into account, the underlying structures can be better observed. Nearest neighbour blurring can help to bring out the underlying structure in images lacking proper labelling density. Moreover, the points that are not part of the structure are suppressed. Figure and caption modified from [Prakash et al., 2015].

resurfaces in the final image. Moreover, there is a resolution loss factor of $\sqrt{2}$ as stated in [Baddeley et al., 2010]. However, nearest neighbour blurring is helpful at revealing structures especially if the sample suffers from a low density of points. Moreover, the points that are not part of a structure are suppressed. Finally, the visualisation method is chosen based on the labelling density and the characteristics of the structure to visualise (1D, 2D or 3D).

2.7.4 Data analysis for SMLM

Advent of various super-resolution microscopy methods have brought to light various diffraction limited biological objects, revealing periodic patterns [Prakash et al., 2015, Früh et al., 2015, Xu et al., 2013] under better resolution. The analysis of periodicity in these studies [Früh et al., 2015, Xu et al., 2013] was based on the intensity information of the images. In addition to pixel intensity information, SMLM provides information about the single molecule coordinates which can also be used for autocorrelation and periodicity analysis.

Single molecule autocorrelation

For single molecule autocorrelation, each localisation was blurred with 20 nearest neighbours and a binary mask was generated (see Figure 2.18) using a global threshold described elsewhere [Prakash et al., 2015, Jianzhuang et al., 1991]. The single molecules within this binary mask were extracted for further analysis. This resulted in keeping only the molecules which belong to the structure or the
clusters considered. For the autocorrelation analysis, a line was fitted manually to pass through the center of the object. The coordinates were then translated and rotated to get a more linear orientation. Finally, the autocorrelation values were calculated on the histogram of the tangential distances along the central axis. The algorithm is described in detail in [Prakash et al., 2015].

2.8 Some further considerations for localisation microscopy

There are a number of artefacts that can arise due to sample preparation mainly due to fixation conditions, permeabilization conditions, antibody concentration and the type of buffer used. These are described in detail in [Whelan and Bell, 2015]. Here, I discuss three more kinds of artefacts that can arise from the way microscope is set up and the coordinates of single molecules are estimated post-acquisition.

2.8.1 Artefacts in localisation microscopy

Figure 2.19 shows negative of wide-field and localisation image of a HL-1 cell nucleus stained with Hoechst. Due to the non-homogeneous illumination of the sample (Figure 2.19A), the lower left of the cell nucleus is more illuminated than the upper right part of the nucleus. This leads to a non-uniform detection of molecules across the sample. For example, the chromatin density at the nuclear periphery (the upper right part of the image in Figure 2.19A-B) is higher than the lower left part of the image. The same pattern of density can also be observed around the nucleolus (black arrows). Another factor that can lead to a non-homogeneous illumination of the sample is the Gaussian profile of the excitation beam. In such a case, the central regions are more illuminated than the regions toward the periphery of the nucleus.
Another type of artefact can arise due to the data reconstruction when there is a high number of signals in each frame (Figure 2.19C). The high density leads to the overlap of the signal resulting in a grid-like patterns. If the centroid fitting algorithm or center-of-intensity (COI) is used to localise the signals then the signal is biased toward the center of the pixel resulting in grid-like patterns (see Section 2.7.1). However, no grid-like pattern is observed with Gaussian fitting, which is more accurate but slower when compared to centroid fitting. One solution to solve this problem is to make sure only few signals blink in each frame so signals do not overlap and can be optically isolated. Then one has to take a high number of frames to get a high density super-resolved image. This can be achieved by initial reversible photo-bleaching of the sample before acquisition and waiting until the uniform blinking of the signals is achieved.

A third type of artefact is experienced when biological objects under study are poorly labelled. The pattern which are obvious in wide-field image are missed in the high resolution images. Such an example can be seen in Figure 2.20. Pol II is known to form barrel-like elongated shapes in polytene chromosomes [Zhimulev, 1996] which are apparent in wide-field image (Figure 2.20A, inset A1). However, SMLM imaging does not reconstruct these apparent patterns of Pol II.
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(Figure 2.20B), following the well-known alternation patterns of dense and light regions of polytene chromosomes [Zhimulëv, 1996]. Pol II-rich regions are enriched for genes, and correspond to the dense regions of electron microscopy images, while Pol II-poor regions correspond to light regions, deprived of genes. This example shows a major pitfall of super-resolution imaging, particularly prominent when the underlying structure is unknown and poor or insufficient labelling of the biological object might lead to a wrong interpretation of the data. This also reflects the importance of a good in-depth literature survey about the biological object and the importance of blurring when the labelling density is limited.

### 2.8.2 Difference between localisation precision and accuracy

The terms localisation precision and accuracy are often used interchangeably. Localisation precision is the exactness with which the position of a signal can be predicted, which can be slightly off the true position of the molecule. This distance between the true position of a molecule and the detected signal is the localisation accuracy. Figure 2.21A, shows a detected signal slightly off from the true position of the molecule. As the signals are not spread, the localisation precision will be good but the localisation accuracy will be poor. In the second case (Figure 2.21B) the detected signals are spread over a large region resulting in a poor localisation precision but an increased localisation accuracy as the detected signals are close to the true position of the molecule. In the third case (Figure 2.21C), localisation accuracy and precision are both high, a typical case for Hoechst and DAPI which directly bind to DNA (high localisation accuracy) and display a high photon count (high localisation precision).
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2.9 Summary

Single Molecule Localisation Microscopy (SMLM) is one of the major emerging tools for the analysis of biological structures at approximately 10 nm spatial resolution. The procedure relies on sequential detection of (a subset of) individual fluorophores. For dense regions (fluorophores with significant overlap), a compromise between labelling density and the photoswitching behaviour of fluorophores is needed to optically isolate molecules in each acquired frame. The last 10 years have seen a significant progress in fluorescence imaging with the development of new fluorescent probes and the discovery of new properties of existing fluorochromes [Szczurek et al., 2014, Żurek-Biesiada et al., 2015], making them applicable for super-resolution imaging.

Until recently, description of chromatin was limited to immunostaining of histone proteins, which does not provide enough labelling efficiency and density for chromatin imaging [Bohn et al., 2010, Ricci et al., 2015]. Nevertheless, usage of conventional dyes dramatically increases the amount of signals recorded, opening avenues for the description of chromatin architecture at all levels of magnification. This is the matter of the next two chapters; Chapter 3 discusses many structural features of chromatin found in interphase, while Chapter 4 presents recent results regarding the chromatin architecture of the pachytene chromosome. Both these aspects of chromatin organisation grandly benefit from the developments presented in the current chapter. In this chapter, I discussed the theory and concepts of SMLM, as well as sample preparation, hardware implementation, data reconstruction, visualisation and quantifications. I closed the chapter with a note about localisation accuracy, precision, resolution and some of other technical pitfalls.

With more efficient fluorophores (i.e. with higher photon counts), highly sensitive camera, high NA objective lenses, an even higher spatial resolution can be expected in the future. A particular important challenge is live cell imaging, which requires both high spatial and temporal resolution though efforts in this direction are already
being made [Biteen et al., 2008, Shroff et al., 2008]. Single particle tracking is another area where photo-switchable fluorescent probes will facilitate tracking of high-density particle in live cells [Manley et al., 2008]. Finally, I hope that together with SIM, SMLM can be broadly applied to chromatin biology and other areas of cell biology to provide insights into the nuclear architecture at nanoscale.
3 Structure, Function and Dynamics of Chromatin

3.1 Introduction

Chromatin is a DNA-protein polymer, which consists of DNA, structural proteins, non-structural proteins and RNA. During interphase, chromatin encodes the information necessary to maintain the primary functions of the cells. At the same time, the cell holds in a relatively small volume (roughly 4000 µm$^3$ of diameter for the nucleus) the entire genome, which is billions of base pairs long and roughly 3 meters in length when completely unfolded. Moreover, information needs to be retrieved from this highly condensed structure when a gene needs to be expressed at a fast pace. To achieve this, chromatin arranges itself in a highly ordered and compact structure. This compaction has several hierarchical levels of folding, similar to fractals, which show similar patterns at multiple length scales. DNA helix represents the lowest level of the hierarchy while the metaphase chromosome represents the highest level. Before the advent of EM studies, research on the nucleus was mainly focused on (1) its chemical composition and (2) the structure of highly condensed chromosomes. The status of chromatin during interphase was oblivious and limited to the description of punctuated elements such as nucleoli. Recently, the overall view of interphase chromosomes has become very detailed, and several intermediate orders have been shown to exist, though the importance of these orders is still unknown.

The main feature of interphase chromatin that has been extensively studied is the bead-on-string like structure called nucleosome. A nucleosome is a structure of 11 nm diameter consisting of DNA and histone proteins [Kornberg, 1974, Richmond et al., 1983, Luger et al., 1997, Kornberg and Lorch, 1999]. The DNA molecule wraps around an octamer of four histones with a linker histone (H1) at the base leading to compaction of nucleosome clusters. Nucleosome clusters deprived of linker histone (H1) decondense and rearrange themselves into ‘beads-on-a-string’ configurations [Thoma et al., 1979]. The DNA sequence has a highly consistent length of 147 base-pairs across nucleosomes. Overall, there is a very good understanding about the chromatin organisation at the DNA and nucleosomal level, but the way chromatin is compacted at higher levels is still oblivious, despite the recent evidence from genomic and microscopy studies.
Due to its significantly higher resolution, previously EM has been a very powerful method to study organisation of chromatin at various length scales. EM could distinguish structural elements such as heterochromatin, nuclear pores or mRNA. Experimental destruction of chromosomes [Cremer et al., 1982b, Cremer and Cremer, 2001] showed that chromosomes barely intermingle inside of the nucleus and for the most part are organized in distinct territories [Zorn et al., 1976, 1979, Stack et al., 1977]. Nevertheless, between these two contrasting levels of chromatin organisation: the nano level (DNA double helix, nucleosome level) and the micron level (chromosome territory level), how chromatin is organized is not well understood. Recent experiments from high resolution microscopy, genetics and genomics have brought new observations to light regarding the apparent hidden complexity of interphase chromatin (Figure 1.8). Methods such as nucleosome profiling or HiC have provided valuable information, but at the same time convoluted the picture of nuclear processes and structural features. As a consequence, there is still not a consensus regarding the way interphase chromatin is organised. Genomics has brought some strong clues, but this information is mostly population-based and suffers from strong cell to cell heterogeneity. As a result, it is hoped that single-cell information coming from microscopy and also from single-cell genomics provides the missing information re-

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<td>Chromatin territories, chromatin domains, chromocenters, nucleoli, nucleosome clusters, DNA fibers</td>
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<td>SMLM: standard fluorophores (histone modifications or other proteins)</td>
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Figure 3.1: Methods from microscopy and genomics to capture chromatin structural patterns.
required to understand chromatin architecture. Figure 3.1 presents various methods from microscopy or genomics to study chromatin architecture.

In this chapter and Chapter 4 on the organisation of meiotic chromosomes, I tried to gather some evidence regarding the organisation of chromatin at multiple levels that I could capture during my PhD studies. I will show how microscopy at single molecule resolution can be a useful tool to identify the different levels of chromatin compaction, from the nucleosome level up to the level of the metaphase chromosome. One of the challenges is the scarcity of data. Here, using newly established SMLM applied to conventional DNA dyes, I highlight the different levels of chromatin compaction. In reverse hierarchical order, I will start by the concept of chromatin territory, which states that chromosomes have defined regions within the cell (Section 3.2.1, scale of 1 to 2 µm). I will then present subchromosomal domains, which are bulky parts of the chromosome territory with potential functionality (Section 3.2.2, scale of 500 nm). I will show how chromatin domains now emerge as fundamental building blocks of chromatin, at least from the point of view of a biologist (Section 3.2.3, scale of 100-400 nm). These regulatory domains have a strong potential to be functional units of chromatin and their detection here is backed up by recent data from genomics. I will finish by describing lower orders of chromatin folding, including nucleosomes and chromatin fibres (Section 3.2.4 and Section 3.2.6). I hope that these findings will help to define a framework for the further investigation of chromatin structure and function.

3.2 The hierarchical organisation of chromatin

There are two classical views about how the interphase chromatin is organised at the highest level of hierarchy. The first is the compartmentalization of nucleus into distinct and functional chromosome territories and the other is the classical bimodal euchromatin and heterochromatin model. In this section, I will provide recent evidences from single molecule localisation microscopy to get a more detailed structure of interphase chromosomes and how their hierarchical nature might result from association of fundamental building blocks of chromatin.

3.2.1 Chromosome territories (scale: 1000-2000 nm)

As mentioned in the first chapter, interphase chromatin has long been described as an alternation of dense and loose chromatin, i.e. heterochromatin and euchromatin, with no further complexity. With time, the idea that chromosomes follow a territorial organisation slowly became established [Cremer and Cremer, 2001]. Later, it was shown that chromosome territories do exist and are well conserved between different cell types [Mayer et al., 2005]. The paradox between the existence of chromosome territories and the lack of visible territories
in electron microscopy has recently been solved by the emergence of super-resolution microscopy. By relying on the detection of single molecules rather than on the capability of the sample to transmit an electron flux, these methods have drawn a clearer picture of the organisation of DNA and associated proteins in the interphase nucleus [Cremer et al., 2006]. Interphase chromatin is presently described as chromatin networks and foci, separated by caveats, as exemplified by EM images [Branco and Pombo, 2007, Markaki et al., 2010]. It is thought that most of these caveats are the place of protein machineries such as transcription factories [Iborra et al., 1996, Sexton et al., 2007] and alternative splicing complexes known as speckles [Zirbel et al., 1993, Puvion and Puvion-Dutilleul, 1996]. Transcription factories co-localise in DNA void regions while the speckles have been shown to anti-localize with DNA elements [Zirbel et al., 1993, Cremer and Cremer, 2001, Markaki et al., 2010]. In this first section, I will show how SMLM can be used to get information about chromatin and reveal some structural properties of CT and other nuclear features belonging to a high-order level of structure.

Figure 3.2: A simulated chromosome territory map (CT) based on SMLM data. Top panel: The nearest neighbour based clustering is used to segregate chromatin into 46 distinct clusters representing individual chromosomes and marking their individual territories. White lines show the delimitations of three chromosome territories. Yellow line highlights a putative active interchromosomal territory (IT). Bottom panels: Magnifications of top panel. In white are depicted three chromosome territories and an hypothetical region of active chromatin is displayed in yellow. Scale bar: 2 µm.
Nearest neighbour clustering identifies chromosome territories and inter chromosomal compartments

Nearest neighbour molecules information was used to predict territories of different chromosomes. The algorithm generates a hierarchical cluster tree of localization data using the MATLAB built-in function `linkage`. This function links pair-wise fluorophores in order to form clusters, then links the clusters again pair-wise and so on. The process is iterated until only one cluster is found. A parameter threshold that helps to decide when to separate territories, was set to fit the number of expected regions (39 territories here). The resulting image is a mosaic of clusters that are predicted to be chromosome territories (Figure 3.2). Further validation is required to prove whether the prediction of territories positions is correct. This could be done using FISH or additional labelling techniques.

Interestingly, the picture also reveals regions of lower density (dark regions) which are overlapping two to four chromosomes. This pattern is a putative inter-chromosomal territory, a region of the nucleus thought to be the place of active transcription, while the core of the territory displays a more condensed chromatin [Cremer and Cremer, 2001] (yellow territory in Figure 3.2, see also Appendix A.1). The alternation between light and dark regions of Figure 3.2 further validates the CT/IT model proposed in [Cremer and Cremer, 2001].

![Image](image.png)

Figure 3.3: Identification of subchromosomal territories. Top ppanel: The number of signals is gradually increased from 10000 to 100000 to reconstruct the final image. Bottom panel: corresponding values of localisation precision. Irrespective of the increase in number of signals, the average localisation precision is found to be around 20 nm in each case. However, increasing the number of signals acquired helps to identify sub-chromosomal territories (top right panel).

Good labelling density is required to distinguish chromosome territories and sub-chromosomal compartments

Single molecule microscopy is highly useful to identify the precise location of molecules and distinguish signals whose relative position with respect to the neighbouring molecules is not distinguishable in conventional microscopy. Moreover, by gradually increasing the number of detected molecules, one is able to refine the description of various nuclear structures. Figure 3.3 shows the minimum number of signals required to distinguish various nuclear compartments. For
instance, the nucleolus is only visible for 100000 signals detected. Conversely, a much higher number of signals is required to distinguish individual chromatin domains and the dense chromatin at the nuclear periphery commonly seen in EM images (Figure 3.3). Another thing worth noting is that localisation precision remains around 20 nm throughout our analysis.

SMLM reveals putative sites for transcription

Our SMLM setup is useful at probing chromatin structures without prior knowledge about the underlying DNA topology or sequence. One such interesting structure revealed is the discrete sites of gene expression called transcription machineries [Sutherland and Bickmore, 2009] different from the nucleolus. The nucleolus is known to be a large nuclear compartment devoted to constant transcription of ribosomal RNA (see the seminal study of nucleolus RNA by Gall and Pardue in [Gall and Pardue, 1969]), found in both widefield and confocal images. The representation is globally the same at microscopic level using SMLM even with a low number of frames, for instance 5000. Nevertheless, when augmenting the number of frames to 20,000, new structures start to emerge, of round shape, similar in nature to nucleoli structure, but 50 times smaller (Figure 3.4, right image, see also Figure 3.29). It is hypothesized that these are the sites of machineries transcribing a cluster of genes. One can relate these patterns to a possible low diversity of genes transcribed at single cell level.

Conventional light microscopy (LM) has already shown some sub-chromosomal structures of chromatin [Mora-Bermúdez and Ellenberg, 2007, Dietzel et al., 2004], but due to the resolution limitations of LM (∼ 200 nm), the precise organisation of chromatin during interphase is barely described. Though transmission electron microscopy has been spectacular at describing the nanoscale structure of cellular objects [Haggis, 1992, Dehghani et al., 2005] (see comparison to high resolution microscopy in [Betzig et al., 2006]), superresolution methods have

Figure 3.4: Sub-chromosomal regions corresponding to potential transcription machineries distinct from nucleolus are revealed by SMLM with a high frame number. On the left, a widefield image of a sample. On the middle panel, a picture with 5000 frames. In both widefield and low frame number, only two giant nucleolus foci are visible. On the right, a high number of frames reveals emerging structures corresponding to potential transcription factories (Figure and caption modified from [Zurek-Biesiada et al., 2015]).
been a real advancement in localising individual molecules inside the nucleus.

Here, SMLM was used to image the chromosome territories of an interphase nucleus of a primate fibroblast (Figure 3.5). Magnification and manual segmentation of chromatin structure helps at describing sub-regions of chromosome territories, as proposed in [Cremer and Cremer, 2001]. Between different dense regions, one can easily distinguish corridors, which are likely to give freedom for transcription machinery to function (Figure 3.5, top inset), though only staining for RNA Pol II or messenger RNA would allow to confirm this hypothesis. The pattern observed follows the model of chromosome territories described previously [Cremer and Cremer, 2001], with chromosome territories showing the shape of grapes, each of the grains representing a sub-chromosomal domain (Figure 3.6A).

3.2.3 Chromatin domains (scale: 100-400 nm)

Recent proof of a universal chromatin domain morphology in mammalian systems

Genomics has recently generated exciting maps of chromosome interactions within the nucleus, via chromosome capture technologies (3C, HiC and others, see Figure 1.8). These maps have allowed to identify structural regions called Topologically Associating Domains (TAD). Functionally, this kind of structure comprises genes and remote regulatory regions, and correlate strongly with replication domains [Ibn-Salem et al., 2014, Pope et al., 2014]. Structurally, a TAD is an element of about 185 kb in mammals, ranging from 100 kb to 1 Mb [Rao et al., 2014]. Low-throughput experiments have been made to validate these structures using DNA probes, however no study has tried to give these genomic data a visual perspective. Thus, a detailed
description of fundamental building blocks of chromatin, beyond nucleosome and chromosome territory scale linking genomic data to microscopy data is of immediate importance. For example, how do one-dimensional genome browser or HiC plots (from sequencing data) correlate to microscopy data? Say one observes 100 nm clusters containing 40 signals of activating mark H3K4me3 on microscopy images and finds several peaks on the same region in a ChIP-seq dataset for H3K4me3 (in a similar cell line). How can one relate the two kinds of data? Some models have been described, that attempt to address this problem, but these are mostly theoretical without experimental basis (Figure A.2).

Recent studies based on FISH and super-resolution microscopy have estimated the sizes of clusters to be between 50-400 kbps and around 100-500 nm spatially ([Prakash et al., 2015, Boettiger et al., 2016], and Chapter 4 of this thesis). The regions probed were selected based on combination of histone modifications, distinguishing active, inactive and repressed regions. Overall, the studies provide evidence that there is a functional fundamental building block of chromatin around 100-400 nm confirmed by microscopy data (see Figure 3.6, the different categories of active and repressed chromatin, red and blue boxes in panel A, respectively). From the center of a domain to the periphery, a gradient is observed, from highly dense chromatin, which is likely compacted, to chromatin of low density, which is loose and probably an active place of transcription (Figure 3.6B, white box). In a different analysis, chromatin at the periphery of a domain was associated to intense DNA transcription and stress-dependent gene activity (see Section 3.4 for more details).

In a recent study [Boettiger et al., 2016], active, inactive and repressed chromatin domains were studied based on ChIP-seq data of histone modifications from [Filion et al., 2010]. The authors chose H3K4me2 (which marks both enhancers and promoters [Barski et al., 2007, Wang et al., 2008]) as the mark to study active chromatin domains. H3K27me3 was chosen to mark the repressed and condensed chromatin. It must be noted that H3K9me3 is the mark of the most condensed chromatin while H3K27me3 often localises at the periphery of H3K9me3 and is slightly smaller in size than H3K9me3 clusters [Prakash et al., 2015]. Nonetheless, in the study from [Boettiger et al., 2016], the active regions based on H3K4me2 could roughly be divided into two categories: short active regions, around 50 kb and of 100-200 nm of radius, and long active regions, around 100-200 kb and of 200-400 nm. Repressed regions based on H3K27me3 designated as regions of most condensed chromatin (corresponding probably to the early concept of ‘heterochromatin’), were restricted to a 100-200 nm size.
SMLM identifies chromatin domains without prior knowledge about the function or sequence

The data from Boettiger et al., 2016 were generated using DNA probes coupled to fluorochromes and directed toward specific DNA sequences. Interphase chromatin using our SMLM setup that uses conventional DNA binding dyes or EdU coupled to a fluorochrome was also explored. The image of interphase chromatin (Figure 3.6) identifies different chromosome territories, sub-chromosomal domains (panel A, white broken lines), chromatin domains (panel B, white stars), categories of chromatin domains (panel A, blue and red for repressed and active domain, respectively), and loci with different levels of compaction (inset A1 and A2, with denser region in the center in blue and active region in the outer region in red).

In order to highlight the hierarchical levels of chromatin folding, EdU was coupled to a fluorochrome, showing the positions of freshly replicated DNA molecules within the nucleus. As the targets are theoretically unbiased, a complete view of chromatin distribution within the nucleus was possible (Figure 3.7). Domains are found to be in the range of 100 to 500 nm, as predicted by other methods (see Figure 3.16 for comparison, red rows). Moreover, magnification of the domains reveals smaller highly identifiable spots, likely to be individual loci, possibly nucleosomes (Figure 3.7A1 and Figure 3.7A2).
**Universality and functionality of chromatin domains**

With respect to recent literature, chromatin domains have started to emerge as the units of genetic regulation, with two important characteristics:

1. **Universality of the patterns**: In HiC experiments, chromatin domains (the term used in genomics is topologically associating domain, or TAD) were found to be about 90% cell-type independent (2763/3000 conserved boundaries between two assayed cell types [Dixon et al., 2012]). The 100-400 nm scale is confirmed in recent studies [Prakash et al., 2015, Boettiger et al., 2016], indicating a very high consistency and possibly universality of chromatin domains. However, one should be cautious in comparing the data, because most of HiC data come from mammals while the work of [Boettiger et al., 2016] was conducted in Drosophila. Moreover, the relevance of the patterns found in HiC data is challenged by the low amount of reads (poor sequencing depth) generated by this type of analysis (Figure A.3).

2. **Functionality of the patterns**: Chromatin domains facilitate function by bringing genes and their regulatory elements closer to each other, with an optimum at 50 kb distance [Doyle et al., 2014]. The first comprehensible equivalence between genomic and physical distance provided by [Boettiger et al., 2016] confirms this value. A pure threading pattern of fibres would never allow these sorts of patterns, which hints at folding for both active and inactive regions of the genome at TAD, following models from [Rao et al., 2014]. In terms of functionality of chromatin domains, [Prakash et al., 2015, Boettiger et al., 2016] show that these chromatin domains come from epigenetically characterized regions. Thus, the results presented in Figure 3.6 and Figure 3.7 further show the potential to find different morphologies of compaction among these patterns.
3.2.4 Chromatin fibres (scale: 30-100 nm)

Measurements of DNA is key to describe chromatin accurately. Describing a heterogeneous polymer as complex as chromatin requires to identify its most fundamental elements. Early studies of chromatin spectrum showed several peaks at 110, 55, 37, 27 and 22 Å, shown to be in the direction of the axis of the helix (values highlighted in [Finch and Klug, 1976]). Later this proved to be corresponding to a beads-on-a-string pattern with a width of 8 nm, below an expected 11 nm diameter. The value of 11 nm was confirmed later (see [Luger et al., 1997] for instance). First measurements of DNA and DNH (nucleohistone) led to an early incorrect model of chromatin. The molecules of DNA were thought to be in the center of the structure, and the histones at the periphery, though diameter was correctly predicted to be 10 nm [Luzzati and Nicolaieff, 1963]. Later experiments proved that the real structure follows a different configuration, with DNA molecules wrapping around an octamer of 4 histone proteins. In-vitro evidences from Olins [Olins and Olins, 1974] have described strings of nucleosomes more or less packed and have provided solid evidence for the existence of fibres, but this, only in in vitro studies.

Seminal study from Finch and Klug led to the description of a higher compacted state of chromatin, that was named ‘chromatin fibre’ with a width of 300 Å. Nevertheless, a close look at pictures reveals that there is an intrinsic variability and that the width of elementary chromatin size spans from 30 nm to 70 nm (Finch and Klug 1976). Though Maeshima et al. [Maeshima et al., 2014] argue that this finding is highly depending on salt concentration, these pictures are likely to capture some elementary features of chromatin. The study also showed that each transversal section of chromatin comprises about 4-7 nucleosomes, leaving a first estimation of correspondence between distances in nm and kb. As found, 12 (visible) nucleosomes of about 200 bp each (if compaction is maximum) multiplied by a factor 2 (to take into account nucleosomes that may not visible), compaction is estimated to be 5-fold. As will be seen later, that is largely an underestimation. An earlier finding from Joseph Gall estimates the diameter of a chromatin fibre around 40-60 nm [Gall, 1963].

Different patterns have been seen for chromatin fibres, with more or less nucleosomes visible across transversal plane but this is explained by different relaxation levels of the fibre, highly depending on environmental conditions [Bassett et al., 2009]. Opponents to chromatin fibres have proposed a solenoid model [Dubochet et al., 1986], though possible in theory, does not threaten the concept of fibre and the possibility to build higher order building blocks. Enlightening study from Woodcock and collaborators [Woodcock et al., 1984] has shown how a fibre-like (or solenoid-like) chromatin of 30 nm diameter leads to higher orders of chromatin folding. A very revealing image from their report is reproduced here showing the transition between three turns of the 30 nm chromatin fibre and a more compacted pattern of about 100 nm diameter, a putative chromatin domain (Figure 3.8).
It is a rare case of pattern showing transition between two levels of chromatin compaction, giving a hint about the way structure builds itself hierarchically.

This direct proof of evidence of hierarchy between the fibre and chromosomal domains has not been highlighted in literature, to a point that some researchers now question the existence of fibres. Scarcity of evidence led some authors to recently dispute the concept of chromatin fibre [Fussner et al., 2011], but the question remains open as the article failed at disproving the notion and based its assumption on a spectrum, which can be very well disturbed by the multilevel complexity of chromatin. More evidences account for the high conservation of a level of chromatin compaction in order 40-60 nm across cell types and species [Mayer et al., 2005, Harmon and Sedat, 2005]. Generally accepted is the idea that fibres can display several levels of compaction and diameter ranges between 30 to 60 nm (Figure 3.16).

Various groups have experimented new optical devices in order to get insight into fundamentals of chromatin architecture. Most of direct images of in vivo chromatin have been low resolution, and so far only Scanning Electron Microscopy (SEM) and Atom Force Microscopy (AFM) have been able to give a good idea of the actual shape of chromatin. Spectacular images of chromatin from 3T3 cells taken with SEM by Haggis [Haggis and Pawley, 1988, Haggis, 1992] show chromatin architecture as a combination of bulky (‘balls’) and elongated regions connecting ‘balls’ together, the ‘linker’ domains (see Figure 3.9). Measurements of the two categories reveal a configuration of fibres compatible with previous findings of Joseph Gall [Gall, 1963]:

• ‘balls’ display an apparent size of 42 nm.
• ‘linkers’ which bind the ‘balls’ of length 100 nm on average. Width is close to 40 nm.

The compaction here is not a thread, but a rather cluster on a string. Each cluster or ‘ball’ is a product of compaction of many nucleosomes (size: 7 nm), possibly several hundreds, for about 50 kb of DNA length. Besides, AFM has been used by Ushiki and Hoshi [Ushiki and Hoshi, 2008] to image mitotic chromosomes. Authors find similar ‘ball and stick’ patterns, whose sizes are approximately 50 to 60 nm (see the comprehensive scale in [Hoshi and Ushiki, 2001] and figure 4c in [Ushiki and Hoshi, 2008]).

To summarize, history of chromatin research in the last decades has demonstrated the existence of at least two levels of DNA compaction, beyond nucleosomes. One is the 30 nm chromatin fibre, which has been demonstrated beyond shadow of a doubt in several instances. The picture can be a little refined by saying that this element is in most cases not elongated, but rather shrinks to form higher order structures, questioning the epithet ‘fibre’. Nevertheless, in several instances (relaxed interphase chromatin, pachytene loops), the term fibre is highly appropriate. One should forget the picture of chromatin as a thread of fibres and replace it by a more complex fibre, which
gives birth after folding to a second level of DNA compaction, which is the building block of chromatin regulation (the chromatin domain, whose size is of 100-400 nm).

Finally, I mention the accepted idea that chromatin fibres are one level of ordered compaction of DNA during mitosis (see [Ushiki and Hoshi, 2008] for nice AFM pictures showing both fibres and chromosome domains; see also Figure A.4). Beautiful imaging of condensin proteins together with DNA have helped build one of the best models of chromatin architecture proposed until today, with a condesin core holding chromatin around in a regular pattern ([Maeshima et al., 2014], Figure 6).

Figure 3.10: Bead on a string model. Monkey kidney fibroblast-like cell stained with Vybrant Violet to reveals positions of chromatin with several levels of magnification, A, B, C and F. In the magnified section C, it is interesting to note the beads-on-a-string-like patterns that are commonly seen in EM images of 10 nm in vitro nucleosome structures, which fit with the scale bar (200 nm in the inset). The average density is around 3000-4000 molecules per µm². The localization image was acquired with a high intensity laser excitation 491 nm, detecting more than 1300000 signals in an optical plane through section of approx. 500-600 nm. The mean localisation precision was 15 nm with a standard deviation of 4 nm. In D random distribution of C is presented, in G random distribution of F. In E and H the positions of the single molecules are displayed.

3.2.5 A cluster-on-a-string model to describe the fibre/domain transition

In order to describe transition between fibres to chromatin domains, one could imagine chromatin domains as clusters on a string. The
the periodic and dynamic structure of chromatin

chromatin fibres of 30 nm would be the string that link two or more domains together. On Figure 3.9, one can see the white peanut-shape regions as the clusters, while fibres could be the darker grey regions between them. This model is one level higher compared to the bead-on-a-string model in the hierarchy of chromatin compaction and is a sort of intermediate chromatin organisation between the lowest levels of compaction and chromosome or sub-chromosome territories. Imaging of chromosome in meiosis shows that this type of structure is maintained during meiosis and is potentially even more visible on SMLM preparations of meiotic chromosomes if staining against histone modifications such as H3K4me3 is used [Prakash et al., 2015].

3.2.6 Nucleosome domains (scale: 10-30 nm)

A number of studies have dealt with chromatin fibres at a scale of 30 nm and have tried to establish fibres as the basic structures of chromatin both in inter- and metaphase [Frenster et al., 1963, Hay and Revel, 1963]. A few studies [Davies, 1968, Davies and Small, 1968] have pointed out that chromatin is more or less distributed randomly towards the interior (mostly euchromatin) while periodic lumps of chromatin are attached to the nuclear periphery (mostly heterochromatin). In the following section, I revisit this idea from single molecule co-ordinate information and try to explore it further.

Nearest-neighbour method identifies worm-like patterns

In order to study the structure of chromatin at the lowest order, I analysed images of fibroblasts (Figure 3.10). On the magnified image, the distribution of bead sizes shows an average diameter of 10 nm, in line with the historical measurements of these structures [Oudet et al., 1975, Olins and Olins, 2003]. In order to give more weight to these beads and strings associations and validate the patterns, I used blurring of nearest-neighbours. Applied to HeLa cells, this technique resulted in finding worm-like patterns of roughly 5-10 nm of periodicity (Figure 3.11), close to the magnitude of the theoretical nucleosome size [Oudet et al., 1975]. On the magnification presented in this figure, one can note some highly identifiable shapes in the decondensed chromatin, which form circles and crosses.

Comparison of the worm-like pattern to simulated random patterns

To understand if the worm-like pattern or beads on the string pattern is a real structure, I simulated the same type of data using a stochastic distributed process to produce the locations. Surprisingly, I could find similar and comparable worm-like structure with overlaid density variation (Figure 3.12).

If the building block is real, the shapes created at scale of 100 nm on this picture could be potential artefacts and the result of a random superimposition of basic patterns. Though one cannot conclude on the relevance of the shape of the chromatin patterns seen around 100

Figure 3.11: Inverse distance map of pixels based on the next 5 neighbours. The distance of the center of a pixel i to the next 5 locations is measured and averaged. 1/mean distance is then assigned as a grey value to pixels i. The procedure is iterated over all pixels in the image (even those where no fluorophore resides in). The image is then scaled to 8 bit. Is the worm-like pattern a real structure? The cell imaged is a HeLa cell stained with Hoechst 33258.

Figure 3.12: Comparison of chromatin patterns in random and experimental data. (Left) Simulation. An image was generated with locations produced by a stochastic gaussian distributed process. (Right) Measurement. Comparable worm-like structure with overlaid inverse distance variation are observable. The cell is the same as the one on Figure 3.11. For the simulated image, the density map is based on the list of localisations or single molecule coordinates. For every pixel in the image the local density is measured based on the mean distance to the next 5 neighbours in the list of localisations. The reciprocal value of this mean distance is then mapped to the corresponding pixel.
nm, one can still observe more accurate patterns that can be seen at higher scale by using nearest-neighbour methods.

![Image of chromatin patterns](image)

**Figure 3.13**: Comparison of chromatin patterns generated with random simulated data to experimental data when different number of nearest-neighbours are taken into account. Top block: Random case. Bottom block: SMLM Measurement. From left to right, influence of the number of next neighbours is considered. In each block, the second row shows the region highlighted with a red box in the first row. In the case of the random configuration, worm-like structures are visible at all scales. In the case of the real data, the worm-like structure vanishes when enough next neighbours are taken into account. Same cell as in Figure 3.11.

**Nearest neighbour method helps to capture further chromatin complexity using combinations of building blocks**

I then increased the number of nearest neighbours taken for calculation of mean distance and I observed that in the random data worm-like structures were visible at all length scales. According to the theoretical definition, random data is one which is not correlated and therefore does not change under scaling. Interestingly, the worm-like structures vanished when enough next neighbours were taken into account (see Figure 3.13.).

While the low scale patterns found using nearest neighbour are likely to correspond to topologically associating domains of low scale of around 100 kb (‘chromatin domain 2’), the higher order elements defined here correspond to the ‘chromatin domain 1’ and TAD of about 1Mb (see Figure 3.16 for nomenclature). The former are around 100 per chromosome, while the latter are 10 per chromosome and may be equivalent to active genomic regions of high gene content.

**Quantification of chromatin condensation**

I next quantified chromatin compaction in SMLM images by analyzing distances to 5, 10, 20, 50, 100 nearest neighbours (Figure 3.14).
Considerable differences were observed between the experimental data and randomly simulated data. First, the nearest neighbour distances (NND) in the experimental measurements were considerably less than the random simulated when enough number of nearest neighbour was taken into account. Significant differences started to emerge using 20 to 100 nearest neighbours (65 nm vs 80 nm). This fact was indicative of local condensation in the experimental data and also provided the expected degree of condensation. Secondly, the distribution of NND in the experimental started to broaden up as the number of nearest neighbour molecule increased. The broadening of peaks can be attributed to the fact that the sparser distributions of chromatin might be represented at the boundary of condensed chromatin, a common feature of chromatin organisation (please refer to Figure 3.6).

3.2.7 Inference of further intermediate chromatin structures using local chromatin density maps

Images of isolated molecules appear to be similar to the beads-on-a-string-like patterns that are commonly seen in EM images of folded chromatin in vitro (Figure 3.15). To further investigate this hypothesis, the experimental data were compared with the random simulated data. Comparison of the local inverse distance maps with the distance maps generated by a random process shows that at a larger scale there is a local condensation of the fluorophores whereas at a finer scale the structure becomes random. In the case of real data, the large structures are different from the structures that one observes at a finer scale - which are ‘wormlike’ shape. In random data, the worm-like pattern is visible at all scales. This result shows that one cannot resolve the fine substructure because there is none. The molecule signals are real, but the patterns at low scale are not meaningful. Only at a larger scale structure becomes dominant. Hence, organisation of chromatin is clustered at large scales but distributed randomly at fine scales. If our result is confirmed in the future by complementary experiments, our method will prove competence at detecting beads-on-a-string patterns in situ, which is not possible with other current
structure, function and dynamics of chromatin

methods so far.

![Figure 3.15: Inference of pattern from local chromatin density maps. (Left) A composite image shows the impact of blurring and condensation enhancement when different number of nearest neighbour (NN) are taken into account. (Right) Same cell with 5 nearest neighbour blurring. The far left block in both images (5 NN) are identical. Scale bar: 1µm.]

### 3.2.8 Hierarchical organisation of chromatin structure

I finally summarize information from literature and personal findings regarding chromatin architecture and its different levels of hierarchical compaction in Figure 3.16. The table shows the hierarchy of chromatin organisation from nucleosome to chromosome territory, including the building block of a size around 50 nm. In Section 3.2.6, a 50 nm pattern is visible with superresolution microscopy performed on interphase cells. Similar configurations are further shown in stem cells and confirm the existence of functional chromatin clusters around 50-100 nm using the meiotic chromosome as a model, and histone modifications H3K27me3 and H3K4me3 as targets, instead of DNA itself (see the Chapter 4 on meiotic chromatin).

### 3.3 The dynamics of chromatin

Only recently, gene regulation has started to be seen as the result of chromatin dynamics inside of the cell nucleus. A way for chromatin to be dynamically regulated is to switch between heterochromatin and euchromatin states. Electron microscopy, though of high resolution, is poor at identifying regions of low density, such as euchromatin [Cremer et al., 2006], though usage of an expended protocol for Giemsa staining has been shown to turn euchromatin denser and so reveal chromosome territories [Stack et al., 1977]. In any case, for a long time, the description of chromatin was confined to distinguish dense and clear regions as compact chromatin (heterochromatin) and relaxed chromatin (euchromatin) respectively, the latter being the place of transcription. Besides, other nuclear components such as the nucleolus were also identified.
The periodic and dynamic structure of chromatin

<table>
<thead>
<tr>
<th>Study</th>
<th>Chromatin feature</th>
<th>radius (nm)</th>
<th>Length (bp)</th>
<th>Method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Olins and Olins 1974</td>
<td>Nucleosome fiber</td>
<td>8</td>
<td>147 bp</td>
<td>EM</td>
</tr>
<tr>
<td>Finch and Klug 1976</td>
<td>Chromatin fiber (thin)</td>
<td>30</td>
<td>?</td>
<td>EM</td>
</tr>
<tr>
<td>Higgins 1992</td>
<td>Kinks and thick fibers</td>
<td>Kinks: 46-60 nm Linkers: 40 nm</td>
<td>?</td>
<td>SEM</td>
</tr>
<tr>
<td>Heng et al. 1996</td>
<td>Mitotic chromatin fibers</td>
<td>60</td>
<td>110 kb</td>
<td>EM</td>
</tr>
<tr>
<td>Woodcock et al. 1984</td>
<td>Transition chromatin fiber to chromatin domain</td>
<td>Fibers: 38 nmDomains: 100 nm</td>
<td>?</td>
<td>SEM</td>
</tr>
<tr>
<td>Cremer et al. 2000, Cremer and Cremer 2001</td>
<td>Chromatin domain type 1 Chromatin domain type 2</td>
<td>Type 1: 500 nm – 1 μm Type 2: 100 nm – 300 nm</td>
<td>Type 1: 1 Mb Type 2: 100 kb</td>
<td>Chromatin treatment and LM (for Type 1)</td>
</tr>
<tr>
<td>Roettiger et al. 2016, Prakash 2016 (this report)</td>
<td>Chromatin domains</td>
<td>100-400 nm</td>
<td>From 50 kb to 400 kb</td>
<td>SMLM</td>
</tr>
<tr>
<td>Prakash et al. 2015</td>
<td>Mitotic chromatin domains</td>
<td>50-100nm</td>
<td>?</td>
<td>SMLM</td>
</tr>
<tr>
<td>Lieberman-Aiden et al 2009, Kahor et al. 2011</td>
<td>Fractal globule</td>
<td>?</td>
<td>From 50 kb to whole chromatin</td>
<td>HC</td>
</tr>
</tbody>
</table>

For historical purpose, I have showed in the first chapter a photograph of a classical euchromatin/heterochromatin dichotomy, generated from a human leukocyte (Figure 1.5). A characteristic very thin layer of heterochromatin is present close to the nuclear envelope, while most of the center of the nucleus is the place of a loose chromatin (white arrows). The nucleolus, which is the place of active transcription of ribosomal RNA, is the large dense cluster in the middle. Some stem cells show a contrasting phenotype with euchromatin in the exterior and hetero-chromatin toward the interior. This is discussed in the following section.

### 3.3.1 Contrasting arrangement of eu- and hetero-chromatin inside the cell nucleus

Previously, chromatin was broadly divided into classical bimodal model i.e. euchromatin and heterochromatin regions. Euchromatin is the open and transcriptionally active compartment of chromatin, mostly found in the interior of the cell, and mostly associated with histone acetylation and certain histone variants. Heterochromatin is condensed and is mostly found at the nuclear and nucleolar periphery. It is also usually referred to as ‘silent DNA’. Repressive histone marks and hyper-methylated DNA are characteristics of heterochromatin.
A comparison of fibroblast cells and mesenchymal stem cells shows that this textbook picture is rather the characteristic of the pattern observed in the fibroblast. Images show a clear contrast between compact and relaxed chromatin, as well as a predominant nucleolus (Figure 3.17A, monkey fibroblast). On the opposite side, stem cells have a broader spectrum of gene expression and show several foci of heterochromatin in the middle, possibly by migration of heterochromatin away from the lamina (Figure 3.17B), from a mouse mesenchymal stem cell).

3.3.2 Classifier identifies intermediate states between eu- and heterochromatin regions in differentiated cells

I developed a new method called Pixel Density Classifier (PDC) to classify localisation microscopy data into regions with different spatial densities and structural features. I applied PDC to select different levels of chromatin compaction on SMLM images (Figure 3.18). Setting the parameter to three different levels of chromatin compaction, I could define three compartments with different densities: one is associated to a loosened state of chromatin, present in the nucleus as large foci (Figure 3.18C) and corresponding most likely to transcription machinery compartments (which bare chromatin speckles, place of splicing machinery; see similar patterns stained with antibodies against speckles on Figure 6 in [Cremer and Cremer, 2001]). The second degree of compaction (Figure 3.18D) is the surrounding area of these foci; this category has the largest distribution of the three and mostly corresponds to euchromatin, that is, the part of chromatin deployed out of the chromosome to be transcribed. Finally, dense chromatin (heterochromatin) is found at the outer part of the nucleus (Figure 3.18E).

3.3.3 Chromatin dynamics during differentiation of mesenchymal stem cells

In order to study dynamics of chromatin, I present an example in Figure 3.19 which shows two images of differentiated and undif-
ferentiated mesenchymal stem cells. From this data, one can draw scenarios regarding the timing of chromatin dynamics during differentiation, even if refined synchronization is needed to capture the entire dynamics.

Step captured in Figure 3.19A slightly precedes Figure 3.19B. The chromatin has almost the same level of compaction. Nevertheless, binning the level of compaction into three levels shows that first figure displays elongated patterns of chromatin of intermediate compaction level, forming threads, showing the progression of chromatin towards condensation in the middle. Figure 3.19B is a slightly later time point, when the compaction is maximum.

Such particular patterns have been also observed previously in [Popken et al., 2015]. The intermediate stages of the stem cells associated with central heterochromatin islands are reported. Differences between ESC versus differentiated cells chromatin status have been also exemplified in [Mikkelsen et al., 2007], confirming the model.
3.3.4 Dynamics of chromatin upon stress

Stress as a good model to study chromatin dynamics

In order to capture the changes that chromatin can experience during a dynamic process, cardiomyocytes under a cellular stress mimicking infarctus, ischemia, were imaged using SMLM. Stress has been shown to remodel chromatin \cite{Johnson2007, Hargreaves2011} and seems to be a good source to study dynamics of chromatin. Extreme patterns of stress highlighting specific ring-shape patterns, likely for mechanistic protection, were previously reported in \cite{Everid1970}. This study shows compaction patterns of chromatin following citrate treatment of chicken erythrocytes.

In the present study, the effect of environment on chromatin nanostructure with SMLM and 3D structured illumination microscopy (SIM) was evaluated. Following a short-term oxygen and nutrient deprivation (OND) of the cardiomyocyte cell-line HL-1, chromatin architecture experiences a dramatic changes, adapting to large ring patterns, of 1 to 5 \(\mu m\) in diameter, with sparse voids inside. These rings most likely correspond to individual chromosomes, hinting at an intense chromatin compaction. The findings show a dramatic adaptation of chromatin to environment, probably due to a major change of energy status.

Distinct changes of nuclear morphology upon stress

In order to mimic ischemia, SMLM was employed on HL-1 cells transiently exposed to OND. OND procedure was performed by collaborators as follows: cells were put in a hypoxia chamber (Whitley...
the periodic and dynamic structure of chromatin

Figure 3.20: Chromatin compaction upon stress, stained with YOYO-1 (a-f) or Edu (g-l) and imaged via SMLM (figure and caption modified from [Kirmes et al., 2015]). YOYO-1 staining. a-c: untreated cells; d-f: cell subjected to one hour of OND. g-i: 24 hours of 10 μM EdU labeling. g-i: untreated cells; j-l: after one hour of OND. After fixation, EdU was fixed to AlexaFluor 488 via click chemistry in situ (see Zessin et al. 2012 for method). Regions devoided of chromatin are indicated by an asterisk, atolls are indicated by a white arrow. c, f, i and l: wide-field images corresponding to b, e, h and k, respectively.

Hypoxystation, see [Kirmes et al., 2015] for details) during one hour without any nutrient (ion solution with no organic molecules), to then recover by restoration of normal oxygen concentration and nutrients (Claycomb media). Localization maps were generated in minimum nine replicates for each condition, by integrating 30,000 observations capturing photons re-emitted by the samples after 50 ms of exposure. The images generated spots at the positions of molecules under the diffraction limit, at a structural resolution of 103 nm, which is actually above the theoretical resolution of 67 nm that can be expected.

HL-1 cells treated one hour with OND displayed a major change of their nuclear architecture. Chromosomes shifted from classical interphase territory distribution to a characteristic ring-shape. Most of the chromosomes are attached to one another, mostly at the periphery of the nucleus (Figure 3.20d,j). Certain chromosomes are bound to the lamina, with elongated patterns nicely exemplified by 3D surface plot in Figure P8. Almost all chromosomes are bound together and form a sort of continuous chain. No part of chromatin shows the diffuse chromatin pattern observed in untreated condition.

3.3.5 Reversible compaction of chromatin under stress

Next, a time course of chromatin organisation upon hypoxia (Figure 3.22) was evaluated. Stress induced posture happens within the one hour of induction, while relaxation takes up to four hours to reach complete normal state (Figure 3.22). The typical stress induced pattern is already vanished after 5 minutes, leaving the cell with a few caveats that disappear totally after 4 hour of relaxation. Additional images of the time course can be found in appendix (Figure A.5).

This pattern has been related by collaborators to H3K14ac signal during the same hypoxia process; result from confocal imaging shows that H3K14ac is reversibly vanishing during hypoxia (Figure 3.27 and [Kirmes et al., 2015], Supplementary Figure 4). This result hints...
at the restoration of the normal phenotype of the cell. Overall, the patterns observed upon stress demonstrate a protective rearrangement mechanism of chromosomes, associated with a reduction of transcription-related histone modifications.

**Nearest neighbour analysis to describe the extent of chromatin reversibility**

I then tried to describe comprehensively the dynamics of chromatin and its reversible characteristic by computing the distance distribution of the nearest neighbour molecules to regions of interest (ROI) and see how molecules are forming clusters during stress. I find that...
molecules clustering upon 1 hr of hypoxia tend to be kept away to each other at approximately 100 nm (Figure 3.23). The normal distribution is broader, showing a more diffuse pattern of chromatin, while the OND-induced condition is narrower and shows further distance, describing the observed clusters. The pattern shifts back to normal upon return to normal environmental conditions, with nearest neighbour distance showing broader distribution again, describing the diffuse pattern (Figure 3.23, 240 minutes).

To parametrise the method, I had previously tested the influence of the number of nearest neighbours to calculate the average distance to neighbours (Figure 3.23B). In the case of 1h OND, both median distance and breadth of distribution increase with the number of nearest neighbours, showing that low sampling favours neighbours from the same cluster while high sampling captures more complexity and more distant patterns.

I further plotted the distance to nearest neighbours for the different conditions (Figure 3.24). Interestingly, patterns show that the distribution of distances tends to have an exaggerated normal phenotype upon 4 hr of relaxation, with a mean distance lower for 4h relaxation than normal condition, and a narrower peak. This result hints at an even lower amount of caveats in the cell under relaxation, caused by an even higher diffusion than for normal state (as the distribution is shifted to the left in Figure 3.23A), associated potentially with small clustering difficult to observe by sight, of slightly granular shape (as the distribution is narrower, a characteristic of clustering behaviour seen in Figure 3.23A).

Such a pattern may be necessary for the cell to recover from damage, or is a sign of permanent DNA damage. Finally, the recovering pattern after 4h of relaxation may account for an anarchical distribution of chromatin, resulting in a random pattern of signal position.

Resolution estimation of DNA data

Monitoring the resolution for the different steps of the experimental procedure shows that resolution is better for the normal and post OND-induced conditions, while the OND states are more difficult to resolve (Figure A.6), probably due to condensation and formation of highly dense chromatin. This can come from a poor localisation precision of the signals in the case of the OND state (Figure 3.25).

3.3.6 Conclusion

I have shown in this section that our super-resolution setup is able to capture the dynamics of chromatin upon biological processes, using hypoxia as model. Such observations would be very difficult to observe using lower resolution methodologies as exemplified by comparisons of our results with widefield images and confocal images. Dynamics of chromatin under stress have shown exceptional patterns rarely described before (see early study by [Everid et al., 1970] on...
influence of citrate on chicken erythrocytes, which created foci of stress in chromatin). Our set up can also be used for biomedicine in order to further describe the consequence of ischemia for myocardiac cells.

Regarding cellular differentiation, chromatin dynamics is a drastic change in gene expression management. Differentiated cells show clear contrast of compact and relaxed chromatin, with an active region corresponding to the nucleolus which shows that translation is preponderant compared to transcription, leading to betting all nuclear energy on transcribing rRNA (Figure 3.17A from an adult mouse fibroblast). On the opposite side, stem cells have a broader spectrum of gene expression and show several foci of heterochromatin in the middle, by migration of heterochromatin away from the lamina (right picture on Figure 3.19, from a mouse mesenchymal stem cell).

From these basic morphologies, one can hypothesize that some kinds of cells do not need to transcribe a lot of genes, but ribosomal RNA; while cells with a stem capacity have to transcribe many specialized genes associated to differentiation and maximize transcription by migrating their dense regions toward the center, to increase the available space for genes to deploy their transcription machinery. Similar patterns have been also observed previously [Popken et al., 2015]. In this article, authors report intermediate stages of cells differentiation associated to central heterochromatin islands.

Findings presented in this chapter show both that cells have an intrinsic capacity to condense chromatin (the basis of all developmental processes) and that a cell about to die maximizes its protection mechanism by showing an extreme condensation phenotype. I do not claim here that the model of compaction holds true for every kind of cells, but that it could rather be a specific properties of certain stem cells which have a high potential of compaction (compactibility) as the genome is not completely folded yet and can be assumed in a ‘naïve’ state.

A model for chromatin dynamics

In the analysis of the differentiation of mesenchymal stem cells and more importantly of the reaction to hypoxia of HL-1 cells, a similar pattern is found: reprogramming of the cell, whether it is for enhancing gene expression at genome scale, or condensing chromatin for protecting DNA integrity, requires condensation or reshuffling in the center of the nucleus. DNA is still present at the lamina, though in little amount compared to classical euchromatin/heterochromatin dichotomy; in the case of mesenchymal stem cells, mostly all over the lamina, while in the case of HL-1 cells, at certain foci which possibly play the role of anchors. In a situation of massive gene regulation as early differentiation events, a big part of the genome can be bound to lamina and so be silenced. The situation for highly stressed cells is different: the entire chromatin has to be packed. In order to facilitate the process, the amount of chromatin attached to the lamina, a process
necessary for maintaining coherence of chromatin, has to be as little as possible, so the packing can be done on most of the chromatin.

3.4 The function of chromatin

Chromatin was initially defined as a nuclear material composed of histone proteins [Kossel, 1884], other proteins [Mirsky and Ris, 1951] and possibly RNA [Busch, 1974]. In order to refine the description of chromatin structure and correlate structure to function, information from histone modification and other nuclear components were employed. This information helped to further identify compartments in SMLM images, something which was not possible with EM previously [Haggis, 1992]. In this section, different labelling strategies are used in order to understand how the dynamic architecture of chromatin relates to function. Importantly, I show that the periphery of chromatin domains (see Section 3.2.3 for a thorough description of these domains) is associated with active transcription and related enhanced replication activity.

Figure 3.26: (A) DNA synthesis occurring at the periphery of chromatin domains in a monkey kidney fibroblast cell. Purple channel shows chromatin and green regions of newly synthesized DNA. White represents the regions overlapping. (A1) zoomed-in section corresponding to yellow box in (A). The vast majority of EdU signals anti-colocalize with chromatin and is observed at the periphery of chromatin domains (B). Scale bar in A is 1000 nm while in A1 is 500 nm.
3.4.1 Periphery of chromatin domains is associated with high DNA synthesis

Early replication is associated to regions of high transcription [Boulos et al., 2015]. To further describe chromatin domains, I decided to test where replication sites localise in the nucleus. If the outer part of chromatin domains is the place of more active transcription, then replication sites should also localise at the periphery of the domains. To investigate this hypothesis, sites of DNA replication were targeted by incorporating EdU, a DNA-basepair analogue (Figure 3.26). Alexa 647 was conjugated with Cu(I)-induced ‘click chemistry’. Intensity of pixels coming from DNA or EdU signals were recorded on an homogeneous section of the preparation. It is observed that in newly synthesized DNA sites, the signal locates at the periphery of the chromatin domains (chromatin domain 1 or sub-chromosomal domains, of about 1 µm, in the classification presented in Figure 3.16), confirming that this region of the nucleus is the site of new synthesised DNA and active transcription, while the center of chromatin domains is a place of repressed transcription, due to condensation of chromatin.

Figure 3.27: OND induces compaction of chromatin to mechanistically reduce transcription (Figure and caption modified from [Kirmes et al., 2015]). HL-1 cells were subjected to both anti-H3K14 immunostaining and counter-staining with Vybrant DyeCycle Violet. Signals were analysed using a SMLM set up. a-b: untreated cells; d-e: cells after one hour of OND stress. b-e: magnifications of white boxes in a and d, respectively. c-f: wide-field images corresponding to b and e, respectively. Regions deprived of chromatin are highlighted with an asterisk and atolls are shown with a white arrow.
3.4.2 Stress-dependent transcription at the periphery of chromatin domains

As previously discussed chromatin can protect itself via contraction (Section 3.3.4). HL-1 cells were transiently exposed to OND and stained for both DNA and H3K14ac, a histone modification known to be associated to active promoter state [Karmodiya et al., 2012]. Cells were fixed, immunostained with AlexaFluor647 conjugated anti-H3K14ac antibody and counter-stained with Vybrant DyeCycle Violet [Zurek-Biesiada et al., 2015]. The dynamics of histone modification H3K14ac was monitored during stress. Result shows that this mark experiences a great regression (Figure 3.27).

Resting state of the nucleus is associated with a classical diffuse pattern of chromatin, with denser regions observable close to the nuclear periphery (Figure 3.27). The threading network is complex and is interspaced by small inter-nuclear compartments. Staining for an active mark H3K14ac shows punctuate distribution throughout the nucleus (Figure 3.27). Foci of H3K14ac are found to be present at the edge of chromatin regions (Figure 3.27b) and in very few places inside of the mass, a result in agreement with theory on nuclear compartmentalization, which identifies inter-chromatin regions as places of transcription and transport of messenger RNAs [Cremer et al., 2015]. Wide-field images are not sufficient to show the tight relationship between chromatin and histone modifications (Figure 3.27c). As H3K14ac is related to active promoters, it is hypothesized that the cells imaged here are subjected to a high reduction of transcription. This clearly advocates for a physical mechanism of self-protection of chromatin by contraction, which leads to the shut-down of transcription in order to preserve the physical integrity of the DNA.

3.4.3 Histone modifications allow to further dissect chromatin into active and inactive domains

In order to gain insight into the epigenetic landscape of the interphase nucleus, and study how its structure may be regulated by histone modifications, several histone modifications were stained (Figure 3.28). A fluorophore density per 100 nm² of 0.0125 for H3K9me3; 0.0119 for H3K27me3 and 0.0089 for H3K14ac was found (Figure 3.28). Globally, this identifies centromeric mark (H3K9me3) as a mark of high density, active chromatin mark (H3K14ac) as the least dense, and the repressive chromatin mark (H3K27me3) as having the best balance between strength of signal and overall repartition. Comparison between H3K14ac and H3K27me3 marks reveals that the former has a distribution shifted to the left (Figure 3.28, bottom left image). This shows that the H3K27me3 clusters are broader than the H3K14ac and so are less dispersed. Overall, these findings confirm the highest density of chromatin associated to repressive histone marks.
3.4.4 SMLM identifies potential sites of transcription machineries in the mammalian nucleus

Transcription factories are self-organising discrete sites where polymerases and other transcription factors are concentrated [Cook, 2010]. Similarly to Section 3.2.1, transcription machineries are identified using SMLM. As shown in Figure 3.29, while nucleoli are visible with a low number of signals, certain central structures start to appear when enough number of signals are accumulated (white arrows). The organisation of the structures is thought to be an active region of transcription because their round shape is analogous to nucleoli and they are likely to be a collection center of chromatin coming from several chromosomes, similar to the territories/inter-territories model presented in Section 3.2.2.

3.5 Summary and discussion

SMLM was successfully applied to conventional DNA dyes (Hoechst and DAPI) to describe different levels of chromatin organisation, from nucleosome to chromosome territories. High labelling density (more than $10^7$ signals per 500-600 nm optical section) of these minor groove binding DNA dyes helped to infer structural features and density variations in chromatin organisation at the nanoscale. It was found that chromatin is clustered at large scales but distributed randomly at the finest scale. At a lower order of organisation, statistical analysis of chromatin distribution revealed distinct differences from a random density distribution. At an intermediate order, 100-400 nm domains emerged as the functional building blocks of chromatin architecture, with differential condensation states. The outer side of these domains being less condensed as compared to the more condensed inner domains.
Furthermore, some examples of dynamic processes that chromatin undergoes were shown, with special emphasis on stress. The compaction of chromatin observed upon stress conditions indicates that it might be experiencing a phase separation process. At its core ‘phase separation’ means ‘like dissolves like and unlike separates/phases out’. For example, GC-rich might separate out from AT-rich regions. From a polymer physics perspective, monomers of the same species phase separate from monomers of a different species. At a chemical level, a polymer composed of hydrophilic and hydrophobic components may arrange itself differentially in order to maximise or minimise interactions with the surroundings medium. In OND conditions, one observes large and dense ring/rod like structures. It is known that most AT-rich region are heterochromatic due to the presence of 2 hydrogen bonds (less active) and that GC-rich regions are euchromatic due to the presence of 3 hydrogen bonds (more active). Since Hoechst and DAPI have high specificity for AT-rich sequences, the GC-rich block of the chromosomes phase separates to form non overlapping micelles [Ostashevsky, 1998]. Staining of DNA using different oligonucleotide probes specific for simple repetitive DNA sequences might provide further clues.

Finally, using multicolour staining, the structure-to-function relationship of chromatin was studied with focus on metrics that could hint at chromatin activity. The active chromatin regions were on exterior and in decondensed regions (Section 3.4.1 and 3.4.2) while the inactive regions in the interior of the domain (Section 3.4.3), with an increase of chromatin density. EdU and several histone modifications helped in identifying novel chromatin compartments. Histone modifications associated with active chromatin were always on the periphery of a chromatin while histone modification associated with repressed chromatin were more toward the interior of a chromatin domain. Also, several new orders of chromatin domains were reported in this chapter.

Overall, it is hoped that the data presented in this chapter will help acknowledging that chromatin folds at various length scales and that domains in the range 100-400 nm constitute the fundamental functional elements of nucleus organisation. Focus on understanding the biology of these domains will be of great help to understand the mechanisms behind chromatin folding and organisation.
Only a structure built on profound symmetry and periodicity can possibly fit 3 meters of DNA inside 10 micron wide nucleus.

4 Periodic and Symmetric Organisation of Meiotic Chromosomes

In this chapter, single molecule localization microscopy (SMLM) is combined with analytical tools to describe the chromatin organisation of the pachytene chromosomes. DNA is found to be non-randomly distributed along the length of chromosome proteinaceous backbone, the synaptonemal complex (SC), in condensed clusters. Furthermore, chromatin is organized in spatially distinct functional clusters associated to specific epigenetic marks (Figure 4.1). For functional characterization, various post-translational histone modifications were selected based on information from genomic data and the three following chromatin compartments were identified in the pachytene chromosome:

1. **Radial chromatin** identified by trimethylation of histone H3 at lysine 4 (H3K4me3) — indicative of actively transcribed chromatin.

2. **Polar chromatin** identified by trimethylation of histone H3 at lysine 9 (H3K9me3) — indicative of centromeric chromatin.

3. **Tangential chromatin** identified by trimethylation of histone H3 at lysine 27 (H3K27me3) — indicative of repressed chromatin. This compartment is remarkably associated to the backbone of the chromosome, showing a putative implication in the regulation of recombination.

Periodic clusters of H3K27me3 are found at 500 nm intervals along the SC, while H3K9me3 mark is associated with a large and dense cluster at one of the ends of SC. H3K4me3 is arranged in a radial hair-like loop pattern emerging laterally from the SC, observed for the first time in mammals, especially in context of post-translational histone modifications. For the first time, SMLM is combined with immunostainings and DNA stains to map the global epigenetic landscape of pachytene chromosomes. In this study, single molecule localisation microscopy protocol was optimised to combine direct staining of SC proteins either with DNA molecules or modified histones. This work can be used as a rational to explore the chromatin organization of any cell nucleus, giving both an overview of DNA molecules and refine the picture with meaningful functional annotations.

Finally, taking into account the arrangement and composition of chromatin, as well as the region-specific distribution of post-
translational histone modifications, a model of the chromatin architecture along the SC is discussed in this chapter. It is tempting to speculate on a possible super-coiling of meiotic chromosomes, not seen in mitosis or interphase, possibly needed to mechanically simulate chromosome pairing and recombination.

4.1 Introduction

Meiosis is an essential event in the life cycle of sexual organisms, as it creates new genetic combinations at each generation. The two consecutive major events that participate in generating genetic diversity during meiosis are chromosome segregation and genetic recombination. Chromosome segregation is the sorting of each chromosome of a pair into a different two daughter cell, an event happening in the two cell divisions of meiosis, which results in a major shuffling of alleles. Recombination also participates to diversity by exchanging sequences of 1-2kb of two homologous chromosomes during an event called crossing-over. This event is more likely to generate innovation as the portion involved are smaller and can potentially edit gene scaffolds, regulatory intergenic regions, or non-coding genes. The places of recombination are not random and are heavily constrained by DNA sequence (mainly GC content, see [Clément, 2012]) and chromosome structure.

Figure 4.2 (inspired by [Lichten, 2001, Baudat et al., 2013] and other studies mentioned below) details the mammalian meiotic process, preceded by DNA duplication, as described previously in mouse. Particularity of mouse chromosomes compared to human is the location of the centromere at one telomere, resulting in one-arm chromosomes exclusively. During interphase, chromosomes are complex objects consisting of one chromatid and the telomeric centromere (Figure 4.2)
, Step 1). After DNA replication, the chromosomes display two chromatids, associated at certain locations via cohesin protein. During early meiosis, cohesin spots dramatically increase, leading chromosomes to form typical chain of loops, called axial element (Figure 4.2, Step 2, inset). The chromosomes are unpaired and elongated. Moreover, chromosomes start to attach to the nuclear envelopes via their two extremities (Figure 4.2, Step 3). During zygotene stage, two-chromatids chromosomes start to pair, most likely using extruding DNA generated by double strand breaks (DSB) as probes to find the partner (see pairing in Figure 4.2, Step 4 represented with light green). The search for the partner chromosome is essentially a random process. Chromosomes move along the lamina until they find another chromosome; if the two chromosomes match, they will start pairing (see dynamics in [Sato et al., 2009]). Pairing shows formation of a giant protein scaffold, the SC, which holds the two homologous chromosomes at a distance of between 150-200 nm from each other, which is a prerequisite for recombination to happen consistently in a 3D space. The pairing usually starts close to the centromere, as the DSB are more likely in this region [Pratto et al., 2014]. Pachytene stage shows the most constrained DNA, with complete pairing all along the chromosome (Figure 4.2, Step 5). Chromosome pairs at this time are all attached around the same spot of the nuclear envelope that is called the bouquet [Berríos et al., 2014, Gall and Pardue, 1969, Sato et al., 2009]. During pachytene, recombination happens via the
resolution of chromatid DSB from the homologous chromosome and creating a chimera chromosome with extensive portion of both original chromosomes (Figure 4.2, Step 6, black arrows). Diplotene is a relaxation of chromatin, with unzipping starting from centromeres, leaving progressively the pair attached only at the location of the recombination site (Figure 4.2, Step 7). Meiosis I ends with the migration of chromosomes to the two asters along microtubules, an event that entangles the recombined chromosomes and leads to migration of the two chromosomes of each pair to different sides of the cell (Figure 4.2, Step 8). Meiosis I generates two cells with 2n chromosomes (Figure 4.2, Step 9), while meiosis II completes gametogenesis by generating overall four gametic cells with n chromosomes (Figure 4.2, Step 10).

In this description of meiosis, synapsis is an essential event for recombination of the homologous chromosomes. Though advances of genomics have proven that recombination can be studied by DNA sequence analysis, getting the detailed structure of the pachytene chromosome is essential to understand the mechanistic steps that have to take place in order to make recombination happen. Here, I propose a detailed description of meiotic chromosomes at pachytene stage. I start by exploring the organization of SYnaptonemal Complex Proteins (SYCPs), which form the SC, the backbone of pachytene chromosome, and then I describe the spatial distribution of chromatin, including some of its functional compartments associated to certain histone modifications, in relation to SYCP.

4.2 Organisation of the synaptonemal complex (SC)

4.2.1 Superresolution imaging of the SC substructures

The synaptonemal complex (SC) is an important structural component of meiosis that is used to localise pachytene chromosomes in routine experiments [Baudat et al., 2013]. Two important components of SC, namely SYCP3 (the lateral element, Figure 4.3A) and SYCP1 (the central element, Figure 4.3B) were first characterised in order to study the architecture of meiotic chromosomes.

Chromosome spreads from oocytes were obtained from collaborators (for details see [Prakash et al., 2015]). SYCP3 and SYCP1 C-terminus were labelled on separate preparations using antibodies coupled with Alexa Fluor 555. On average, 2500 photons per cycle were detected for Alexa Fluor 555 and localization maps of the two proteins were generated by integrating roughly 20,000 observations. Each frame captured photons acquired during 100 ms of integration time. Individual localisations were blurred using the mean distance to the 20 nearest molecules (method described in detail in [Kaufmann et al., 2012]). This particular blurring method was chosen for clarity of the visuals and comparison to other visualisation methods is done in Chapter 2, Section 2.7.3.

Main images of SC proteins are shown in Figure 4.3. The colours
show a density map, with denser regions close to yellow and regions with low density close to red. Qualitatively, one can see the double-strand nature of both proteins, which is not apparent in wide-field mode of the same image (Figure 4.3, inset A1 and B1). A dual color image showing relative organisation of SYCP1 and SYCP3 is shown in Figure B.1 and confirms the double-stranded patterns (Figure 4.4).

4.2.2 Quantification of SC substructures

Quantifications confirmed the general structural features of the synaptonemal complex. Profiles of pixel density show the improvement of the superresolution setup compared to a wide-field image of the same object, the double-stranded SYCP3 and SYCP1 scaffold (Figure 4.4A): clearly, the two strands cannot be distinguished with conventional microscopy (for confocal microscopy images, see [Baudat et al., 2013]). Distribution of SYCP1 and SYCP3 signals along the SC shows a clear separation of the two lateral elements, and a more central localisation for SYCP1 (Figure 4.4B). By computing the distance from the maxima of each individual strand of SYCP3, I estimated the distance between the two strands of SYCP3 to be around 181 nm and the width of an
Figure 4.4: Quantification of SC sub-structures (figure and caption modified from [Prakash et al., 2015]): (A) Distribution of SYCP3 along the transversal plane of the SC (i.e. perpendicular to main axis) in SMLM (red) versus wide-field configuration (blue). (B) Distribution of C-terminal end of SYCP1 and SYCP3 along the transversal plane (red and blue plots respectively). The distance between the positions with highest molecule occupancy is 180.7 nm for SYCP3 and 87.9 nm for the C-terminus of SYCP1. (C) Average distance to the 20 nearest neighbors was used to calculate the extension of blurring of the individual molecules. For SYCP3, the distance used was 14.31 nm +/- 5.43 nm and 18.81 +/- 7.40 nm for SYCP1. (D) A schematic diagram illustrating the thickness and the interstrand distance of SYCP3 and SYCP1.

individual strand to be 60 nm (Figure 4.4B). Moreover, analysis of SYCP3 patterns at the ends of the chromosomes shows that the SC is narrower at the telocentric end compared to the other end (Figure 4.11, Figure B.8). I used the same approach for SYCP1, whose distance between the strands was found to be 88 nm and the width of the strands themselves 47 nm.

The inter-distance between strands was calculated by taking the position with the maxima of molecule distribution on each strand. Individual fluorophores were detected with a precision of 11 nm for SYCP3 and 16 nm for SYCP1. Moreover, a Fourier Ring Correlation (FRC) resolution of 43 nm and 56 nm was found for SYCP3 and SYCP1 C-terminus, respectively. For SYCP3, the nearest neighbour distance was 14 +/- 5 nm and for SYCP1, this distance was 19 +/- 7 nm (Figure 4.4C). These distances were used as the standard deviation of the Gaussian distribution applied to the individual molecule position for blurring, a slight modification of Gaussian blurring (see Figure 2.17 of methods chapter for comparison of visualisation methods using the SC data as example).

Furthermore, in a two colour experiment both SYCP3 and SYCP1 C-terminus were stained. Immunostainings were performed using either Alexa 555 coupled to an antibody against SYCP3 or Alexa 488 coupled to an antibody against the C-terminal of SYCP1 (Figure B.1). The merged image clearly shows that SYCP1 is located inside of SYCP3 (Figure B.1C), of similar double-strand nature (insets). I roughly summarize the findings in a visual that shows SYCP3 proteins on the outside of the SC and SYCP1 on the inside (Figure B.1D). These results are in line with observations from other studies [Gustafsson et al., 2008, Syrjänen et al., 2014, Schücker et al., 2015]. A recent SMLM study reported the width of individual strands of SYCP3 to
be around 56 nm while the distance between strands to be around 165 nm [Schücker et al., 2015]. The width of SYCP1 C-terminus was reported to be 45 nm with overall width of central region (composed of transverse filaments (TF) and the central element (CE)) to be around 148 nm, similar to the values found in my analysis (Figure B.1D).

4.2.3 A model for organisation of SC

In this section, I suggest a model for the SC incorporating further information from [Syrjänen et al., 2014]. As the antibodies are directed toward the C-terminal of SYCP1 proteins, information obtained from localization of these molecules confirms the inner position of the SYCP1 C-terminal domain (Figure 4.5), with N-terminal sides of SYCP3 molecules directed toward the center of the SC. SYCP1 dimers could interact to form a ladder-like structure, while SYCP3 molecules link neighbour DNA loops, as demonstrated in the model of [Syrjänen et al., 2014]. The figure shows the two chromosomes modelled with two sister chromatids shown in light and dark blue. SYCP3 triads can act to bring distant locations on a chromosome together by self assembly [Syrjänen et al., 2014]. This would eventually lead to the shortening of the chromosome axis longitudinally while lengthening or looping out of chromatin radially. The chromatids for both homologs are separated by a distance of roughly 150-200 nm i.e. the distance between the two strands of SYCP3 (green box). The inter-loop DNA is figured with a black line. This region is likely to be the site of repetitive DNA sequence and may be enriched with histone marks that condense chromatin like H3K27me3 [Pauler et al., 2009]. SYCP1 is depicted as a blue box. Similarly to SYCP3, SYCP1 might play an important role in the final assembly of the pachytene chromosomes.

Figure 4.5: A model for the synaptonemal complex explaining the results presented in this chapter with evidences and models from [Syrjänen et al., 2014] is shown. The view shows the two chromosomes modeled with two sister chromatids in light and dark blue; the inter-loop DNA is figured with a black line. SYCP1 is depicted as a blue box and SYCP3 with a green box; both show their N and C terminal domains.
4.3 Periodic organisation of pachytene chromosomes

The pachytene chromosomes have a very constrained pattern in 3D space [Schücker et al., 2015], which is highly identifiable on mammalian chromosome spreads. This is due to the fact that recombination process requires two chromosomes of a pair to be kept apart 100 nm of each other in order exchange of chromatids to happen [Petronczki et al., 2003]. As a result, both the highest order of chromatin complexity and density is attained at pachytene stage of meiosis, the moment when recombination takes place. Pachytene chromosomes are visible in EM (for instance in [Moses et al., 1977]) and SEM (Figure B.3) preparations of mouse samples and display a typical caterpillar shape. Though EM and SEM are among the most powerful techniques to probe nanoscale structures, they do not stain efficiently and specifically particular proteins. High resolution light microscopy based measurements of pachytene chromosome are therefore necessary and occupy the next section of the present chapter.

Figure 4.6: Super resolution microscopy reveals higher order clusters of chromatin patterns along the pachytene chromosome (figure and caption modified from [Prakash et al., 2015]): (A) Samples immunostained using Alexa 555 conjugated anti-SYCP3 and counter-stained with Vybrant Violet, a photocovertible DNA dye (see Chapter 2 for more details). Inset A1 shows the wide-field image for comparison. B. DNA density map of the pachytene chromosome. Scale bar same as in (A). (C) Magnified section corresponding to yellow box in B. Scale bar: 250 nm. (D) Distributions of SYCP3 and DNA molecules around central axis of SYCP3. (E) Autocorrelation plot of chromatin patterns along the SC axis based on chromosome section displayed in panel C. Periodicity is found to be 550-700 nm tangentially and the cluster diameter is estimated to be in the range 170-225 nm. Blue lines show the 95 percent confidence bounds (+/- 0.08) of the autocorrelation function.
4.3.1 Superresolution imaging of pachytene chromosomes reveals periodic clusters of chromatin

Experimental procedure was close to the one described for the characterization of SC proteins. The protocol for imaging DNA has been described in [Zurek-Biesiada et al., 2015]. Briefly, samples were immunostained using Alexa 555 conjugated anti-SYCP3 and DNA with Vybrant DyeCyble Violet (Life Technologies), a dye with similar properties as Hoechst and DAPI [Szczurek et al., 2014, Zurek-Biesiada et al., 2015]. Blinking efficiency was stimulated using our custom switching buffer consisting of glycerol with 10% (wt/vol) imaging buffer (stock comprising 0.25 mg/mL glucose oxidase, 0.02 mg/mL catalase, 0.05 g/mL glucose in PBS). For SYCP3, localisation maps were generated integrating roughly 20,000 observations and about 100,000 observations for DNA. A two-color image was generated after application of nearest-neighbour blurring to the raw single molecule data (Figure 4.6A). Density map of the DNA channel reveals periodic clusters of chromatin, characterized by a central high density region (Figure 4.6B). Elongated extensions of the DNA are localised laterally, possibly involved in recombination [Gall, 2012, Callan, 2012]. General shape of chromatin is reproducible (Figure B.6) and is validated by SEM experiments (see Figure B.3).

4.3.2 Quantification of periodic chromatin clusters

Quantification helped to further describe the density distribution and the periodicity of the chromatin clusters. Pixel density classification (Figure B.4) reveals that the clusters have two major regions: a central region which bears the highest density (3.5 signals/nm$^2$) and an outer region of lower density (1.5 signals/nm$^2$ see Figure B.4, purple and green regions, respectively).

In order to characterize the periodicity of the clusters and distinguish them from background, I first applied auto-correlation, an algorithm to find similarity of signals (Figure 4.6C). Periodicity lies in the range 550-700 nm tangentially along the SC axis (Figure 4.6E, Figure B.6A3). The average diameter of the clusters is found to be in range of 170-225 nm (Figure B.9). Later, a new algorithm was developed to further characterize the clusters (Figure 4.7). First, a binary mask was generated based on distance to 20 nearest neighbour and signals within this mask were taken for further analysis. A randomly generated image with the same number of localisations is presented for comparison (Figure B.2B). The random distribution served as a control to be compared to the SMLM data. Nearest neighbour distances were used to characterise the local condensation in SMLM and randomly simulated data (Figure B.2C). In the experimental data, the mean distance to 500 nearest neighbours was around 86 nm while in the simulated random data, it was 110 nm (see [Prakash et al., 2015], supplementary data). This non-random distribution of DNA was indicative of the fact that the clustering observed in SMLM images of DNA is a consequence of structural packing of DNA.
4.4 Functional organisation of pachytene chromosomes

4.4.1 Rational

The power of high resolution light microscopy over electron microscopy is to specifically label particular structures on a given sample (for comparison on same sample refer to [Lippincott-Schwartz and Patterson, 2009], Figure 5). With SMLM, one can not only observe nano-scale structures but is also able to describe them in molecular terms. For example, individual functional compartments of chromatin whether active, inactive, or repressed can be described and categorised independently. Each of these categories experiences a different epigenetic regulation and is enriched with various combinations of epigenetic modifications.

I was curious to investigate the contribution of epigenetics, more specifically histones post-translational modifications (PTM) associated to the structure of pachytene clusters observed in SMLM experiments (Figure 4.7). In interphase, PTM are known to regulate gene expression by modifying DNA accessibility (see example on Figure 4.8 and Chapter 1, Section 1.5). In meiosis, apart from de novo H3K4me3, which is thought to be a major regulator of meiotic recombination by promoting double strand breaks [Mihola et al., 2009, Sommermeyer et al., 2013], not much is known about the epigenetic regulation of chromatin. As a result, I tried to define a rational to select meaningful histone modifications in order to investigate and better characterise...
the chromatin architecture of the pachytene chromosomes.

I decided to take a naive approach to systematically select relevant histone marks for the study. Assuming that chromatin states such as gene activation or gene repression are often defined by combinations of post-translational histone modifications (also known as the 'histone code'), it is likely that positions of several histone marks, having similar function, may co-localise throughout the genome. Finding these clusters of marks would tell what is the minimal number of marks to study in order to get a rough picture of chromatin functionality. Therefore, I studied the co-occurrences of histone marks and derived meaningful functional clusters. As the data is sparse for mouse oocytes meiotic chromosome, I used data from classical studies of [Barski et al., 2007, Wang et al., 2008] in human immune cells to benchmark histone mark associations. This method is described in detail in [Prakash, 2012]. The Boolean model helped to select genomic positions which have strong ChIP-seq signals to study the association of histone marks at these sites. This resulted in a table where associations between histone modifications are marked with a coloring scheme (Figure 4.9).

Figure 4.9: Co-occurrences and clustering of histone post-translational modifications in CD4 T cells: Blue circles represent positive correlations between histone modifications while red circles represent negative correlations. Size and color depth indicate the measure of the correlations. Histone modifications with no significant correlation are left blank. The dark blue rectangles along the diagonal of the correlation matrix represent clusters of histone modifications and are based on the results of hierarchical clustering. The cluster on the top left corner shows H3K4me3 correlating with several acetylation marks. The bottom right cluster shows positive correlation of H3K27me3 with H3K9me1, H3K9me2 and H3K27me2. The fourth cluster along the diagonal shows strong correlation between H3K9me3, H4K20me3 and H3K79me3.

4.4.2 Clustering method sorts chromatin into functional epigenetic compartments

Hierarchical clustering of 39 different histone modifications led to identification of five functional clusters. The first cluster was found to be associated with gene activation, comprising acetylation marks and H3K4me3, a well-known mark associated to initiation of double
strand breaks during recombination (Figure 4.9, top-left cluster displayed as a blue box); a second cluster was found to be associated to H3K9me3, a mark involved in constitutive heterochromatin of centromeres, structures which have a strong importance in synaptonemal complex initiation (Figure 4.9, fourth cluster from the left); lastly, I identified a cluster of repressive marks (Figure 4.9, fifth cluster from the left), from which H3K27me3 has been previously identified as anti-correlated to meiotic DSBs [Buard et al., 2009]. Genomic data confirm the anti-correlation of H3K9me3 and H3K27me3 clusters during germ cell differentiation [Liu et al., 2014]. On the other hand, H3K27me3 and H3K4me3 are shown by genomics to anti-correlate genome-wide [Hammoud et al., 2014]. As a result of this analysis, I decided to stain the following 3 representative marks to further characterize chromatin organisation: H3K4me3, H3K9me3 and H3K27me3. The function and genomic regions where these marks are known to be enriched is summarised in Figure 4.10.

4.4.3 Centromeric histone mark (H3K9me3) labels one end of the SC

H3K9me3 is associated to centromeres and to the initiation of double-strand breaks at the early stages of SC formation [Hernández-Hernández et al., 2012, Mikkelsen et al., 2007]. In mouse chromosomes, centromeres localise at one of the telomeres (often referred to as telocentres), resulting in chromosomes having only one arm. Chromatin staining of the pachytene chromosome shows a huge cluster of DNA at one end of chromosomes (Figure 4.6B). I used SMLM to probe if these dense chromatin regions were enriched with the centromeric mark H3K9me3. Images obtain show that one of the ends of SYCP3 is highly enriched with H3K9me3 (Figure 4.11), compared to the other end of SYCP3. Moreover, the centromeric end is remarkably distinguishable by a narrower SYCP3 structure compared to the other end (Figure 4.11B). This observation is further presented in replicates (Figure B.7 and Figure B.8A-B). Furthermore, at the telocentric end of the chromosome (Figure 4.11C), H3K9me3 co-localizes with a high chromatin density. The top cluster on chromatin image (Figure 4.6B) has a similar average axial spread of 1-1.5 µm as in case of H3K9me3 (Figure 4.11A) image.

4.4.4 Repressive histone mark (H3K27me3) shows characteristic periodic clusters along the SC

H3K27me3 is associated to repeat regions of the genome and some of them can be deleterious for the proper transmission of information to the next generation [Pauler et al., 2009]. Next, I wondered if H3K27me3 might possibly contribute to the periodic clusters seen in Figure 4.6C. In agreement with previous findings [Hernández-Hernández et al., 2010], H3K27me3 post-translational modification was found to be localised close to the SC, directly at the outside of the regions occupied by SYCP3 proteins (Figure 4.12). The important overlap between H3K27me3 and SYCP3 was also visible in wide-field.
Figure 4.11: H3K9me3 displays a centromeric position along the SC (figure and caption modified from [Prakash et al., 2015]): Two-color SMLM image (A) immunostained with anti-SYCP3 (Alexa 555) and anti-trimethylated histone H3K9 (Alexa 488). Inset (A1) shows the underlying wide-field image. Large dense clusters of repressive centromere mark H3K9me3 can be seen at the presumptive telocentric end of the pachytene chromosomes. High H3K9me3 density at the telocentric ends of SYCP3 is concomitant with high chromatin density at the top axial end in (Fig. 4.6B). (B) The strands of SYCP3 where H3K9me3 co-localises (presumptive telocentric end) are found to be closer (∼135 nm) than at the presumptive telocentric end (∼180 nm). (C) H3K9me3 distribution hints for spiralization of DNA at the centromeric end of the SC. Point of representation of single molecules of SYCP3 and H3K9me3 is shown in (C). (D) compares different visualization strategies. Spiralization of DNA was observed at one of the extremities of synapsed chromosomes (D1-D3), probably working as an anchor for the two chromosomes to start synapsis. This spiralization exemplifies the relevance of blurring methods for visualisation, nevertheless, feature is visible in all three visualisation methods.

(Figure 4.12A). However, the SMLM image revealed an unexpected pattern. H3K27me3, instead of spanning the entire length of the chromosome, displayed large periodic clusters, disposed in pairs (Figure 4.12B), found every 450-650 nm along the SC according to auto-correlation analysis (Figure 4.12D). Size of clusters was found in the 90-130 nm range (Figure B.9) and the average lateral distance from the strands of SYCP3 in the 40-50 nm range (Figure 4.12C), though there is an overlap with SYCP3 in several instances, possibly due to twisting of SYCP3. The proximity of H3K27me3 and SYCP3 on the SMLM cliches explains why the two features seem to co-localise with confocal images (∼200 nm resolution of the imaging system).

The patterns shown on Figure 4.12 were reproducible on all chromosomes (see [Prakash et al., 2015] supplementary data). The periodicity of H3K27me3 and chromatin clusters found in Figure 4.6C seem to match and I hypothesize that the larger chromatin clusters with lateral extensions have strong enrichment for H3K27me3 mark at their base, an information that I incorporate in a model of the pachytene
chromosome (see Section 4.6.1).

The pattern of the clusters itself indicates their high functional nature. Symmetry and perfect pairing means that deposition of this repressive mark is dependent on the genomic content of chromosomal regions and is reproducible between chromosomes. What is the function of these regions? The present analysis does not provide any answer, but one speculates that these periodic clusters might correspond to the silent repeated regions of genomes, such as long interspersed elements (LINE) or long-terminal repeat (LTR), as H3K27me3 is often found to be associated to this kind of element [Pauler et al., 2009]. This repressive feature is key to prevent the mobility of jumping elements during meiosis, whose movements can have consequence for the progeny.

4.4.5 Histone mark (H3K4me3) associated with active transcription emanates radially from the axis of the SC

Finally, I present here the distribution of H3K4me3, a mark known to be highly involved in generation of double strand breaks, along the pachytene chromosome. Instead of localising at the axis, H3K4me3 showed localisation in the lateral to the central axis of SYCP3 (Figure 4.13), possibly corresponding to the extensions identified with DNA staining (Figure 4.6). H3K4me3 extensions were found to be 500 nm wide which were in accordance with chromatin protrusions (Figure 4.6D). Similarly to H3K27me3, H3K4me3 forms clusters of 50 nm diameter (Figure B.9). The average spread of the radial emanations of H3K4me3 ranged from 300 to 500 nm, with the overall distribution of H3K4me3 qualitatively similar to the chromatin distribution (Figure 4.6D, Figure 4.13A1). By applying autocorrelation to the tangential distances from the central axis of SYCP3 (Figure 4.13A3), I estimated the average spread (approx. 500 nm) of the protrusions to be larger than their spacing (approx. 200 nm).
4.5 Structure and dynamics of meiotic chromosomes

4.5.1 Lampbrush-like structures in mammalian meiotic chromosomes

Lampbrush chromosomes (LBC) are giant chromosomes found in oocytes of diverse organisms, both vertebrate and invertebrate. They are characterized by paired loops of transcriptionally active chromatin that extend laterally from an axis of inactive chromatin. Among vertebrates, they have been extensively studied in amphibians, reptiles, fish, and birds, but have not been convincingly demonstrated in mammals [Gall, 2012, Callan, 2012].

Though known to be necessary for the pachytene chromosome to function normally, presence of loops in mammals has not been so far optically demonstrated ([Heng et al., 1996], does not show convincing images). Data in this thesis are a good step in this direction, as some of the images show H3K4me3-marked processes forming circular patterns (Figure 4.14) resembling SEM (Figure B.3) and EM data of pachytene chromosomes observed in amphibians [Rattner et al., 1980]. Some putative looping structures are found on our chromatin SMLM pictures (Figure 4.6) but it is possible that the pattern is the result of contact of two adjacent extensions of the chromatids. Nevertheless, the size of lateral chromatin extensions (500 nm) (Figure 4.6D) is similar to the size of H3K4me3 extensions (Figure 4.14D). H3K4me3 is better at spotting possible loops because the labelling density is lower than DNA (DNA staining: 5,000 single-molecule signals per square micrometer [Szczurek et al., 2014], histone staining: 100 single-
molecule signals per square micrometer [Bohn et al., 2010]), which creates more opportunity to distinguish thin or subtle structures. This point is another example of the importance of staining chromatin with both DNA dyes and histone modifications.

4.5.2 A model for SC spiralisation during the zygotene/pachytene transition

The above data provide important information regarding the organisation of pachytene chromosomes. They also provide some hints regarding the dynamics of pachytene chromosomes during meiosis. Though presently there is no time series data of meiosis steps, it is worth mentioning that the images hint at a spiralization of chromosomes in pachytene stage, possibly for functional reasons. It was shown that H3K4me3 displays a helical wrapping around the SC (Figure 4.11). DNA staining itself also shows a trend to form spirals, either only at the extremity (Figure 4.6) or all along the body of the chromosome (Figure B.6). One may object that the situation studied is not native, as the chromosomes have been processed through a rather harsh protocol. Nonetheless, evidences show that the helical structure of single chromosomes is preserved in pachytene chromosomes showing bouquet-like patterns close to native state (Figure B.7, two pair of chromosomes on left).

I further show high-order patterns of H3K4me3 on certain chromosomes, showing clear helical patterns. As H3K4me3 is probably spanning most of the space occupied by chromatin, one can approximate the positions of the H3K4me3 for overall spatial occupancy of
chromatin. To demonstrate the spiralization, I developed an algorithm to identify alternate patterns of H3K4me3 clusters on each side of the SC (Figure 4.15B). Most of the neighbour clusters were found to be separated along the axis of SC, a pattern even more evident on the first image with the SYCP3 staining. Same type of alternative configuration was found using data from H3K27me3 imaging (Figure B.5). Such chromosomes may role around each other in the fashion of mating snakes (see snake model, Figure 4.16). Pairing of the two chromosomes could start by a tight enrolment of chromatin at the centromere, H3K9me3-rich (the spiral pattern of H3K9me3 in Figure 4.11 ascertains this fact), to rapidly induce the wrapping of the rest of the chromosome. Recent data from 3D-SIM confirms a complete 3D twist of SYCP3 along the axis of the chromosome, as predicted by the snake model (David Fournier, personal communication, data not shown). Moreover, helical patterns are clearly identifiable in whole cell preparations of Xenopus oocytes from early studies on pachytene chromosomes [Gall and Pardue, 1969], probably working as an anchor for the two chromosomes to start synapsis.

It is speculated that the helical patterns have a structural or a mechanistic function. Spiralisation is probably essential for pairing to happen, by inducing a wrapping of the two chromosomes around each other once pairing has started. Spiralisation may also help recombination events to form, following the initiation of synapsis to impose certain structural constraints that help crossing-overs to form.

4.6 A model of spatial distribution of chromatin around the SC

Finally, I summarize the composition of high-order chromatin into lower-order histone modification clusters using distance profiles (Figure 4.17, left). One can observe that while chromatin has the broadest
extension, H3K9me3 follows the same shape as the chromatin profile and is normally distributed along the central axis of SC, hinting that the telocentric region is mostly covered by the H3K9me3 cluster, while other regions that extended laterally are deprived of this centromeric mark. Differently, H3K27me3 cluster follows the shape of the synaptonemal complex, hinting for its tangential localization. H3K4me3 profile is asymmetrically distributed and comparison with chromatin profiles shows a level of complexity that chromatin alone cannot capture, as possibly most of the DNA is not active. Most of the profiles are slightly lopsided, that I speculate to be mostly due to chromosome not being in the sample plane and the angle creating the asymmetry.

4.6.1 A ’cluster-on-a-string’ model for spatial distribution of pachytene chromosomes

The different clusters observed (H3K4me3, H3K27me3 and H3K9me3) are obviously of much higher order than basic bead-on-a-string structures of DNA and histone complexes. As a result, I hypothesize that the patterns observed in the pachytene chromosomes are rather a large chunk of those beads, possibly of a state close to chromatin fibres. I describe them as ‘clusters-on-a-string’, to point that they are likely bulky regions epigenetically regulated, surrounded by disorganized DNA fibres. These structures are probably to relate to chromatin domains found in interphase (see Section 3.2.3 and Figure 3.16). More has to be explored in order to see what is the structure of the clusters and the regions in between. For this, more informational staining will have to be performed, using either polymerases, splicing machinery or other enzymes.

Finally, I summarize our findings in a model of the pachytene chromosome, which displays roughly three epigenetic compartments, capturing most of the epigenetic information in chromatin according to the histone code table (Figure 4.17, right). While H3K4me3 is covering the entire chromatin landscape, including lateral extensions, synaptonemal complex region and telocentric end of the chromosome, H3K27me3 is confined to the SC, a fact confirmed by a trend on distribution plots in Figure 4.17, left. I speculate that the two marks anti-correlate in the SC. H3K4me3-rich spots being prone to recombination, following binding of PRDM9. H3K27me3-rich spots focused on repressing intermediate regions, either to silent undesirable elements such as repeated elements, which may strengthen its integrity by over-twisting.

4.7 Summary and Conclusion

Different variations of DNA and histone modifications staining, at single molecule resolution, have revealed two orders of chromatin in the meiotic chromosomes that were unknown before. The analysis shows that histone modifications can be useful not only to add
periodic and symmetric organisation of meiotic chromosomes

Figure 4.17: Symmetric and periodic organisation of pachytene chromosomes: The two strands of the synaptonemal complex are displayed in black. In purple, chromatin covers the entire surface and is thought to be ubiquitously marked by tangential mark H3K4me3, shown in blue. Tangential, symmetrical and periodic H3K27me3 clusters are displayed with yellow spots. Polar chromatin associated to H3K9me3 is shown as an orange spiral pattern.

functional information but also to study the chromatin organisation in more details. It also shows that the level of resolution of histone modification is highly useful to characterize very fine regions such as loops; H3K4me3 staining revealed loop-patterns not observable with the DNA staining while H3K9me3 hints toward spiralization of DNA at telocentric end, a pattern less visible on DNA images.

The above results confirm the predicted anti-correlation from the genomic data of the three histone modifications. H3K9me3 and H3K27me3 clusters anti-correlate, as shown by [Liu et al., 2014] using ChIP-seq data. Similarly to genomic data from ChIP-seq [Hammond et al., 2014], H3K27me3 and H3K4me3 are shown to anti-correlate genome-wide, with lateral H3K4me3 marks being devoid of H3K27me3 mark, while axial H3K4me3 clusters show possible partial overlap with H3K27me3 clusters. Additional co-immunostaining of pairs of histone modifications should further reveal dependency and correlation with other marks.

Spreading technique can question the reliability of the patterns observed and one can wonder if they would be observed in intact nuclei. Though this is unlikely for two reasons; one is that in virtue of thermodynamics, a passive system will only lose complexity with time. Spreading chromosomes can at worst destroy clusters, but unlikely create ones, and moreover these patterns are reproducible across several samples. Second reason is that close to native states are
sometimes observed (Fig B.7), with chromosomes bound by pairs via their centromeres, a pattern reminiscent from the native attachment of all chromosomes to the rRNA center [Gall and Pardue, 1969]. The helical structure of single chromosomes is preserved in these pairs (Fig B.7).

Study of the epigenetic regulation of the pachytene chromosome has left one with several important results. It was shown for the first time a high resolution map of pachytene chromosome using both a DNA dye and histone modifications, which when combined helped to have a comprehensible view of functional chromatin (Figure 4.17). This can easily be pursued in different contexts, especially the one of disease phenotype, to see the implication of epigenetics in disease.

Moreover, this is also the first study to show that mammalian chromosomes display lateral loops, similar to one observed in yeast or amphibians. Finally, this study was the first to show high degree periodicity in chromatin organisation at multiple length scales. More importantly, I show here clusters of DNA and various post-translational histone modifications in a very comprehensive way for the first time, demonstrating the importance of the meiotic chromosome as a model to study chromatin organization. The clusters are arranged according to their functional position, and provide the extend of chromatin compartmentalisation. As such, I at least identify a new type of functional compartment of 50 nm size (using H3K4me3) and another one of about 120 nm (using H3K27me3).

The three histone modifications summarising the clustering generated from the histone code table have different functionalities for the cell activity and exhibit a higher degree of specialization during meiosis. During development, H3K4me3 and H3K27me3 histone marks are present at promoters and have the capacity to turn on and off genes, respectively. As a result, these genes are in a bivalent state. Genes which become activated loose the H3K27me3 mark and start to get transcribed. In more differentiated stages of development, H3K4me3 guides transcription, while genes having only the H3K27me3 mark become totally repressed, eventually being rendered inaccessible via extreme compaction of chromatin [Pauler et al., 2009].

A histone modification associated to this kind of dense chromatin is H3K9me3, mainly associated with telomeric, repeats and satellite sequences [Mikkelsen et al., 2007]. The final picture of the epigenetic landscape of histone modifications can be simplified with a division between active genes displaying H3K4me3, inactive genes displaying H3K27me3 and inaccessible regions (rich in repeated elements) which bare a high density of H3K9me3 mark (Figure 4.10).

In highly differentiated cells such as non-renewable adult tissues, the relationship between epigenetic marks and gene expression is less pronounced, with many genes either up-regulated or down-regulated, which do not seem to exhibit any H3K27me3 or H3K4me3 modulation ([Wu et al., 2012], Epithelial-mesenchymal transition (EMT) data from David Fournier, not published), while many genes are kept totally silent during the entire life of the cell, with H3K27me3 spread all
along the gene body [Pauler et al., 2009]. As a result, the modulation of histone modification amplitude may play a special role in meiosis and possibly guide the structure of the chromosome.

As meiosis is the type of cell division that provides the basis for sexual reproduction and genetic variability, defects in synapsis and/or recombination of meiotic chromosome can lead to aneuploid syndromes and infertility. It is likely that the SC driven chromosomes have structurally distinct histone modifications patterns and a unique chromatin landscape compared to those identified here in the native state. This work also demonstrates the link between the structural hierarchy of chromatin organization in meiosis and epigenetic regulation of transcription.

I urge the scientists to use this model as a platform to study the epigenetic make-up of genomic regions of interest, and the basics of gene expression and epigenetic regulation. The meiotic chromosome, while being very specialized toward one goal, recombination, happens to be a promising candidate to study the fundamental principles that guide chromatin architecture.
5 Conclusions

5.1 Originality of the work presented here

In this thesis, I have shown the potential of single-molecule imaging to study chromatin architecture. The primary challenge was to systematically identify and characterise different building blocks of the chromatin organisation. Some elements were known since long, for example, the nucleosomes at the lowest level and the metaphase X-shaped chromosomes at the highest level of DNA compaction. In between these two extreme levels, a vast spectrum of structures remained mostly unexplored due to resolution limitation of light microscopy and lack of specificity in electron microscopy. Furthermore, an effort to combine and synchronise observations from different studies on chromatin organisation was lacking. This thesis is an attempt to combine old and new evidence to understand various structure-function conundrums of chromatin organisation and understand how chromatin structure affects gene regulation.

For genes to function properly, some fundamental structures must exist in a finite number. I speculate that these structures should be in a restricted size range and diversity. For instance, I found structural elements of about 100-400 nm probably corresponding to functional domains involved in activation or repression of transcription. After studying chromatin organisation at different phases of cell cycle, the following new patterns were described to refine the overall description of chromatin:

- patterns of chromatin in interphase: territories, subchromosomal domains (scale: 500 to 1000 nm), fundamental chromatin domains (scale: 100 to 500 nm) and chromatin fibres (scale: 30 to 100 nm).

- patterns of condensation during differentiation of cells, and more interestingly during stress: deprivation of oxygen and nutrients induces a characteristic ring/rod-like shape of chromosomes (scale: 40 to 700 nm).

- patterns of functional chromatin during meiosis (scale: 40 to 600 nm). Active chromatin localises laterally towards the exterior of pachytene chromosomes, likely facilitating transcription while inactive chromatin locates toward the interior showing a high level of periodicity and symmetry.
Further imaging at different scales should clearly identify patterns found to be associated with various nuclear phenotypes. Toward this, it will be more relevant to focus first on the strongest signals (Barr bodies, nucleolus) to generate certain rules and then go for the data of lower signals (autosomal chromosome territories, low-scale chromatin domains). Similarly to what has been used here, combined staining of DNA molecules and functional proteins, such as histone modifications, will help to characterise these structures in more depth. For instance, characterization of transcription during interphase will be essential. How many genes are transcribed during interphase and which structure chromatin is adopting? Model cells such as mesenchymal stem cells, whose chromocenters are associated to significant transcription, will be useful in these cases. For comparison, functional transcription machinery could be described in other interphase cells of lower transcription. Furthermore, information regarding building blocks of chromatin and the interplay between different hierarchical levels should be summarised in models to better understand the system under consideration. Dynamics of patterns should be determined in the light of various cell processes (either interphase steady state, cells in embryonic development, reaction to a stimulus). The SMLM method can be applied to many questions regarding chromatin organisation, for instance, it could investigate the difference of chromatin shape between the micronucleus and the macronucleus of the Tetrahymena.

The different findings are summarised in a model of chromatin architecture (Figure 5). The various cartoons represent different stages of the cell cycle. In each of them, two kinds of chromatin organisation are distinguished, one condensed and particularly folded, usually associated with gene silencing, and the other being loose chromatin, often related to active transcription. Interphase stage shows most of the condensed chromatin at the periphery of the nucleus, while active chromatin is in the centre. Upon stress (the cartoon on the top right), chromatin starts to condense in the shape of elongated patterns at the periphery of the nucleus while progressively, an extreme compact pattern of chromatin appears toward the centre, forming intriguing ring-shaped structures (middle right cartoon). Before beginning any cell division, whether mitosis or meiosis, cells have to double their genetic material. As a result, to maximise transcription, late S phase to G2 phase is associated with a pattern where the nucleus is made of islands of condensed chromatin (the chromocenters) and shows loose active chromatin located at the periphery of the chromocenters, maximising the surface of transcription. Prophase stage of cell division starts by the recruitment of chromocenters to the lamina, in order chromosomes to find more easily each other in the next steps of mitosis or meiosis (central cartoon). The chromocenters drag the active chromatin behind them, displaying a hair like pattern. Mitosis is the product of attachment of chromatin domains with the aid of condens-
ing polymers (bottom left cartoon). Meiosis is both a condensation process of chromatin (with the help of epigenetic regulators) and a polymerization process of synaptonemal complex proteins, which leads to the typical structure necessary for recombination (bottom right cartoon).

5.3 Limitations of the method and possible improvements

Many interrogations are brought by these findings. First of all, the exact physical mechanism for the powerful combination of 405/491 nm laser combination is unknown. The Jablonski diagram of such mechanism should be established based on appropriate physics methods. Improvement of imaging buffer should also follow a more thorough analysis. Usage of different redox agents, susceptible to improve the blinking of the fluorochrome molecules, should also be considered. Proper benchmarks between the DNA dyes and various combinations of fluorophore are still lacking and need to be set up. Most importantly is the comparison between the images generated by the SMLM methodology and other available high-resolution technologies on the same kinds of cells.

The randomness of some patterns at the lower level is still to be
investigated (for instance in the case of DNA imaging of interphase nuclei). This can be achieved by combining DNA staining with EdU for the detection of new synthesised DNA in the same cell to see if the worm-like patterns follow the elongated EdU clusters. Finally, different ways of analysing individual molecules could be done. For instance, what are the signals that blink exactly at the same position several times? How much blinking does one has per molecule for each DNA dye? Finally, a more thorough comparison between the different DNA dyes will be relevant for the community.

5.4 New avenues for the study of chromatin patterns during meiosis

Complementary techniques should determine which molecules provoke the epigenetic patterns found in meiotic chromosomes. Inhibition or genetic invalidation should confirm their structural roles. The functionality of the clusters observed during meiosis should be explored by association to functional components. For instance, double strand break positions could be characterised on the meiotic chromosome to see which epigenetic mark co- or anti-localize. Complementary biochemical analyses will strengthen the functionality. Mutation of enzymes depositing the marks will provide more information regarding the assembly of epigenetically regulated clusters. Finally, the different stages of meiosis shall be characterised to have a dynamic picture of the epigenetic regulation and the way different patterns are formed.

5.5 Enlarging the spectrum of questions: chromatin organisation as a fundamental principle of nucleus formation

How do chromatin clusters form? Do sequences follow a pre-labelling, for instance via histone modifications, before being put together in a single cluster? Meiotic chromosomes seem to be an example platform to test this structure-to-function relationship. Contrary to interphase chromatin, meiotic chromatin is so well defined that there is potentially little overlap between different epigenetic domains and so a significant potential for isolating domains in further analyses. I also ask the following questions: How does chromatin shape changes during development? Are there defined chromosome territories positions in early phases of embryogenesis? How epigenetics relate to gene expression? All these dynamics are crucial to the understanding of fundamental genomic processes and will benefit from an unbiased, naive and structural analysis such as the ones presented in this work.
Appendices
Appendix A

Figure A.1: Areas and single molecule localisation of inter-chromosomal territories. Chromatin data have been arbitrarily thresholded based on the density of SM localizations and divided into two classes: interchromatin compartments (IC) and chromatin occupied regions. Then the areas and single molecule localization density were quantified. On average, IC displayed about 4 times less DNA-associated signals. However, some regions within IC displayed much lower DNA-associated signal (indicated with squared regions) [Zurek-Biesiada et al., 2015].

Figure A.2: Comparison between objects found in microscopy and genomics. Left panel: model of chromosome territories and their sub-domain, from [Cremer and Cremer, 2001], using information from a conventional light microscope. Right panel: size of functional regions of the genome (chromatin domains), modified from [Rao et al., 2014], generated after analysis of data from HiC.
Figure A.3: HiC data at various levels of resolution. The chromosome 14 (approx $10^8$) is partitioned into bins of 10000 (A), 40000 (B), 66000 (C), 100000 (D) pixels. The figure shows that at a higher order or scale there is a large number of intra-chromosomal interactions on the chromosome 14, however when we start to bin the chromosome into pixels of smaller size these interactions start to vanish.

Figure A.4: A comparison between images of mitotic chromosome DNA recorded using wide field or high-resolution condition. (A) chromosomes in anaphase, imaged by wide-field (bottom) and super-resolution localization microscopy (top). (B) an inset presenting chromosomes visualized with wide-field. (C) chromosomes shown in panel B imaged by super-resolution localization microscopy. Data points were blurred with using the value of their respective localization precisions (see Chapter 2). (D) point representation of single molecules blurred in (C).

Figure A.5: Replicates of the results presented in figure 1.21.
Figure A.6: Fourier Ring Correlation (FRC) analysis of DNA/SMLM data (Figure and caption modified from [Kirmes et al., 2015]). A) Representative normalised FRC curves for untreated, OND, and in recovering cells. The red horizontal line designates the $1/7$ threshold of the radially integrated Fourier frequencies in accordance with [Nieuwenhuizen et al., 2013]. B) Resolution estimates across all experimental conditions based on the threshold determined in A.
Appendix B

Figure B.1: Relative localization of SYCP3 and SYCP1 within the synaptonemal complex. Single molecule localization images of SYCP3 labelled with Alexa 488 (A) and SYCP1 C-terminus labelled with Alexa 555 (B). (C) Dual color image of SYCP3 and SYCP1. Insets in A and B highlight the double strand nature of SYCP3 and SYCP1, respectively. (D) shows an relative outline structure of SYCP3 and SYCP1.

Figure B.2: Validation of the chromatin clusters (figure and caption modified from [Prakash et al., 2015]). In order to validate the clusters found in the SMLM image of DNA (A), I compared it to a randomly simulated dataset (B). I generated a binary mask of the nearest neighbour blurred image and then randomly generated a number of points identical to the SMLM image. (C) The local condensation in SMLM and random images was characterised by detecting the 20-500 nearest neighbours. In each case the mean nearest neighbour distance was found to be significantly shorter than in the random simulated data-set. The mean distance to the 500 nearest neighbour was 86 nm for chromatin and 110 nm for the random data.
the periodic and dynamic structure of chromatin

Figure B.3: SEM data validate the pattern of chromatin found with SMLM. Chromatin shows a caterpillar-shape, with several ring-shape clusters found successively along the SC, similar to Figure 4.6B. Courtesy Wioleta Dudka.

Figure B.4: Chromatin rearrangement upon condensation. After G2 phase chromatin starts to condense around a scaffold of proteins and to achieve a maximal compaction. This moves the silent and inaccessible regions toward the interior while the loose and active chromatin goes toward the exterior, making chromatin accessible for transcription. Three different scenarios exemplifying this transition is shown in (A) meiotic chromatin at the pachytene stage in mouse, (B) organisation of polytene chromosomes in Drosophila and (C) organisation of mitotic chromosomes in anaphase.

Figure B.5: Helical structure of the pachytene chromosomes using information from H3K27me3 clusters. (A) SMLM image of H3K27me3 labelled with Alexa 488. (B) SMLM image of SYCP3 labelled with Alexa 555. (C) Two color SMLM image of H3K27me3 and SYCP3. (D) Clusters of H3K27me3 are highlighted in different colours to reveal an helicoidal structure. Twists of SYCP3 of same order as the H3K27me3 clusters are also observed (C). The size of clusters follows the trend found computationally. Periodicity of twists is close to 500nm. Scale bar: 1000 nm.
Figure B.6: Spiralization of H3K9me3 confirmed by patterns of DNA (figure and caption modified from [Prakash et al., 2015]). Dense DNA clusters seem to spiral at one of the ends of the SC, confirming the spiralization patterns of H3K9me3 found in Figure 4.11. The average spread of DNA (A1) is around 500 nm. The cluster diameter in (A) was found to be 223 nm. (A2) shows the histogram of the tangential distances taken along the central axis of SYCP3. Chromatin clusters were found to occur with a periodicity of 685 nm (A3). The blue lines in the plot correspond to the 95 percent confidence bounds (+/- 0.08) of the autocorrelation function.
Figure B.7: Helicoidal nature of the pachytene chromosomes. Pairs of pachytene chromosomes reminiscent from the \textit{in situ} state of chromatin are displayed. Note that the helicoidal aspect of the paired chromosomes (left) are similar to the one of the solitary chromosome (right).
Figure B.8: SYCP3 strands move apart at non-centromeric end of the SC. The centromeric ends of SYCP3 seem to be closer to each other than the non-centromeric end of SYCP3 (A and B). The average distance at the centromeric end in A and B is found to be 142 nm and 130 nm respectively, while the average distance at the non-centromeric end is 171 nm and 190 nm respectively (A1 and B1). H3K9me3 is normally distributed at the centromeric end (figure and caption modified from [Prakash et al., 2015]).

Figure B.9: Characteristics of the epigenetic clusters identified to regulate pachytene chromosomes.
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"We have a habit in writing articles published in scientific journals to make the work as finished as possible, to cover all the tracks, to not worry about the blind alleys or to describe how you had the wrong idea first, and so on. So there isn’t any place to publish, in a dignified manner, what you actually did in order to get to do the work.”

Richard Feynman

Publications

In peer reviewed journals

1. Single molecule localization microscopy of the distribution of chromatin using Hoechst and DAPI fluorescent probes

   - **Authors:** Szczurek*, Aleksander T, Prakash*, Kirti, Lee*, Hyun-Keun, Żurek-Biesiada, Dominika J, Best, Gerrit, Hagmann, Martin, Dobrucki, Jurek W, Cremer, Christoph and Birk, Udo
     * first co-authors
   - **Description:** In this report, we demonstrate that DNA minor groove binding dyes, such as Hoechst and DAPI, can undergo UV-induced photoconversion, to be effectively employed in single molecule localization microscopy (SMLM) with high optical and structural resolution.
   - **Journal:** Nucleus 2014 (cover page)
   - **Author contributions:** K.P., C.C., and U.B. initiated the project. A.S., H-K.L., K.P., and D.Z-B. designed the experiments. A.S. prepared the samples and performed the single-molecule measurements. H-K.L., K.P., C.C., and U.B. developed and constructed the microscopy apparatus. K.P., G.B., M.H., and U.B. contributed to the software used for data analysis. D.Z. performed the confocal experiments. K.P., A.S., H-K.L., G.B., and M.H. performed the data analysis. C.C., J.D., and U.B. supervised the work. All authors contributed in writing of the manuscript.
   - **Web:** http://www.tandfonline.com/doi/pdf/10.4161/nucl.29564

2. Superresolution imaging reveals structurally distinct periodic patterns of chromatin along pachytene chromosomes

   - **Authors:** Prakash, Kirti, Fournier, David, Redl, Stefan, Best, Gerrit, Borsos, Máté, Tiwari, Vijay K, Tachibana-Konwalski, KiKuë, Ketting, René F, Parekh, Sapun H, Cremer, Christoph, Birk Udo J.
   - **Description:** In this study, we found that chromatin is non-randomly distributed along the length of the synaptonemal complex (SC, thick axial gray lines). Active chromatin (H3K4me3) emanates radially in loop like structures (red dots) while the repressive chromatin (H3K27me3) is confined to axial regions (green balls) of the SC. Centromeric chromatin (H3K9me3) hints at spiralization of DNA at one of the extremities of SC (blue lines at the top).
complex (SC) and displays differential condensed clusters. Chromatin structure is further divided into different functional compartments using histone modifications. Taking into account the arrangement and composition of chromatin, as well as the region-specific distribution of post-translational histone modifications, we discuss a model of the chromatin architecture along the length of the SC. This study is a successful application of our newly developed SMLM method applied to DNA dyes.

- **Journal:** Proceedings of the National Academy of Sciences (PNAS) 2015
- **Author contributions:** K.P. designed research; K.P. and S.R. performed research; K.P., S.R., G.B., M.B., V.T., K.T.-K., R.K., S.P., C.C., and U.B. contributed new reagents/analytic tools; K.P. and D.F. analysed data; K.P. and D.F. wrote the paper with input from all the other authors.
- **Web:** [http://www.pnas.org/content/112/47/14635.short](http://www.pnas.org/content/112/47/14635.short)

3. A transient ischemic environment induces reversible compaction of chromatin

- **Authors:** Kirmes, Ina, Szczurek, Aleksander, Prakash, Kirti, Charapitsa, Iryna, Heiser, Christina, Musheev, Michael, Schock, Florian, Fornalcyz, Karolina, Ma, Dongyu, Birk, Udo, Cremer, Christoph and Reid, George

- **Description:** Using SMLM, we evaluated the environmental effects of ischemia on chromatin nanostructure. We found short-term oxygen and nutrient deprivation (OND) of the cardiomyocyte cell-line HL-1 induces a dramatic and reversible compaction. Chromatin adapts to a previously undescribed sub-nuclear configuration comprising of discrete, DNA dense, hollow, atoll-like structures, which upon removal of transient ischemic-like conditions, reverses to the open structure in untreated cells.

- **Journal:** Genome Biology 2015
- **Author contributions:** C.C. and G.R. conceived of the study and designed the experimental strategy. I.K., A.S., C.H., I.C., M.M., D.M. and K.F. performed experiments. I.K., A.S., K.P., F.S., M.M., U.B. and G.R. analyzed data. U.B. prepared the movie. U.B., C.C. and G.R. supervised this project. G.R. wrote the paper and coordinated the supplemental information. All authors discussed the results and contributed to the manuscript. All authors read and approved the final manuscript
- **Web:** [http://www.genomebiology.com/2015/16/1/246](http://www.genomebiology.com/2015/16/1/246)

4. Localization microscopy of DNA in situ using Vybrant® DyeCycle Violet fluorescent probe: A new approach to study nuclear nanostructure at single molecule resolution
Authors: Żurek-Biesiada, Dominika, Szczurek, Aleksander T, Prakash, Kirti, Mohana, Giriram K, Lee, Hyun-Keun, Roignant, Jean-Yves, Birk, Udo, Dobrucki, Jurek W and Cremer, Christoph

Description: We report here that the standard DNA dye Vybrant® Violet can be used for chromatin imaging using SMLM and helps to describe the nanoscale structure of chromatin. This technique enabled the localisation of a large number of DNA-bound molecules, usually resulting in an excess of $10^6$ signals in a ~ 500 nm optical section of a cell nucleus.

Journal: Experimental Cell Research 2015

Author contributions: D.Z-B. and A.S. planned the experiments. D.Z-B. and A.S. performed the experiments, drafted and revised the manuscript, D.Z-B., K.P. and A.S. performed image data reconstruction. G.K.M. prepared polytene chromosome samples, J.Y. R., U.B., J.D., C.C. supervised the work and contributed to writing the manuscript.


5. Quantitative super-resolution localization microscopy of DNA in situ using Vybrant® DyeCycle Violet fluorescent probe

Authors: Żurek-Biesiada, Dominika, Szczurek, Aleksander T, Prakash, Kirti, Gerrit Best, Mohana, Giriram K, Lee, Hyun-Keun, Roignant, Jean-Yves, Birk, Udo, Dobrucki, Jurek W and Cremer, Christoph

Description: In this manuscript, parameters that influence the quality of SMLM reconstruction using Vybrant DyeCycle Violet, for instance number of frames, wave length or composition of buffer, are investigated, using quantifications and experimental methods.

Journal: Data in Brief 2016

Web: http://dx.doi.org/10.1016/j.dib.2016.01.041
In conferences

1. Identify and localise: Algorithms for single molecule localisation microscopy

- **Authors:** Kirti Prakash*, Gerrit Best*, Martin Hagmann, Udo Birk, and Christoph Cremer.
  * first co-authors
- **Description:** Here, we present a comparative analysis of a range of available localisation algorithms regarding their complexity, applicability and performance by testing them on both synthetic and experimental data. Experimental data come from both sparse and dense regions, with low and high background levels, to determine which method is suited for a given dataset.
- **Conference:** International Microscopy Congress (IMC) 2015
- **Author contributions:** K.P. designed research, performed research and analysed the data. K.P. and G.B. wrote the code.
- **Web:** [http://www.imc2014.com](http://www.imc2014.com)

2. Drift correction strategies for superresolution imaging modalities

- **Authors:** Martin Hagmann*, Kirti Prakash*, Rainer Kaufmann, Udo Birk and Christoph Cremer.
  * first co-authors
- **Description:** We present two drift correction strategies based solely on acquired data without any fiducial markers. Using both approaches we successfully corrected localization microscopy data down to a final drift under 5 nm. We demonstrate that with this procedure the resolution of the final reconstructions was substantially enhanced.
- **Conference:** International Microscopy Congress (IMC) 2015
- **Author contributions:** K.P. and M.H. designed research, performed research and analysed the data.
- **Web:** [http://www.imc2014.com](http://www.imc2014.com)

3. Superresolution imaging of meiosis prophase I chromatin in pachytene stage.

- **Authors:** Kirti Prakash, Gerrit Best, Mate Borsos, Stefan Redl, Kikue Tachibana-Konwalski, Rene Ketting, Sapun Parekh, Udo Birk, and Christoph Cremer
- **Description:** We combined single molecule localisation microscopy with next generation sequencing data and computer simulations to map and analyse the distribution of chromatin and several of its post-translational modifications along the lateral elements of the SC.
- **Conference:** Focus On Microscopy (FOM) 2015
4. Lampbrush-like structures in mammalian meiotic chromosomes

**Authors:** Kirti Prakash

**Description:** Lampbrush chromosomes (LBC) are transcriptionally active chromosomes found in meiosis prophase I of most animals, except mammals. In LBC, chromosomes adapt special loop-like structures that emanate radially from the axis of the chromosomes, most likely to facilitate transcription. These loops have never been observed previously in mammals, somatic cells or diploid. Here, it is shown for the first time that mammalian chromosomes with clusters of transcriptionally active chromatin show patterns similar to the amphibian LBC.

**Conference:** Nuclear Organization and Function, CSHL 2016

**Web:** [https://meetings.cshl.edu/meetings.aspx?meet=NUCLEUS&year=16](https://meetings.cshl.edu/meetings.aspx?meet=NUCLEUS&year=16)
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Kirti Prakash